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INFORMATIK  
Faculty of Informatics



SECURITY &  
PRIVACY  
GROUP

# Foundations and tools for the static analysis of Ethereum smart contracts

Matteo Maffei and Clara Schneidewind

# Outline

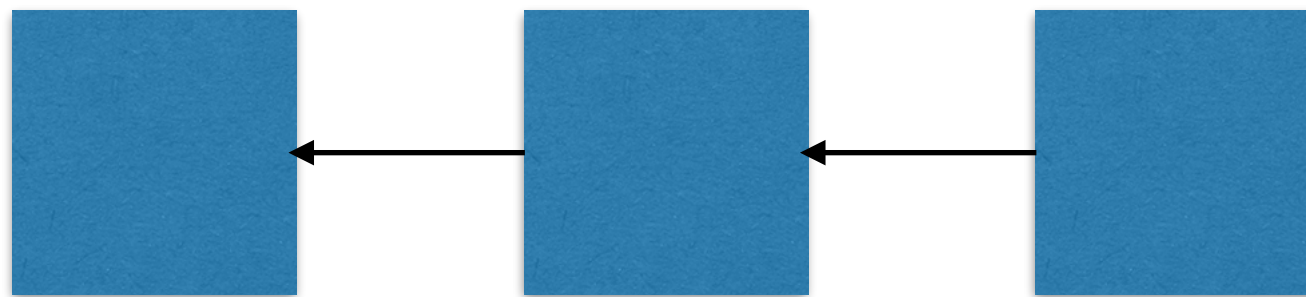
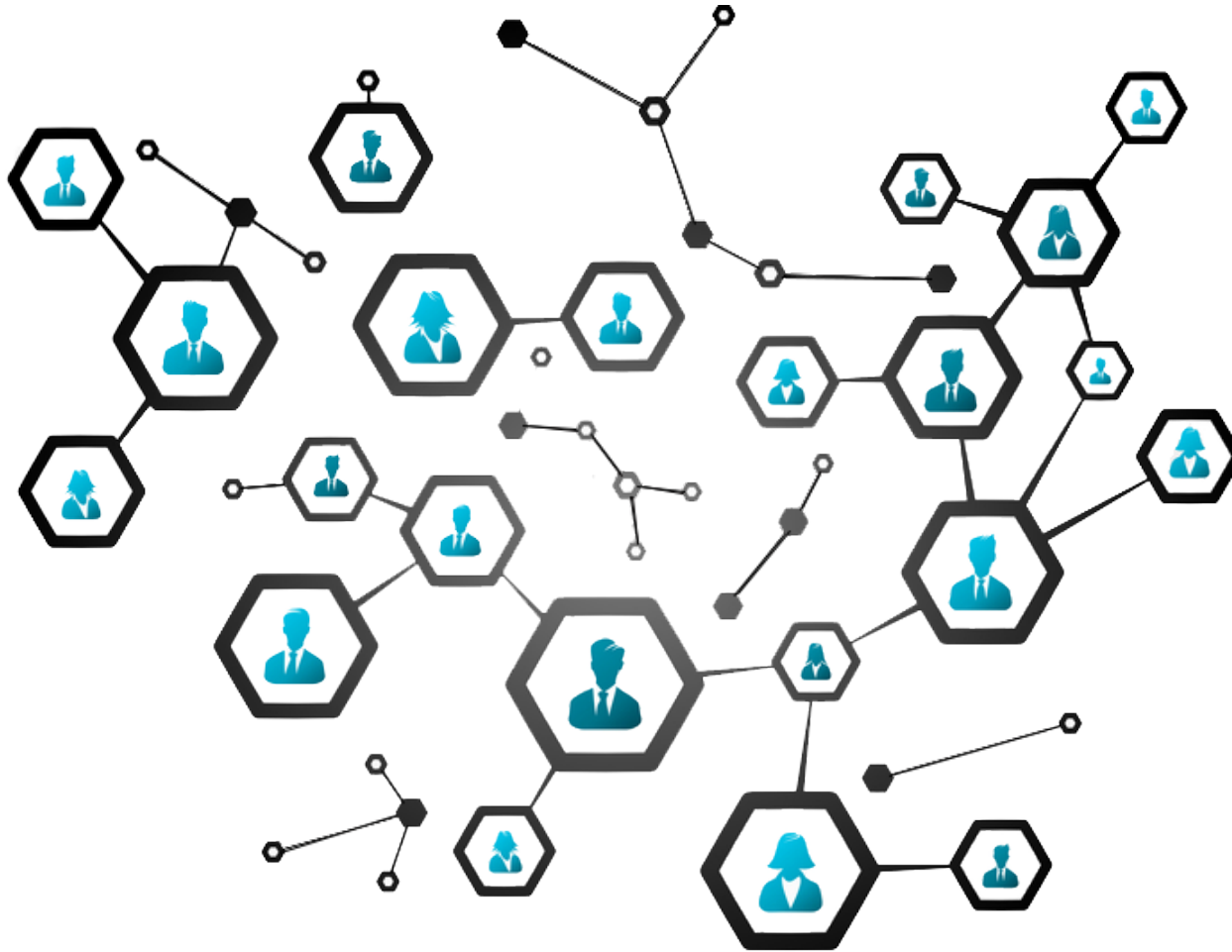
Introduction to Ethereum

Semantics of EVM bytecode

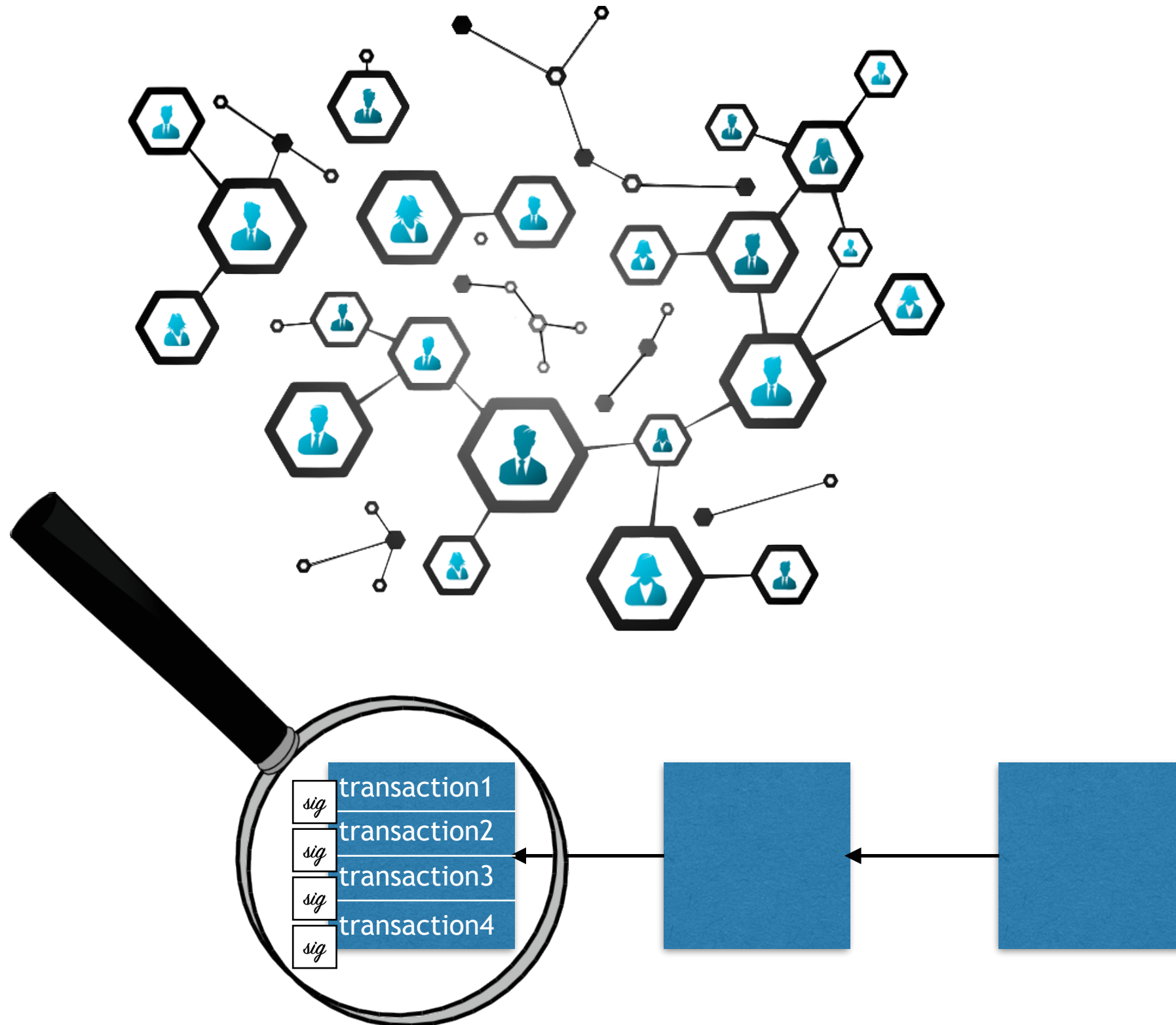
Static Analysis of EVM bytecode



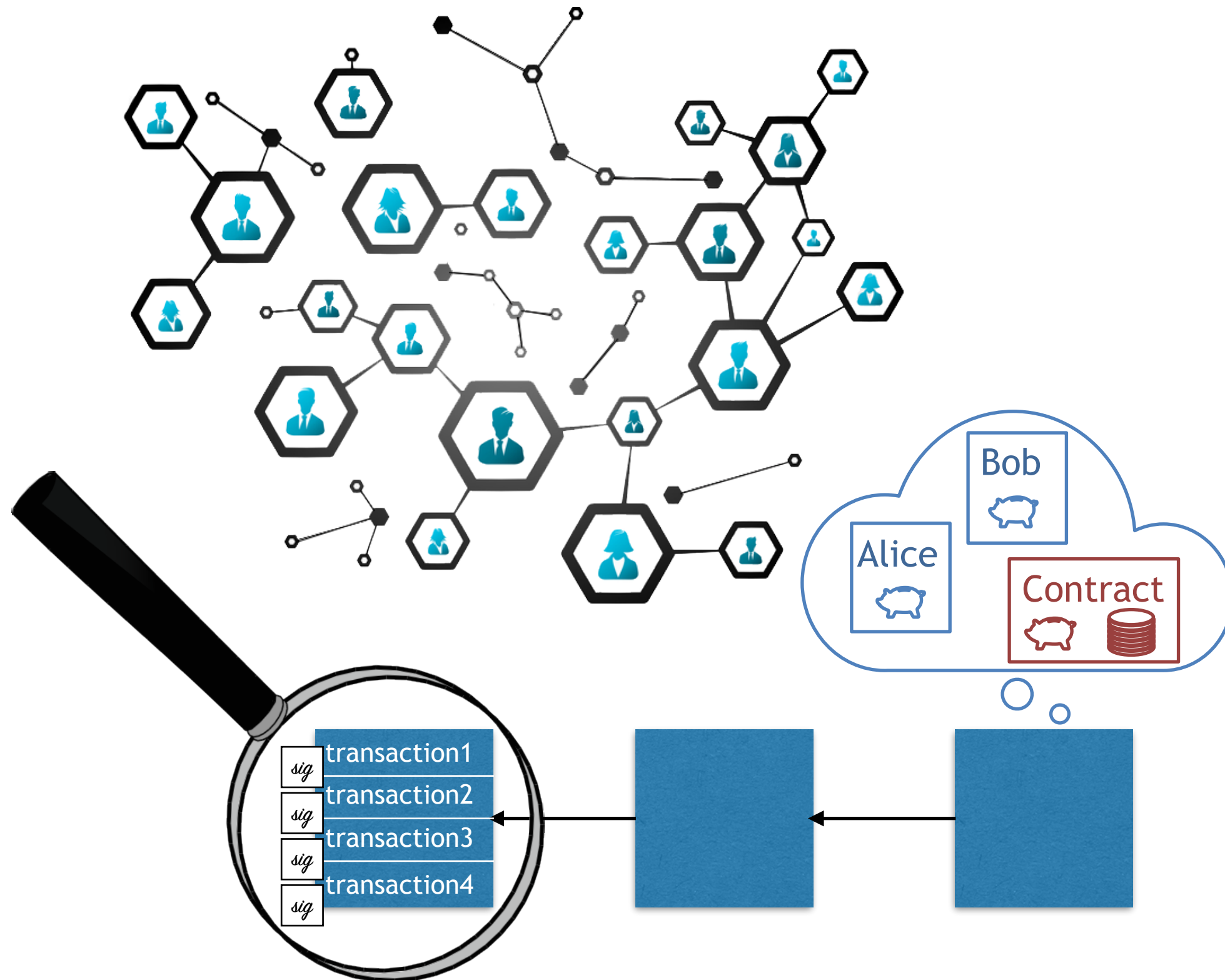
# Blockchain - an overview



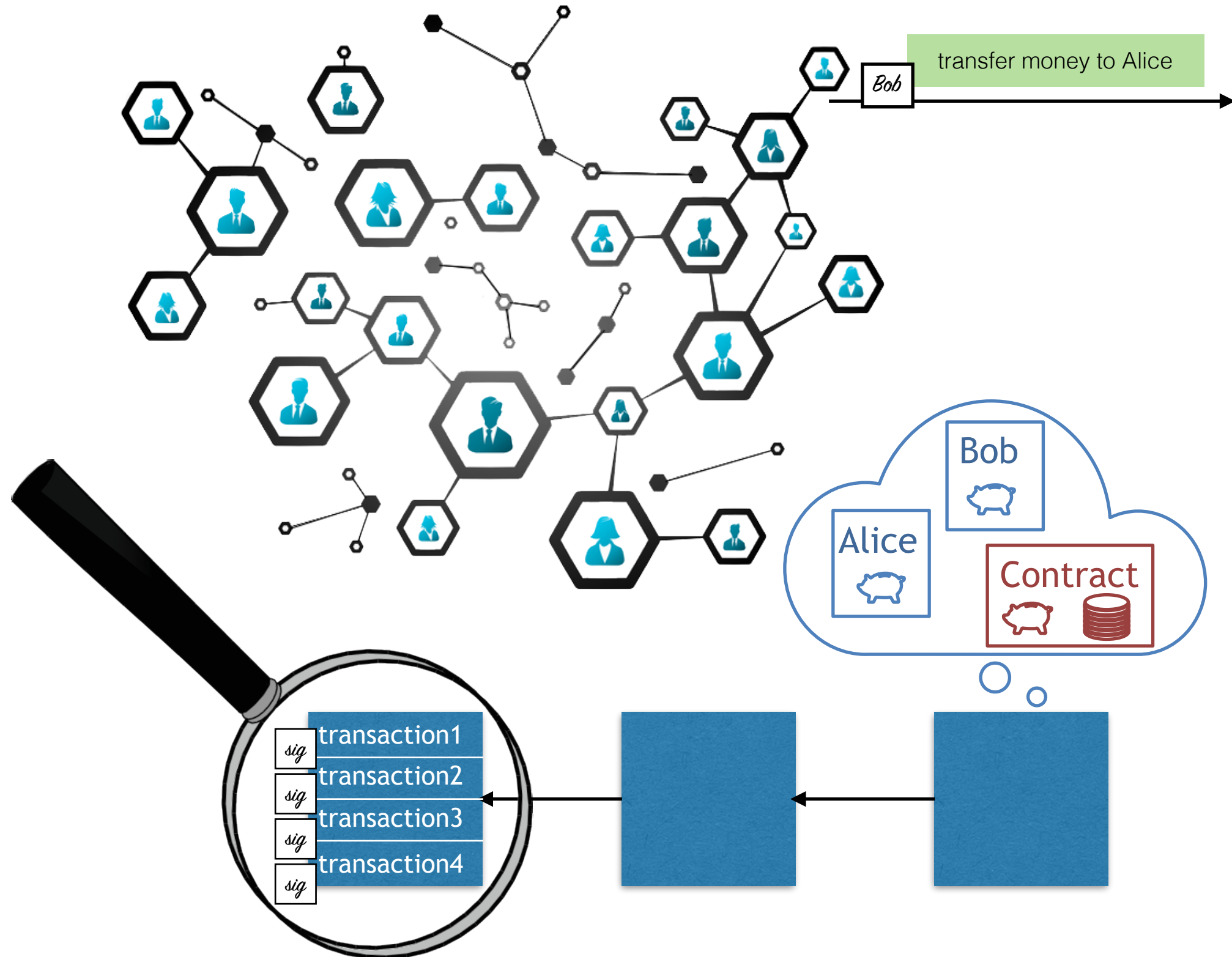
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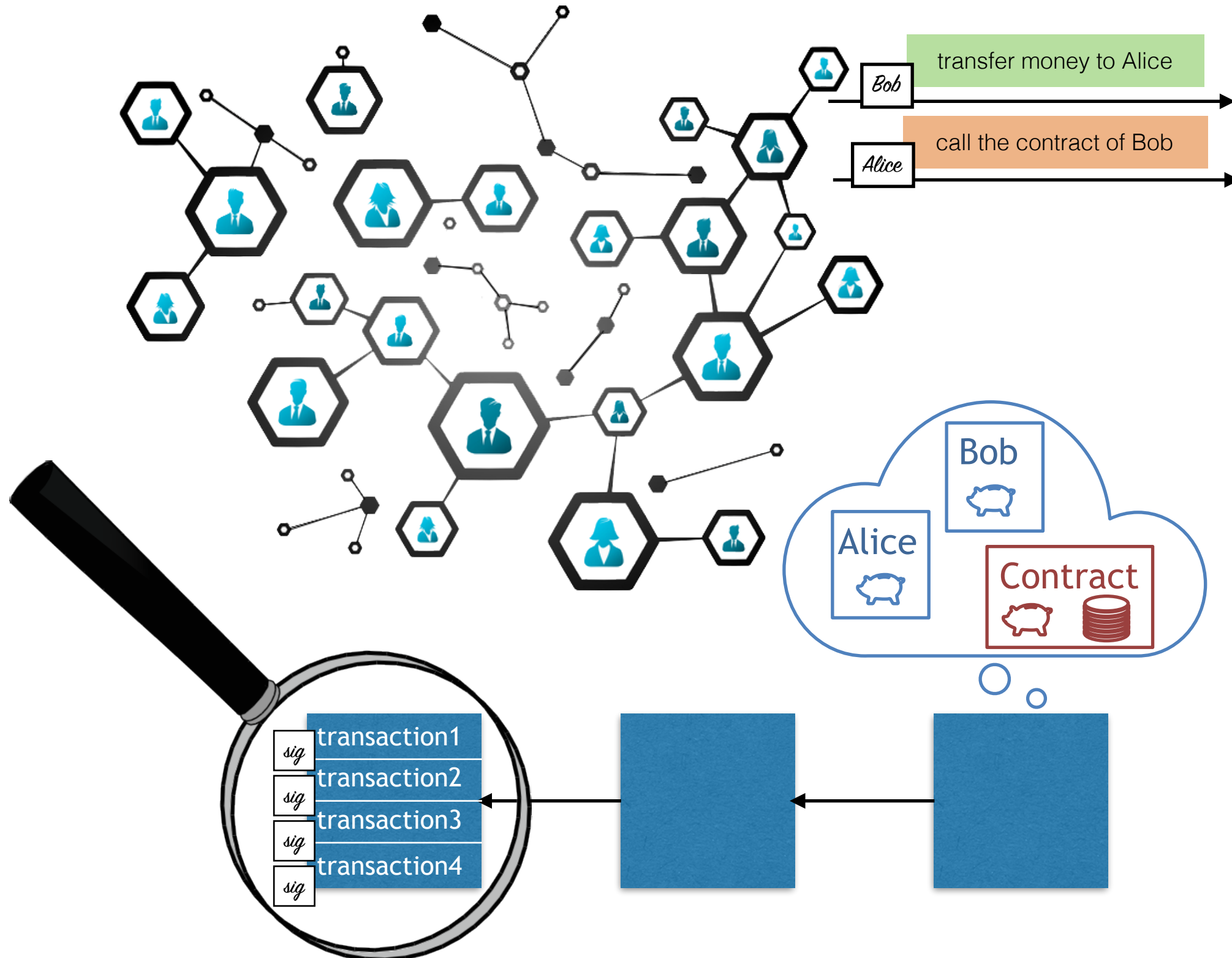


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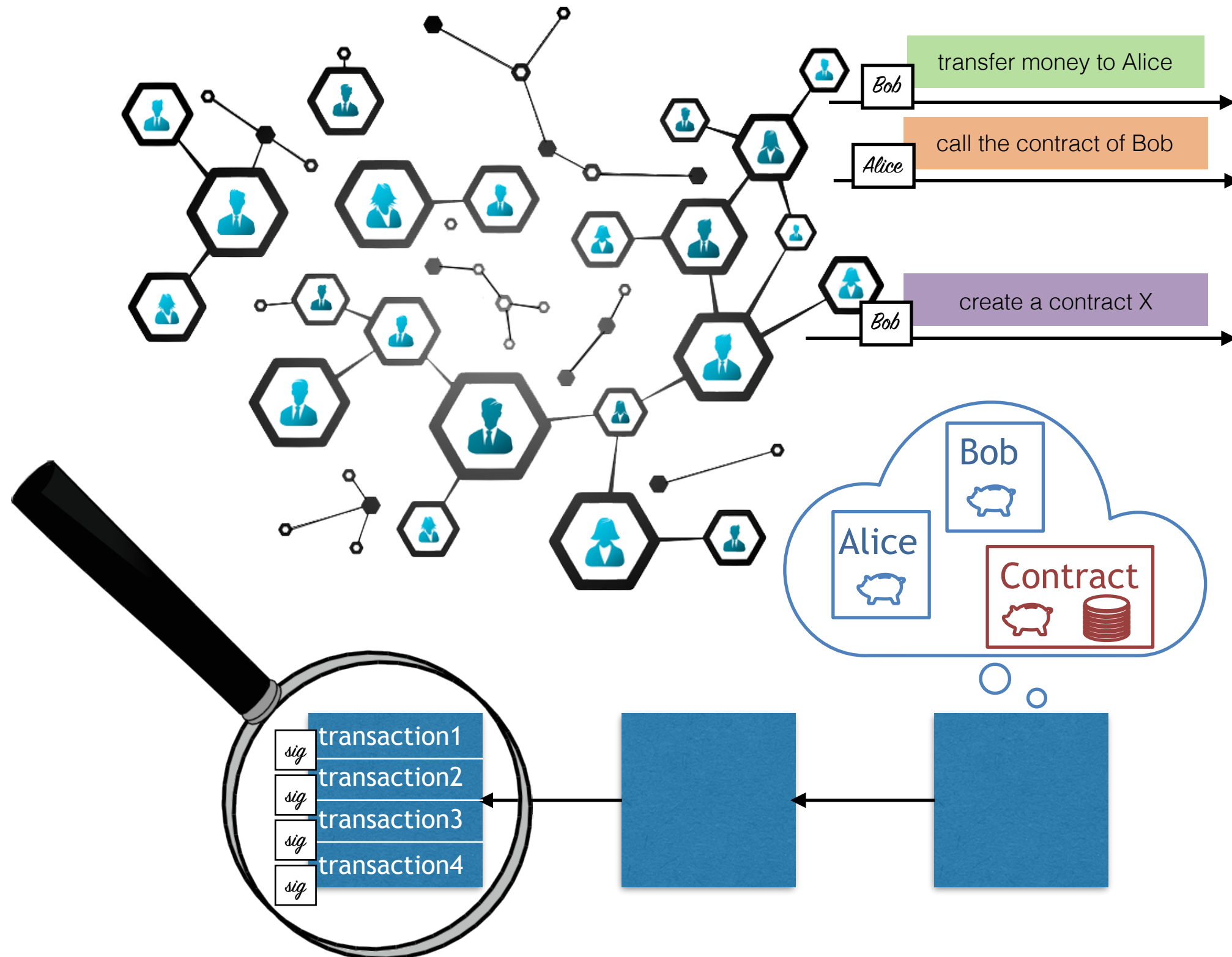




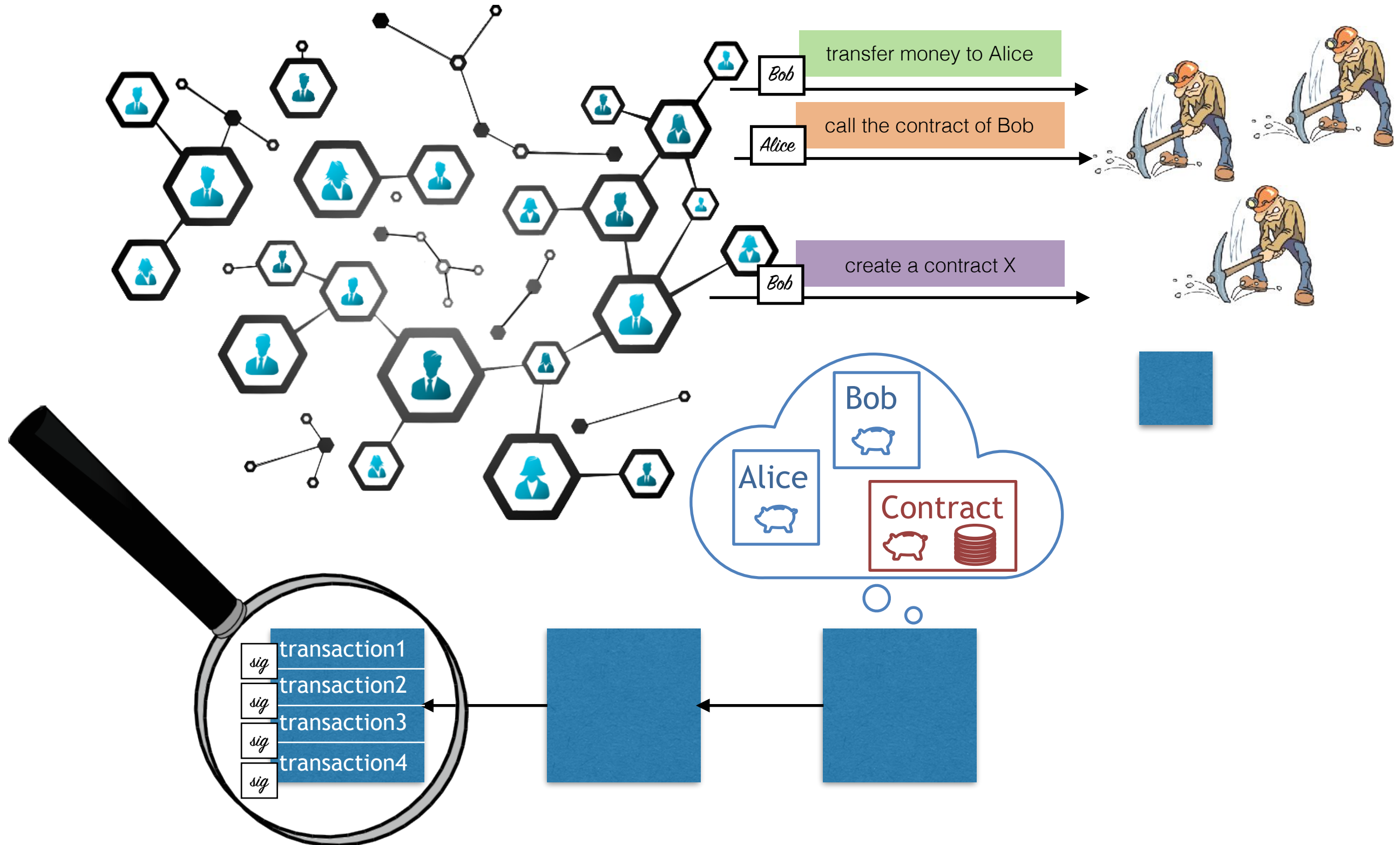
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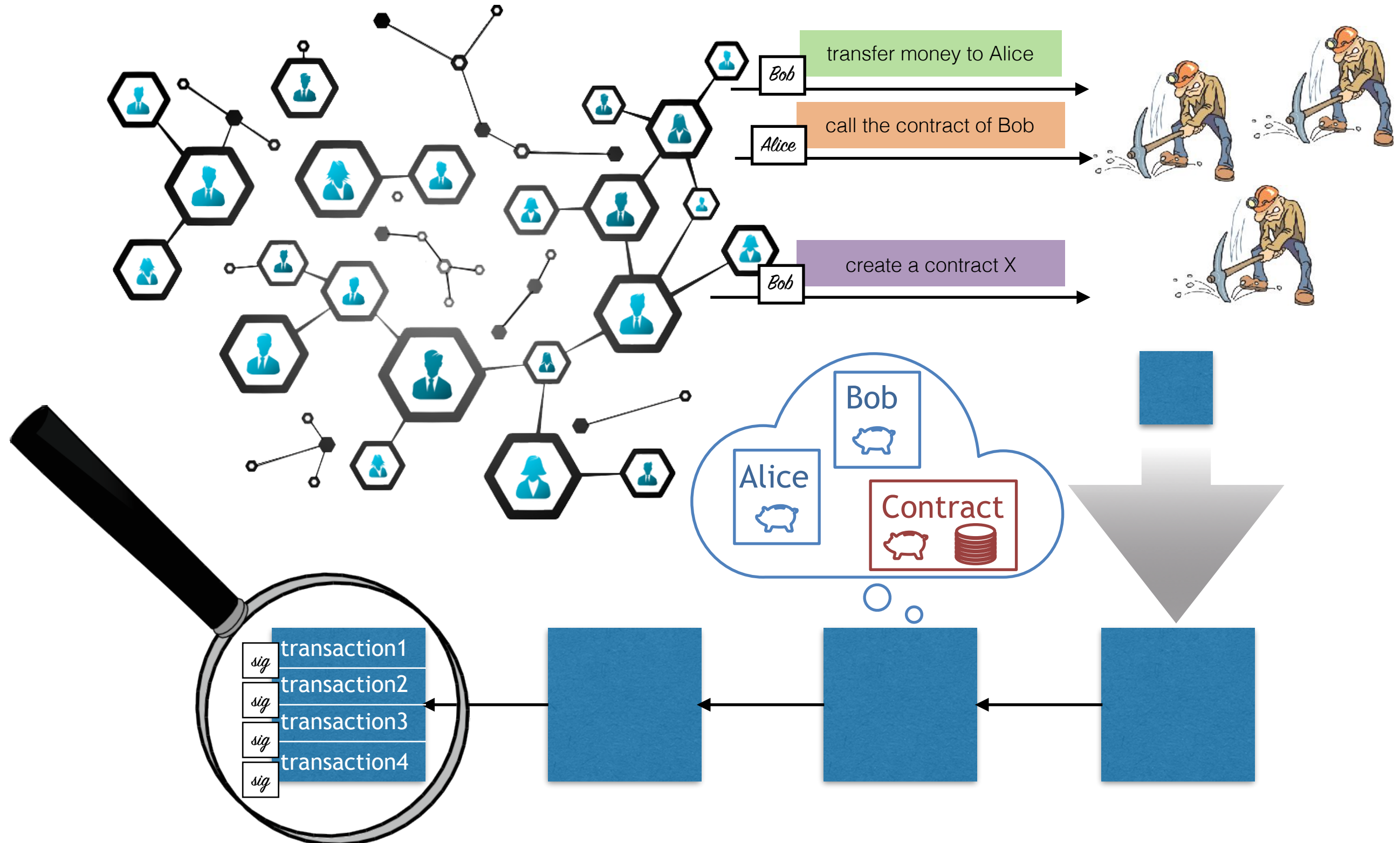
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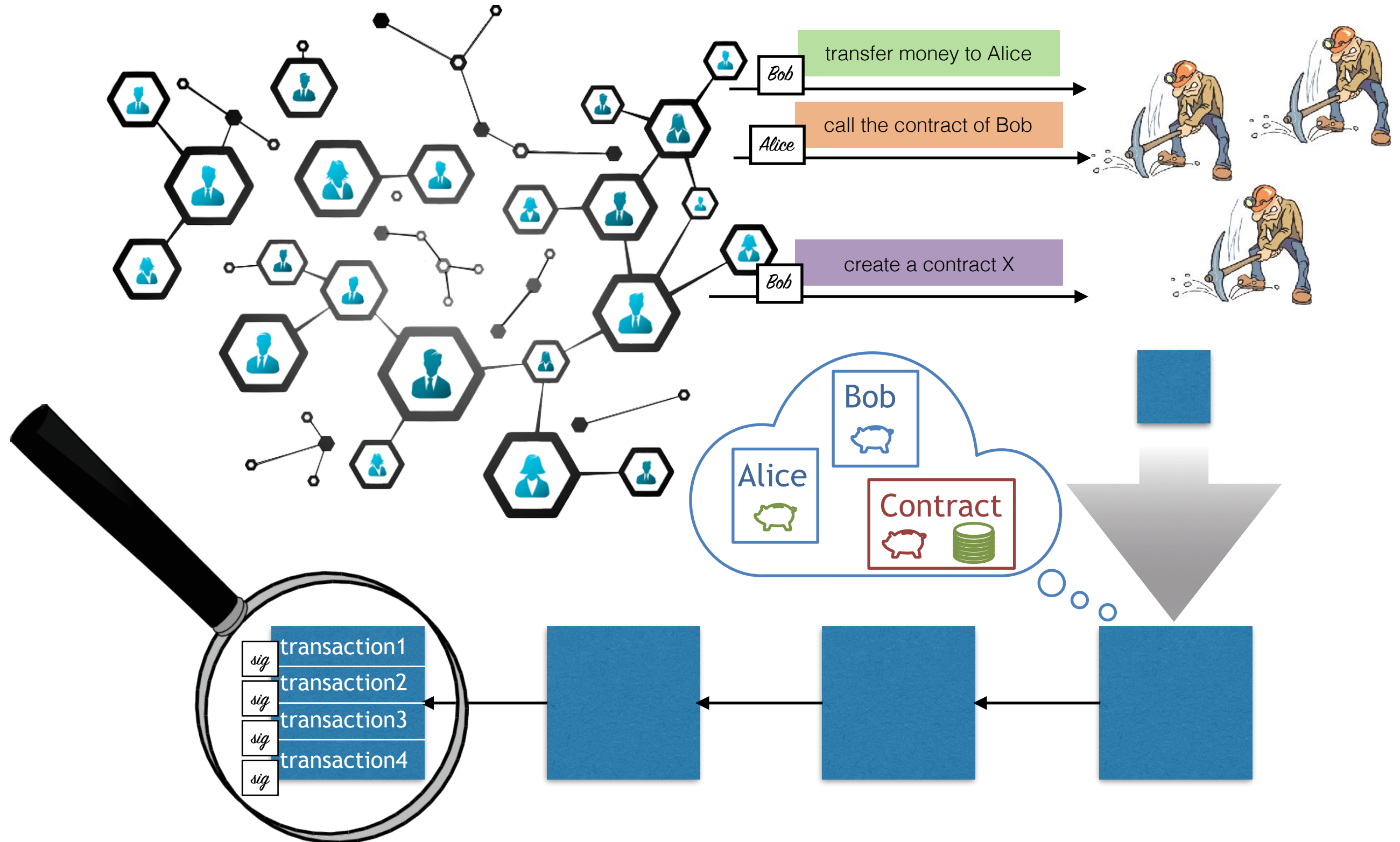


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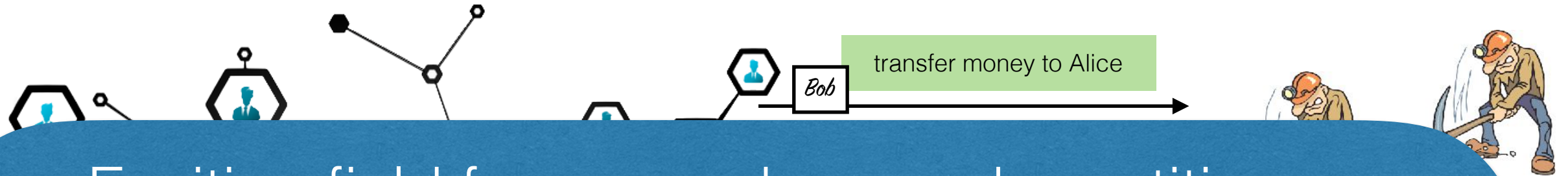




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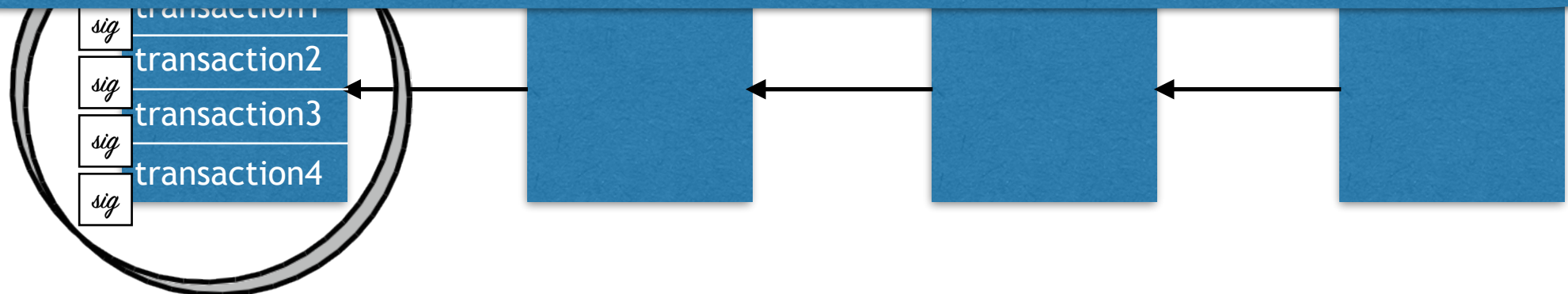
# Blockchain - an overview



Exciting field for researchers and practitioners

Three layer architecture: programs, consensus, network

All of that works by a fascinating combination of game theory, probabilistic consensus, cryptography, and programming language semantics



# Motivation

BLOCKCHAIN

## Blockchain-based Venture Capital Fund Hacked for \$60 Million

David Z. Morris

Jun 18, 2016



News emerged Friday that The DAO, a venture capital fund operating through a decentralized blockchain inspired by Bitcoin, had been robbed of more than \$60 million worth of Ether digital currency, or about 1/3 of its value, through a code exploit. The DAO, which [raised more than \\$150 million in May](#), had been intended as a showcase for the potential of Ethereum, a blockchain platform for cloud-based financial agreements.

The nature of the hack was outlined in an open letter [claiming to be from the attacker](#), posted to Pastebin this morning. In part, it reads:



# Motivation

BLOCKCHAIN

## Blockchain-based Venture Capital Fund Hacked for \$60 Million

David Z. Morris  
Jun 18, 2016

News emerged that a blockchain-based venture capital fund operating the DAO, which had been robbed of \$60 million in Ether, or digital currency, on June 17. The fund, which was intended as a platform for decentralized autonomous organizations (DAOs), was hacked.

The nature of the attack is still unclear, but it appears to be from the same source as the Parity bug. The fund's reads:



coindesk

Blockchain 101

Technology

Markets

Business

Data & Research

Consensus

Tickets are selling fast. Register for Consensus today!



## Parity Team Publishes Postmortem on \$160 Million Ether Freeze



# Motivation

## Parity Multisig Hacked. Again

Yesterday, Parity Multisig Wallet was hacked again:

<https://paritytech.io/blog/security-alert.html>

*“This means that currently no funds can be moved out of the [ANY Parity] multi-sig wallets”*

A lot of people/companies/ICOs are using Parity-generated multisig wallets.  
**About \$300M is frozen and (probably) lost forever.**

Disclaimer: I lost little money (about \$1000) but my friends lost about \$300K.

reads:



**Parity Team Publishes Postmortem on  
\$160 Million Ether Freeze**

# Motivation

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## A survey of attacks on Ethereum smart contracts

Nicola Atzei, Massimo Bartoletti, and Tiziana Cimoli

Università degli Studi di Cagliari, Cagliari, Italy  
{atzeinicola,bart,t.cimoli}@unica.it

**Abstract.** Smart contracts are computer programs that can be correctly executed by a network of mutually distrusting nodes, without the need of an external trusted authority. Since smart contracts handle and transfer assets of considerable value, besides their correct execution it is also crucial that their implementation is secure against attacks which aim at stealing or tampering the assets. We study this problem in Ethereum, the most well-known and used framework for smart contracts so far. We analyse the security vulnerabilities of Ethereum smart contracts, providing a taxonomy of common programming pitfalls which may lead to vulnerabilities. We show a series of attacks which exploit these vulnerabilities, allowing an adversary to steal money or cause other damage.

### 1 Introduction

The success of Bitcoin, a decentralised cryptographic currency that reached a capitalisation of 10 billions of dollars since its launch in 2009, has raised considerable interest both in industry and in academia. Industries — as well as national governments [48, 55] — are attracted by the “disruptive” potential of the *blockchain*, the underlying technology of cryptocurrencies. Basically, a blockchain is an append-only data structure maintained by the nodes of a peer-to-peer network. Cryptocurrencies use the blockchain as a public ledger where they record all the transfers of currency, in order to avoid double-spending of money.

Although Bitcoin is the most paradigmatic application of blockchain technologies, there are other applications far beyond cryptocurrencies: e.g., financial products and services, tracking the ownership of various kinds of properties, digital identity verification, voting, *etc.* A hot topic is how to leverage on blockchain technologies to implement *smart contracts* [34, 54]. Very abstractly, smart contracts are agreements between mutually distrusting participants, which are automatically enforced by the consensus mechanism of the blockchain — without relying on a trusted authority.

The most prominent framework for smart contracts is Ethereum [32], whose capitalisation has reached 1 billion dollars since its launch in July 2015<sup>1</sup>. In Ethereum, smart contracts are rendered as computer programs, written in a Turing-complete language. The consensus protocol of Ethereum, which specifies how the nodes of the peer-to-peer network extend the blockchain, has the goal

<sup>1</sup> <https://coinmarketcap.com/currencies/ethereum>

# Smart Contracts

- Typically written in Solidity (weird JavaScript variant)
- New languages are emerging (weird Python variant)

```
contract SimpleStorage {  
    uint storedData;  
  
    function set(uint x) {  
        storedData = x;  
    }  
  
    function get() constant returns (uint retVal) {  
        return storedData;  
    }  
}
```

- Uploaded on the blockchain as EVM bytecode

```
PUSH1 0x01  
PUSH1 0x60  
MSTORE  
PUSH1 0x20  
PUSH1 0x40  
PUSH1 0x01  
PUSH1 0x60  
PUSH1 0x00  
PUSH32 0x0318247CB34f134f3cF49E97647227dc2D75Abe8  
GAS  
CALL
```

# Overview on Ethereum



# Overview on Ethereum

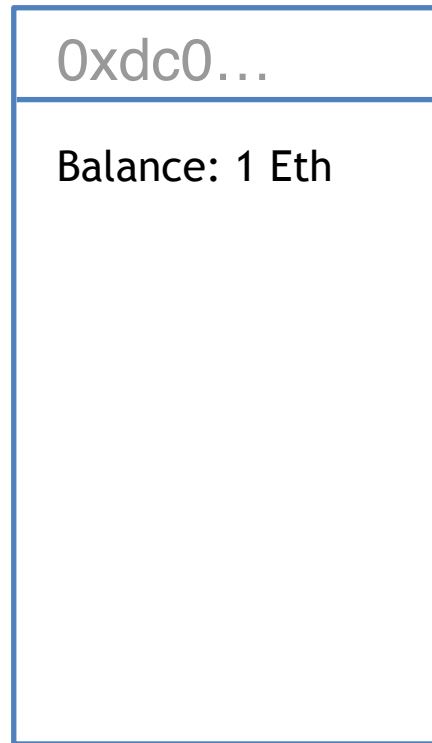
External Account

0xdc0...

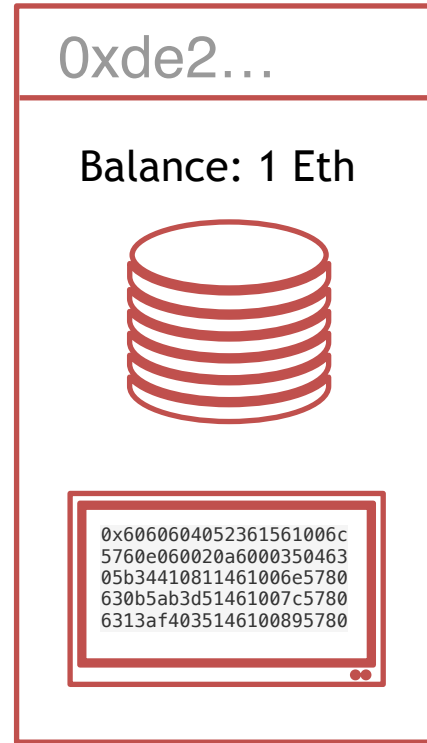
Balance: 1 Eth

# Overview on Ethereum

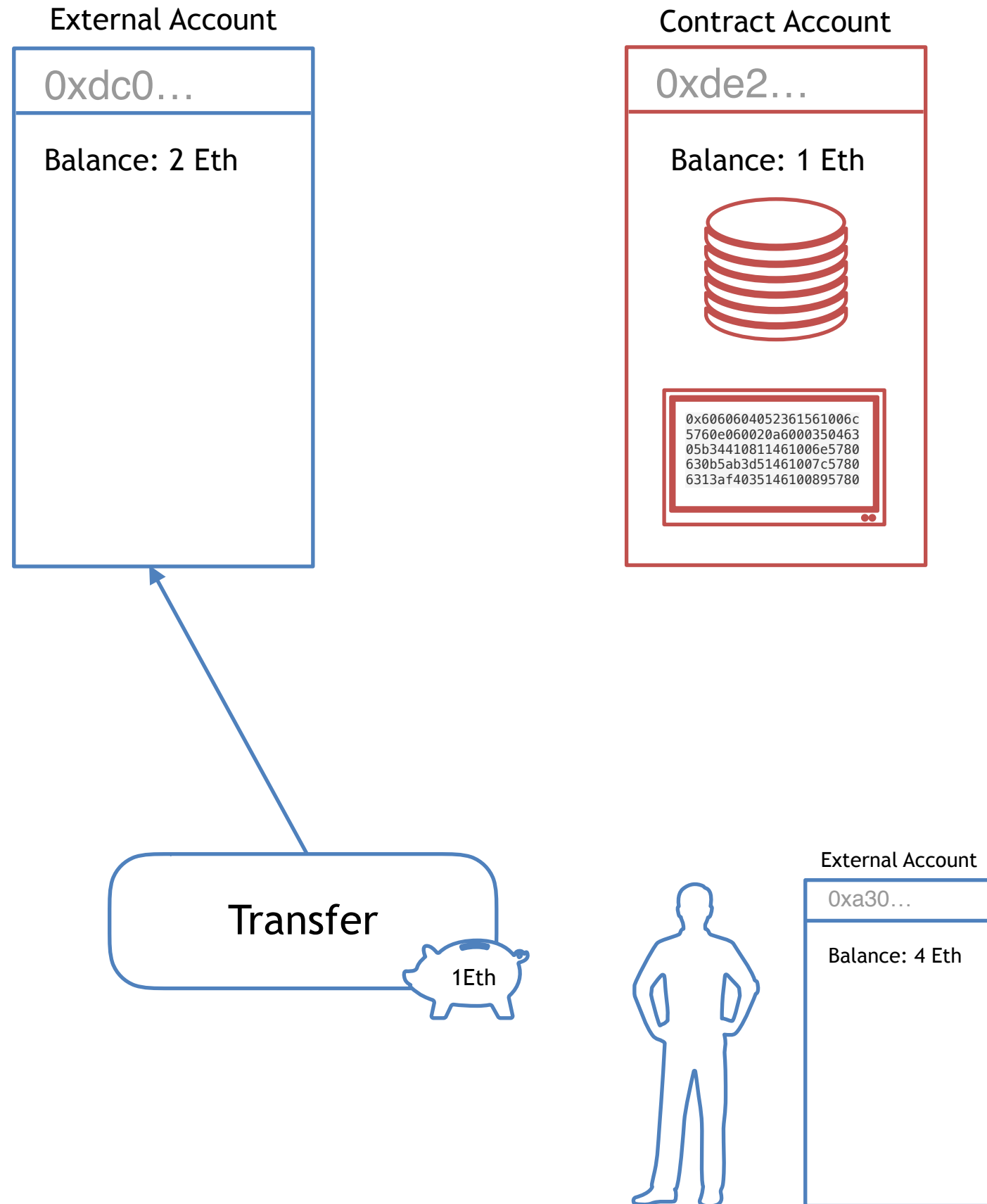
External Account



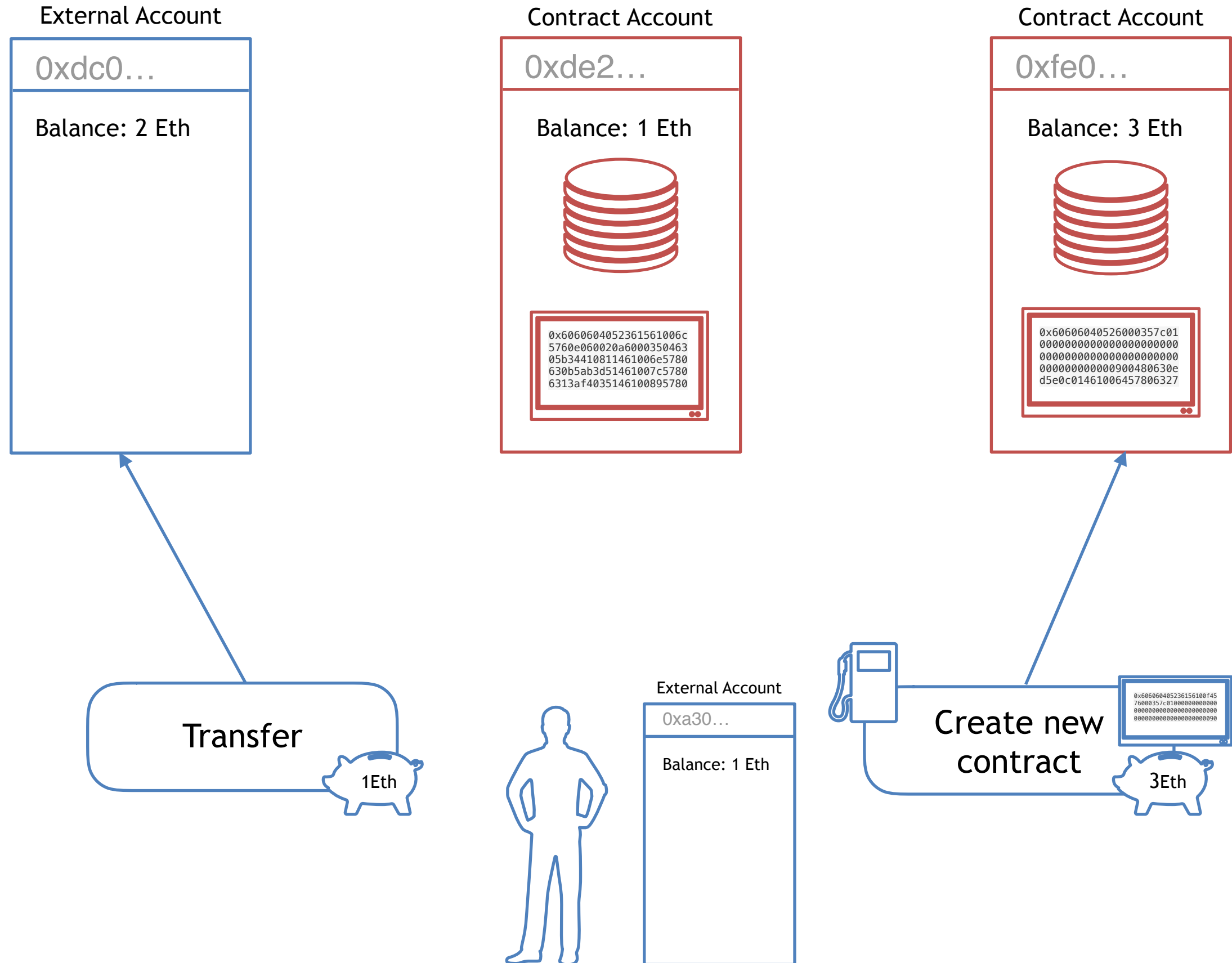
Contract Account



# Overview on Ethereum

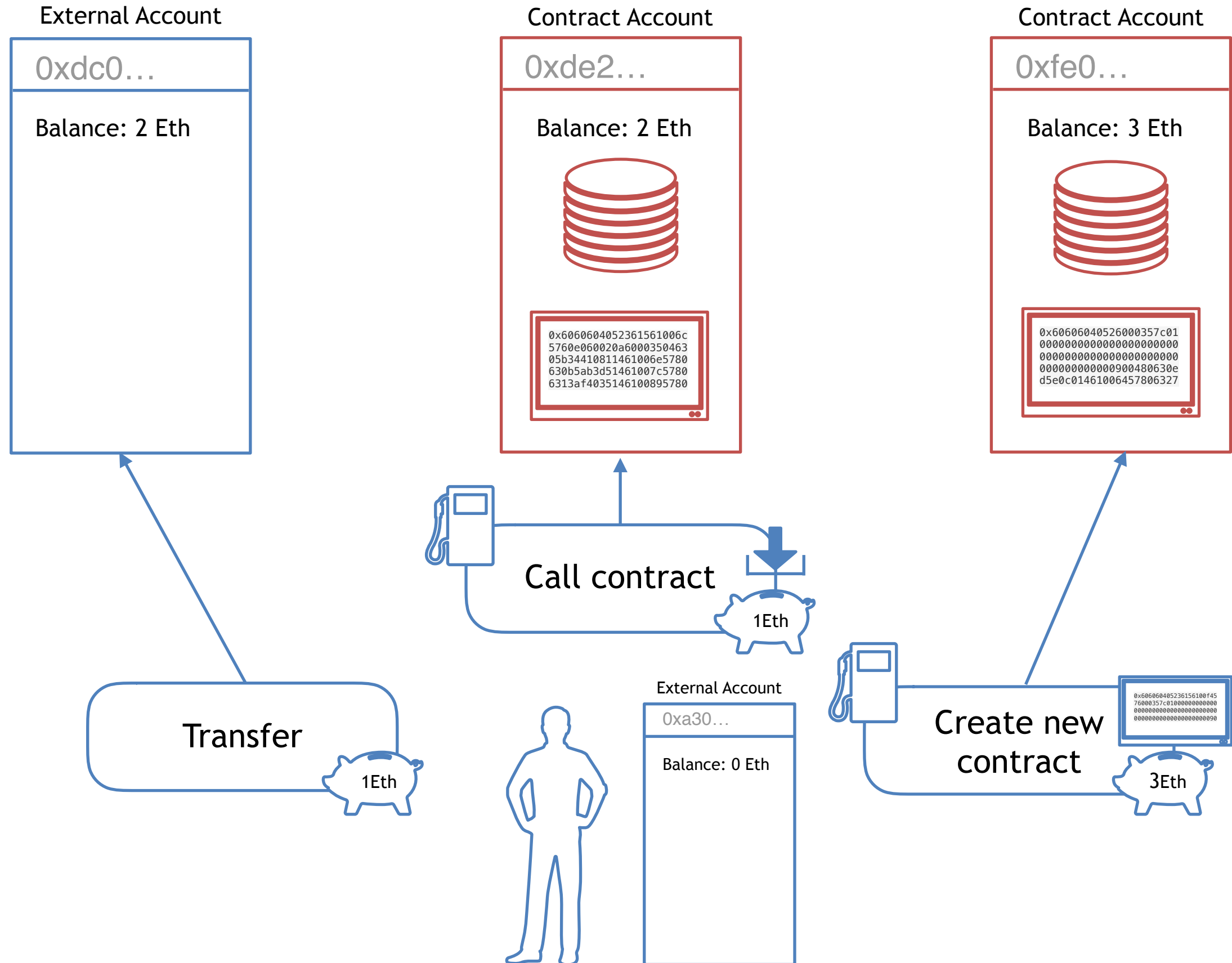


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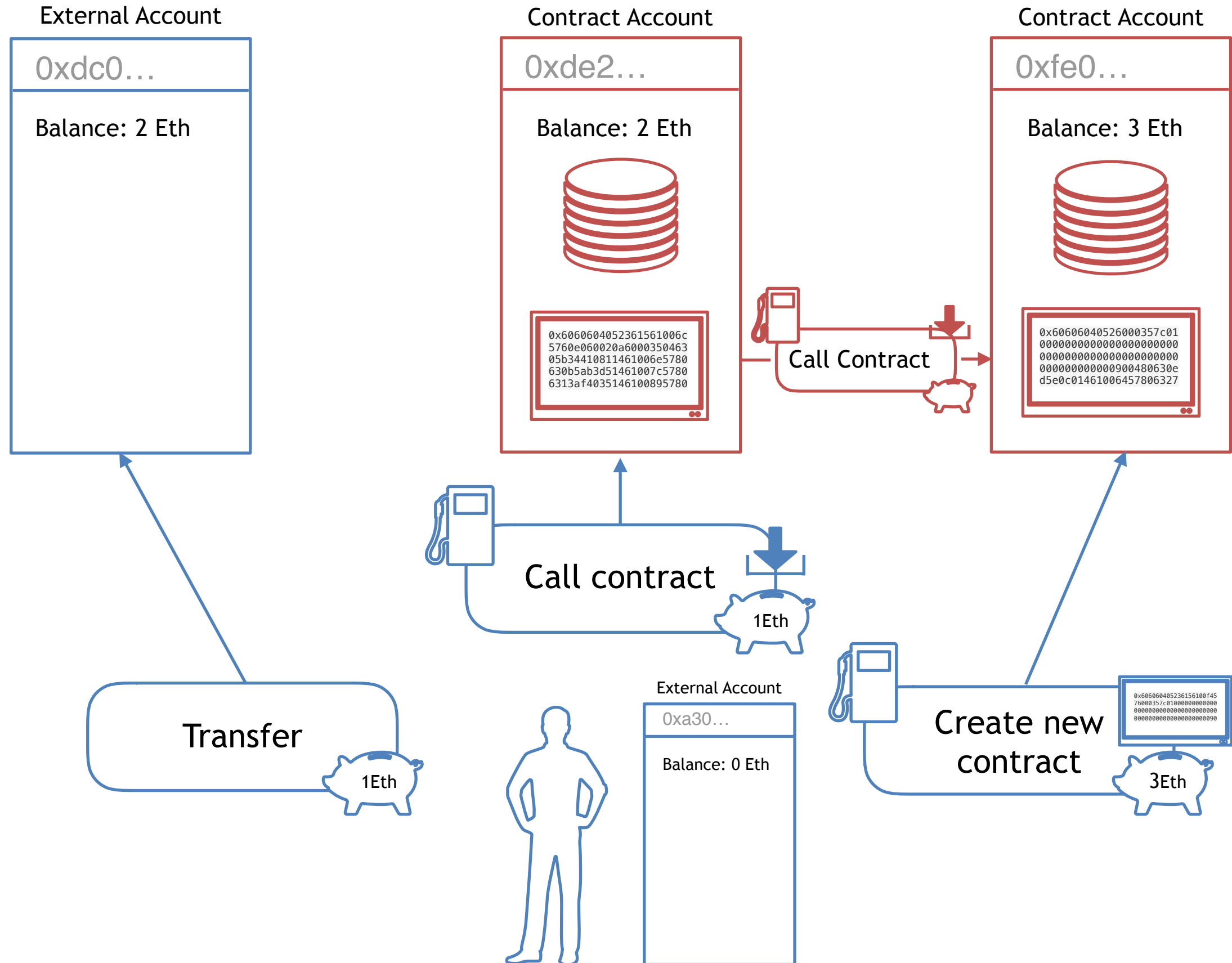




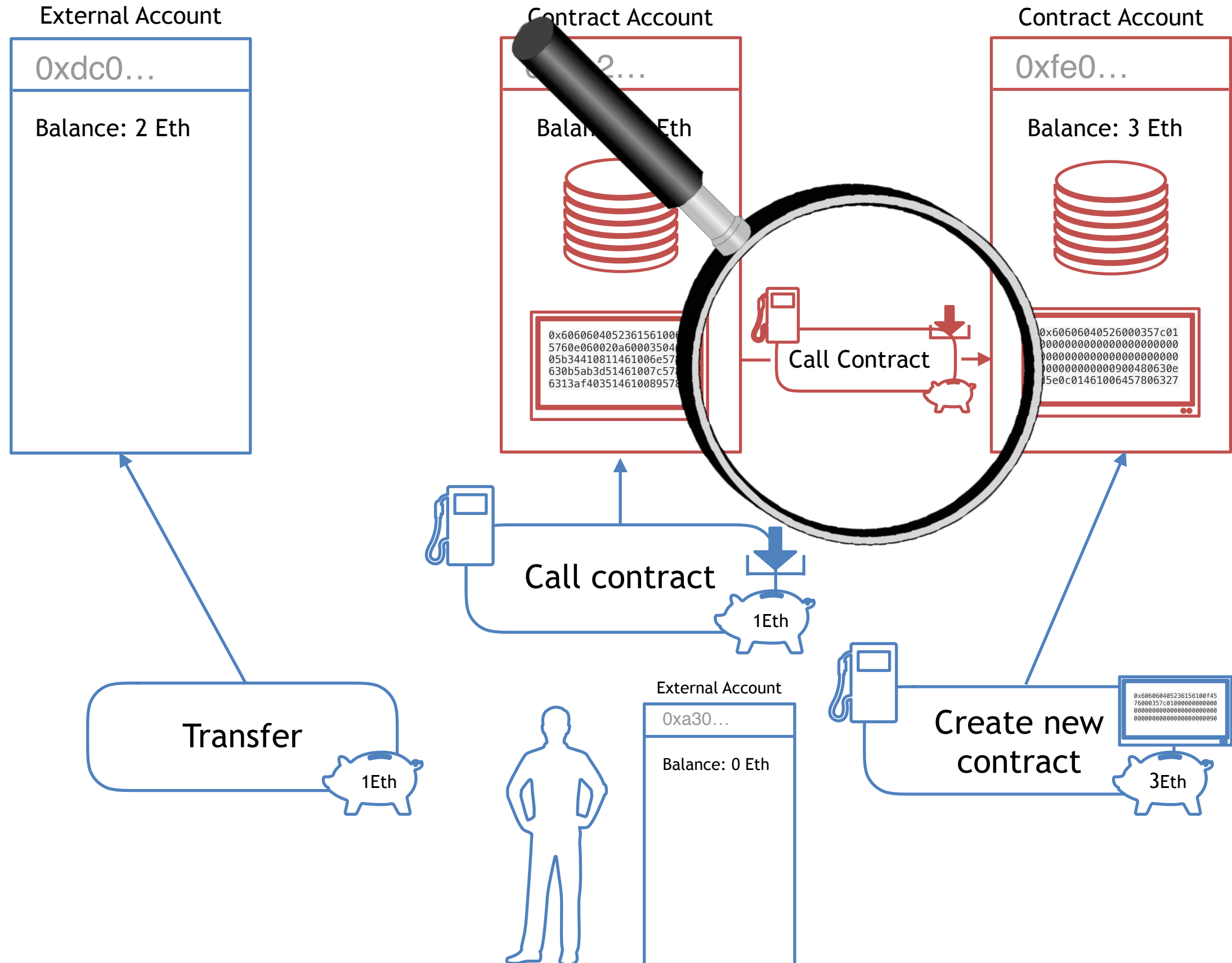
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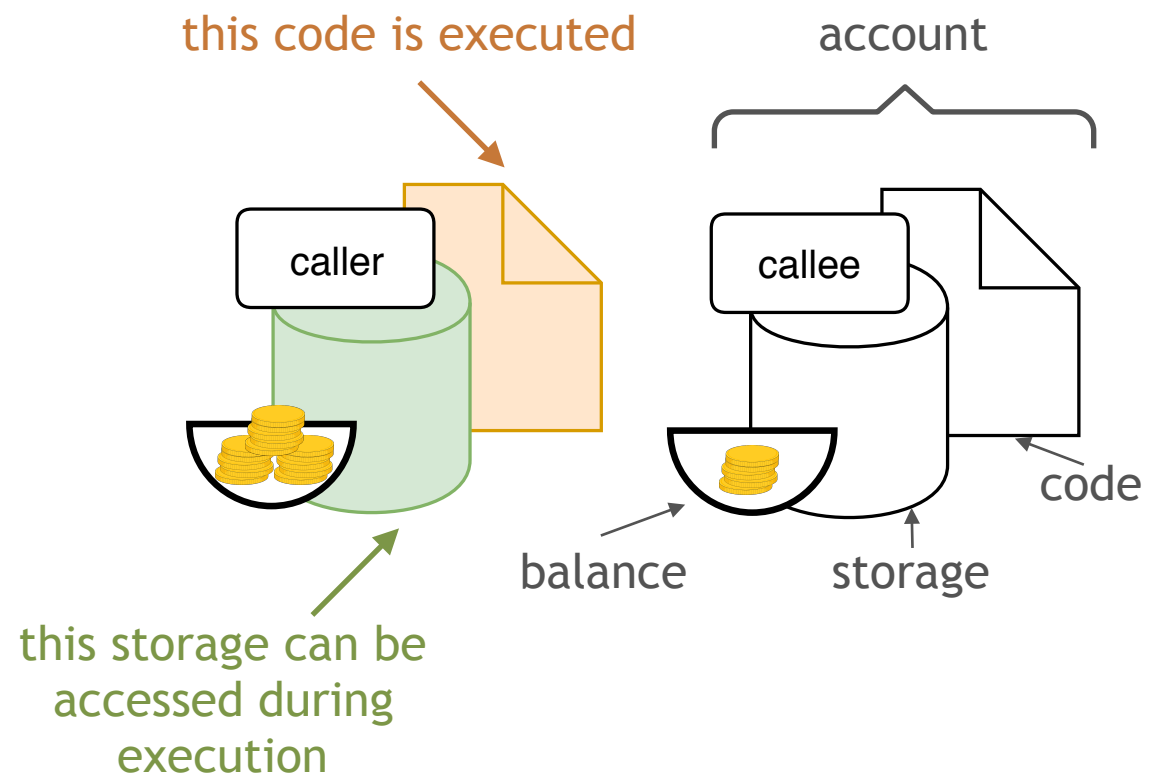
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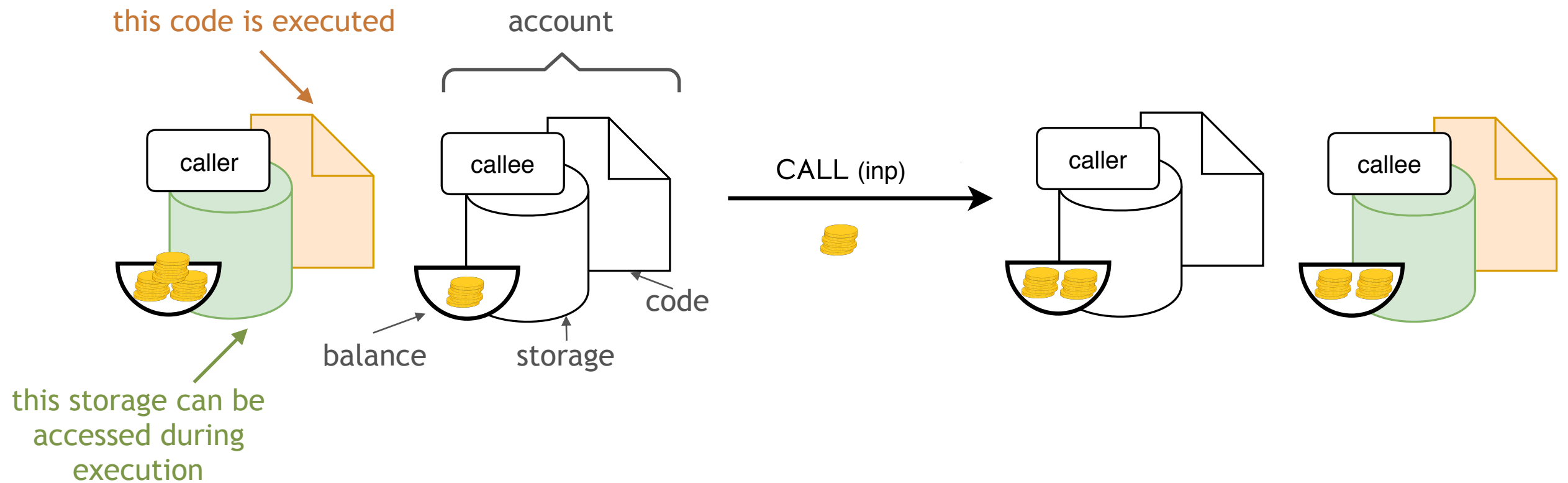


# Call flavours

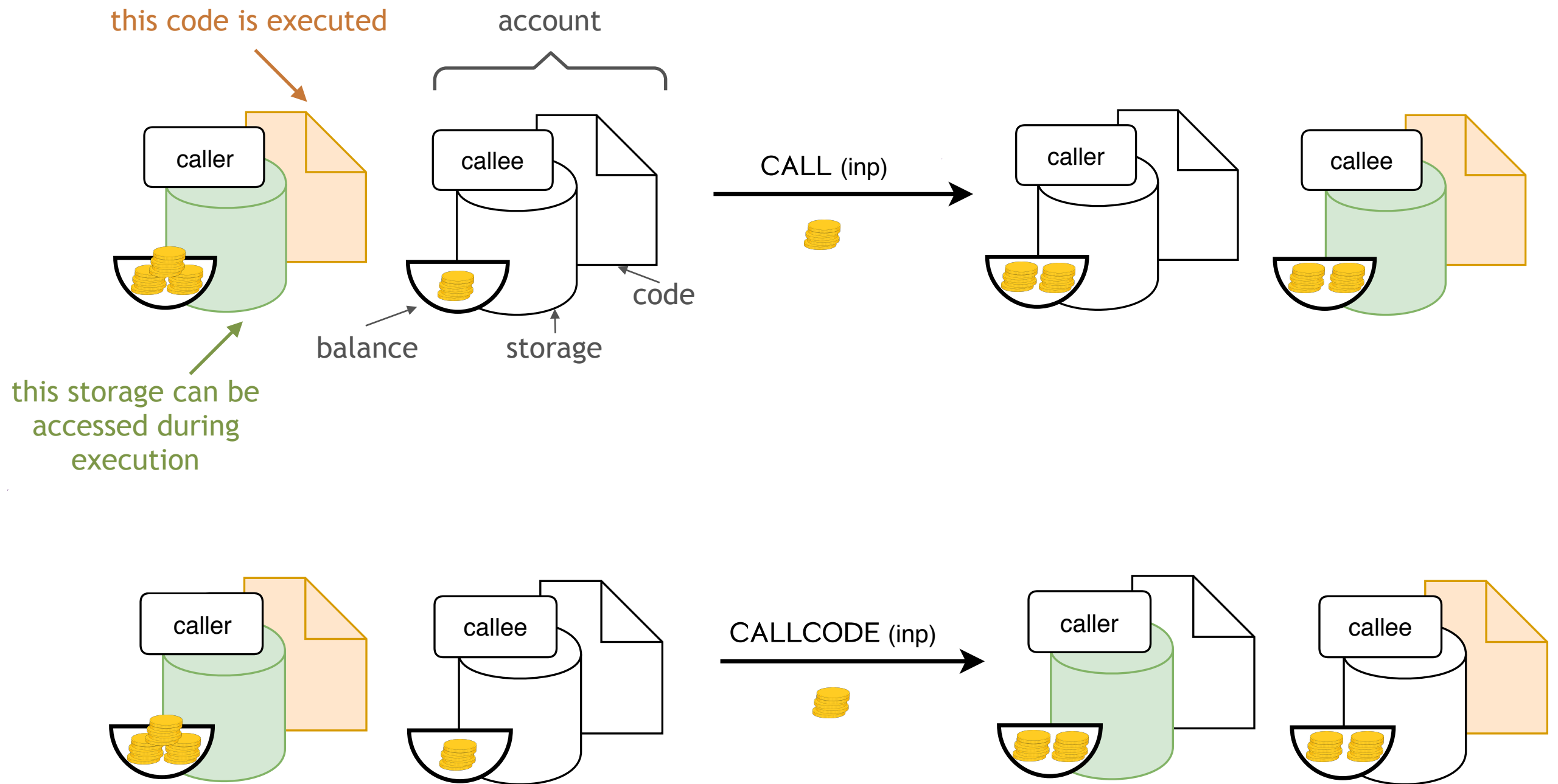




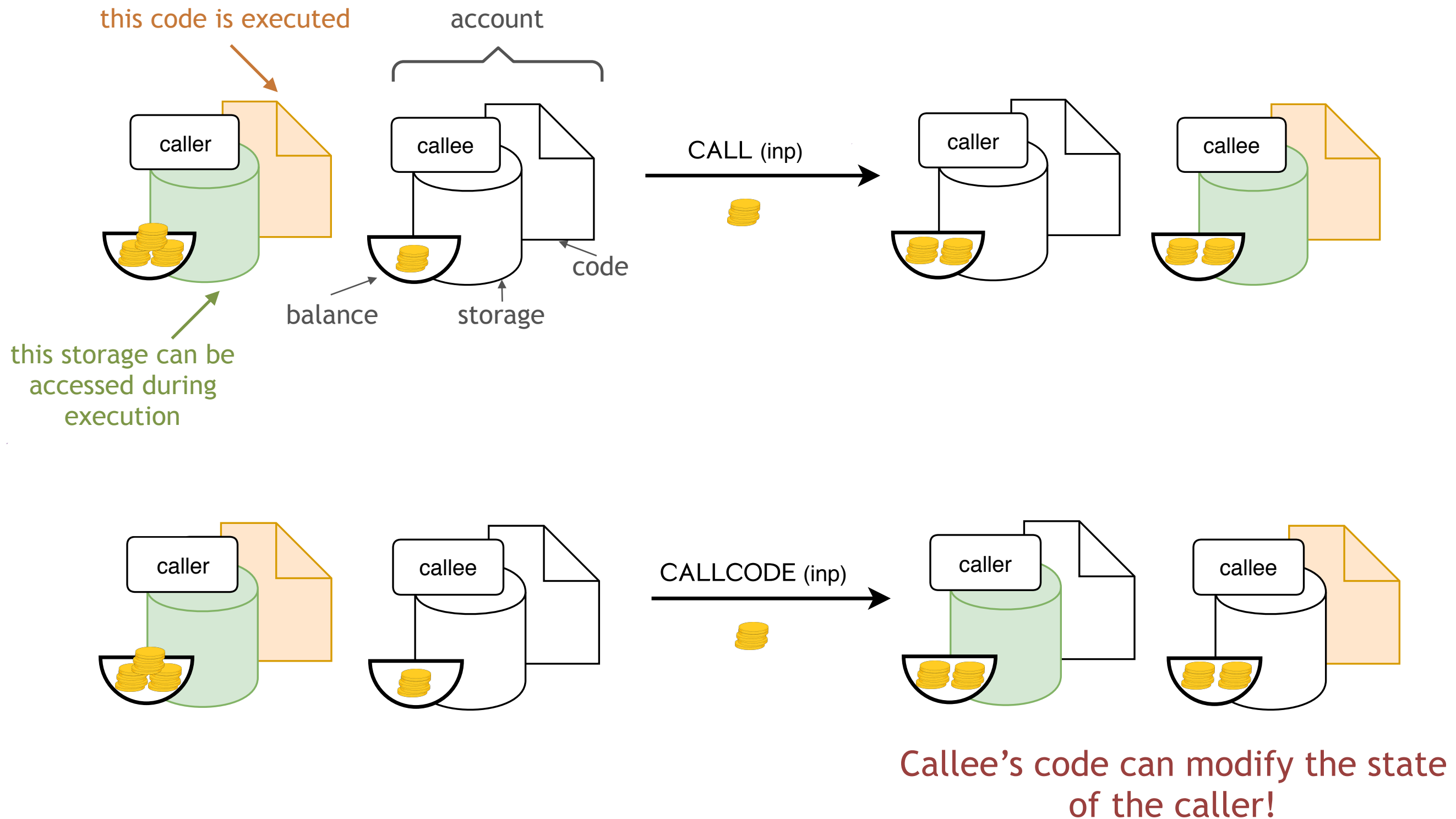
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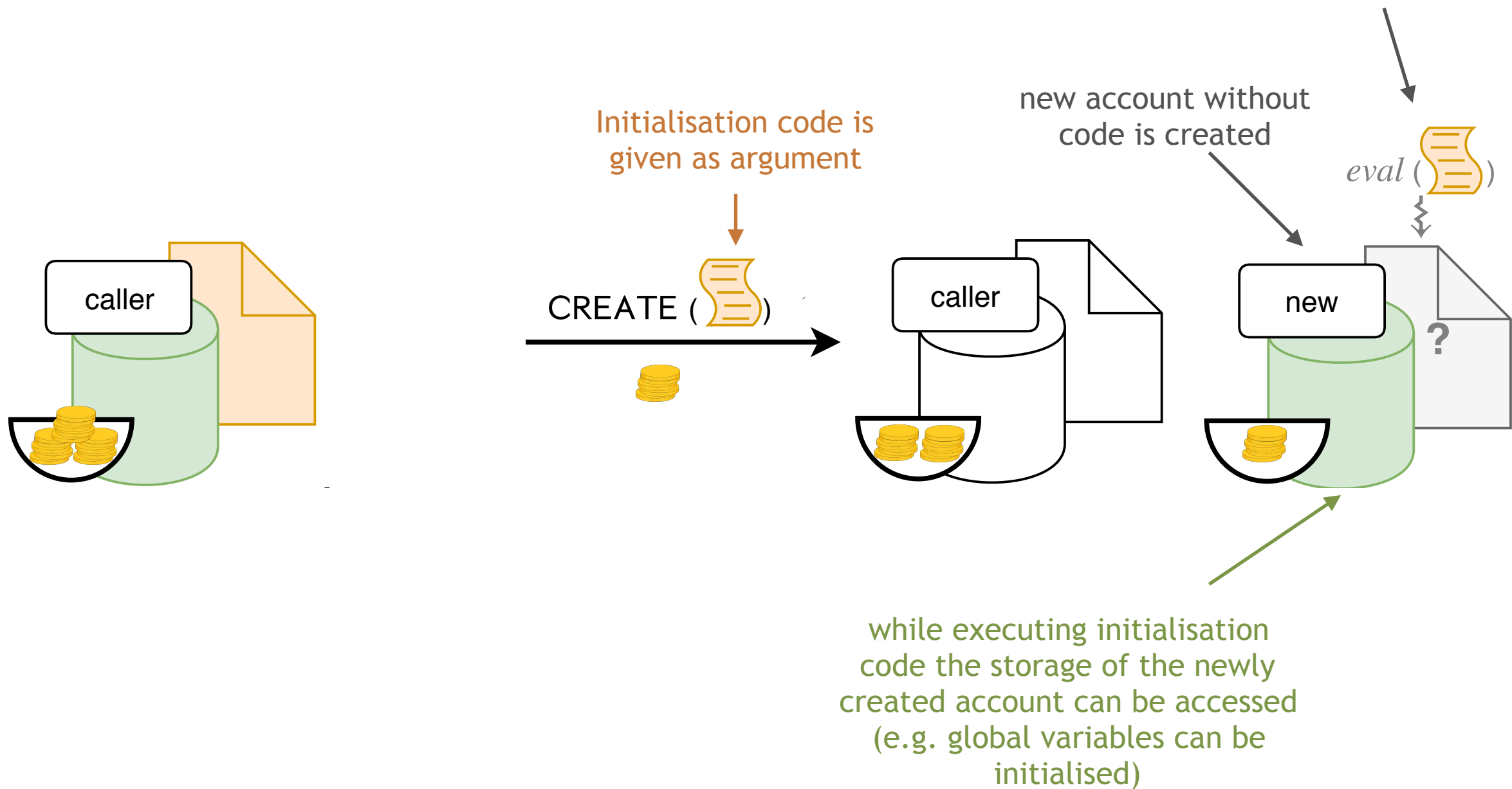


# Call flavours



# Contract creation

Upon successful execution, the initialisation code returns as output a code that will be (from that point on) attached to the new account





# Outline

Introduction to Ethereum

Semantics of EVM bytecode

Static Analysis of EVM bytecode

# We go for a slightly simplified setting

*(Only plain calls, simplified gas treatment, etc. )*

## Full treatment in...

### **A Semantic Framework for the Security Analysis of Ethereum smart contracts**

Ilya Grishchenko, Matteo Maffei, and Clara Schneidewind

TU Wien

`{ilya.grishchenko,matteo.maffei,clara.schneidewind}`

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Best paper award at  
ETAPS'18

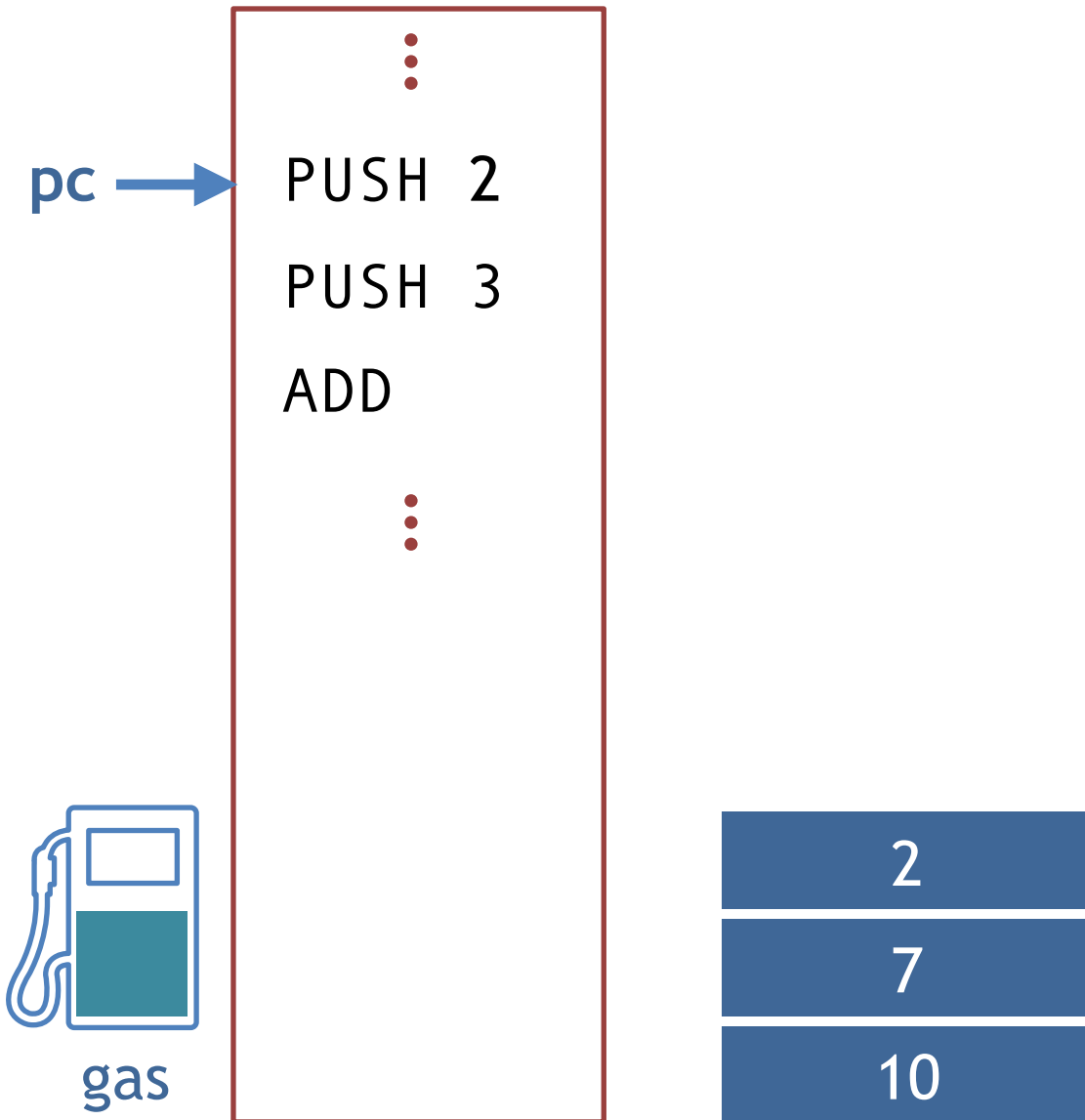
# EVM Semantics Formalization

- First complete formalization of EVM bytecode semantics, in the  $F^*$  proof assistant
- Executable semantics by compilation into OCAML
- Tested against the official Ethereum test suite
- While formalizing, we spotted various bugs and imprecisions in previous (in)formal descriptions, including those used in state-of-the-art static analysers (e.g., Oyente)

# EVM - Layout

Bytecode

Stack

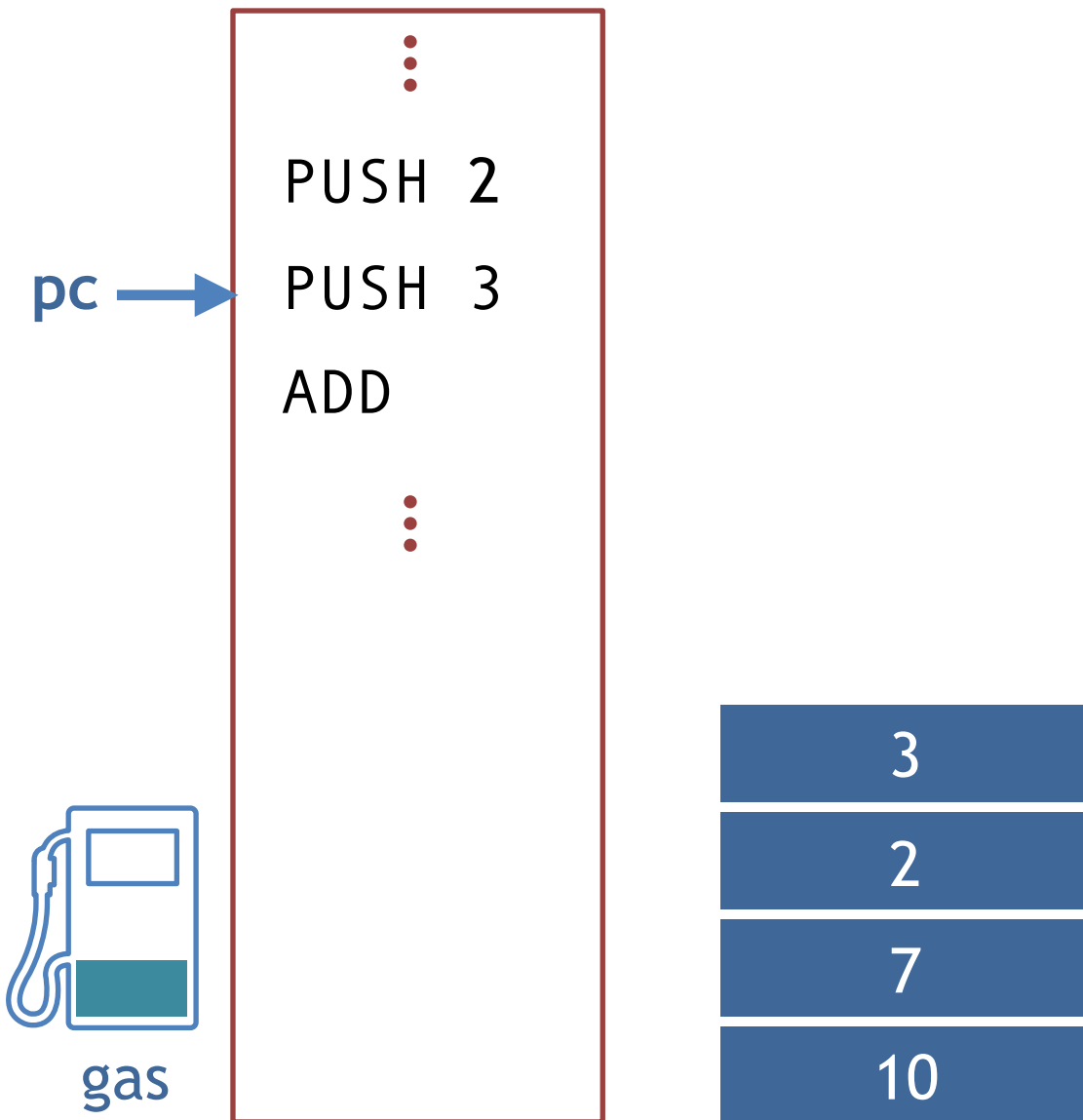




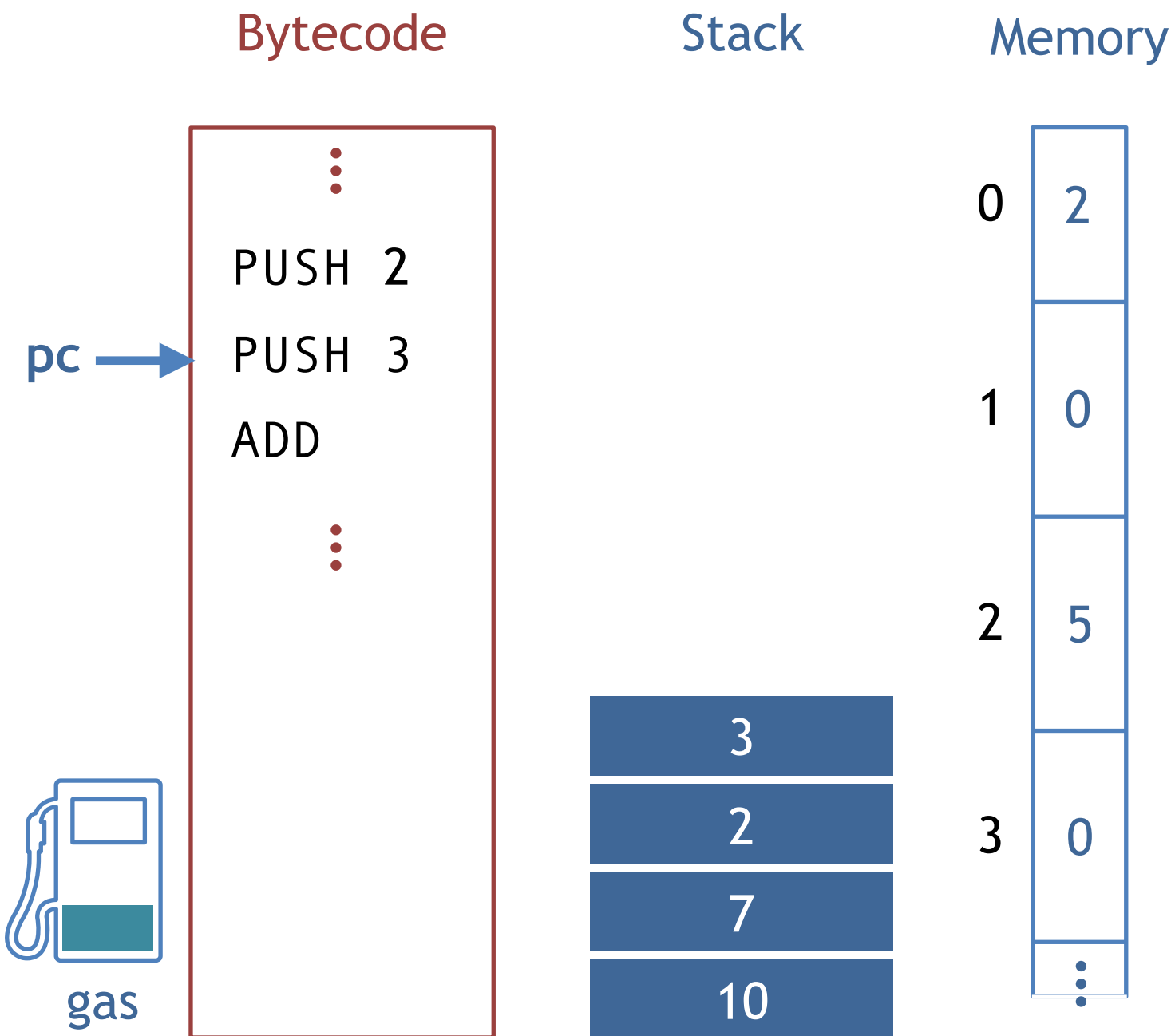
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Bytecode

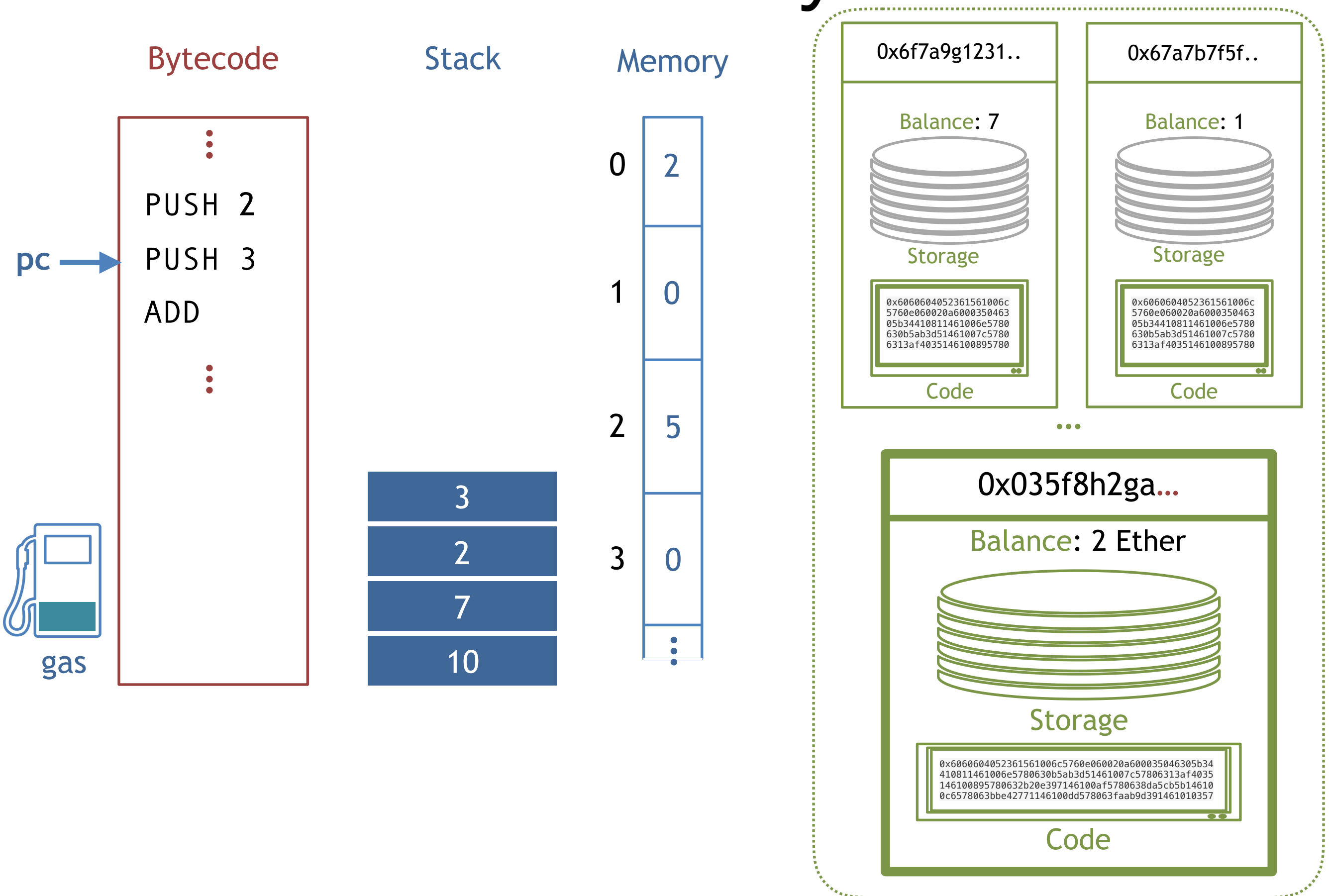
Stack



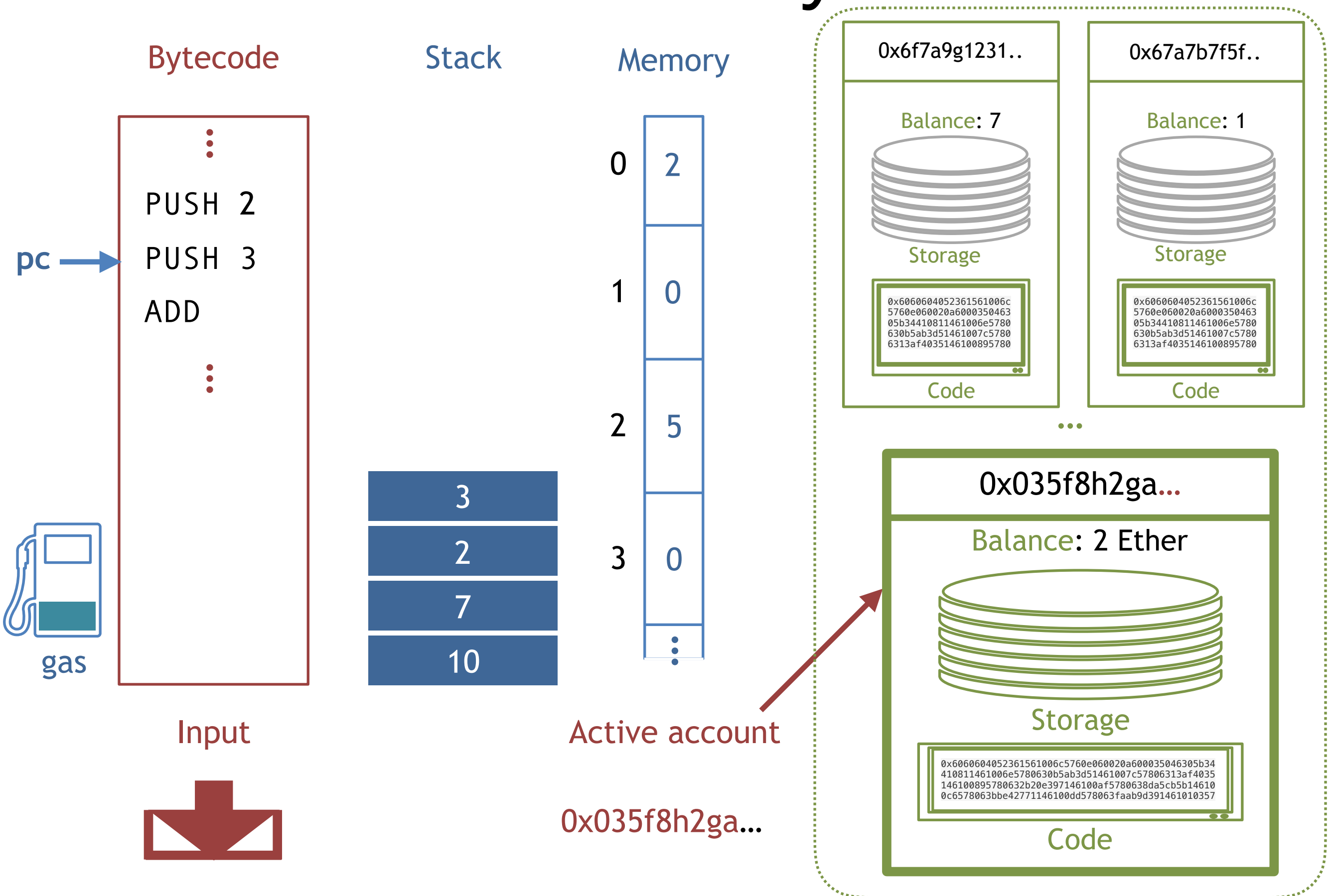
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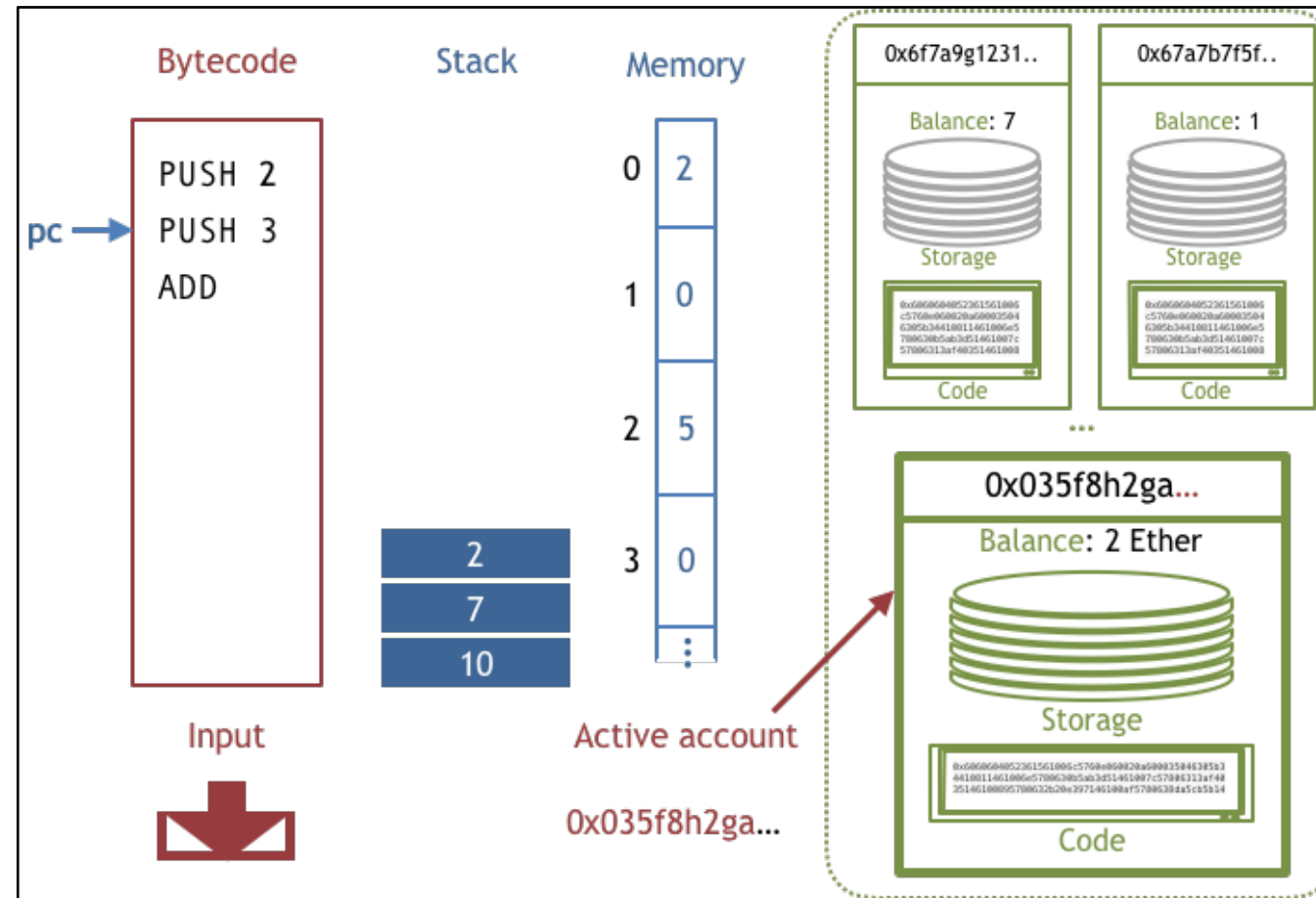
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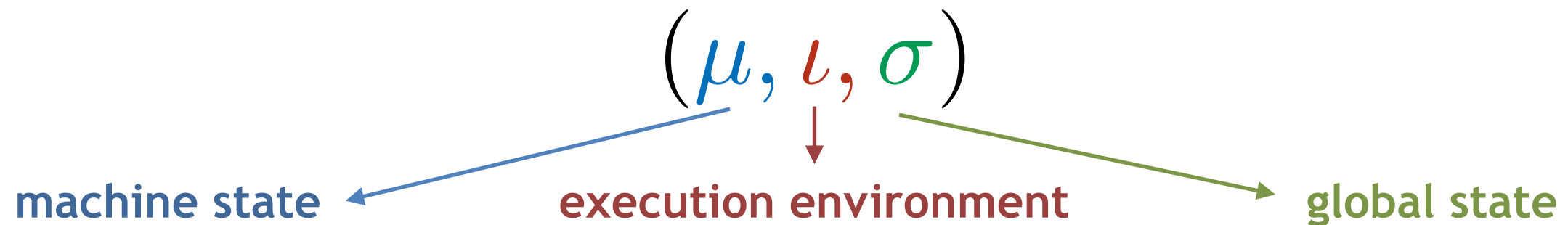
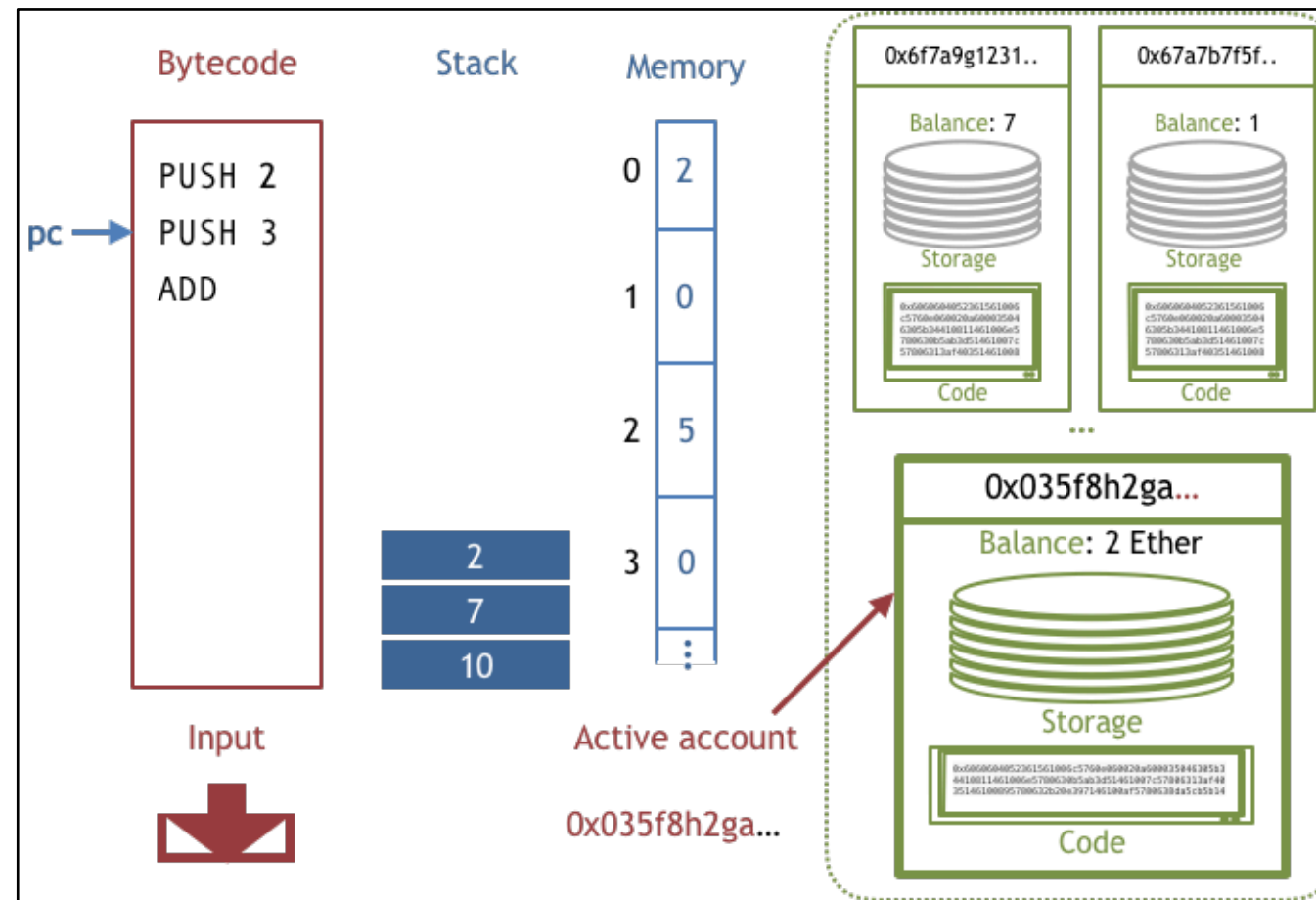


# Execution states

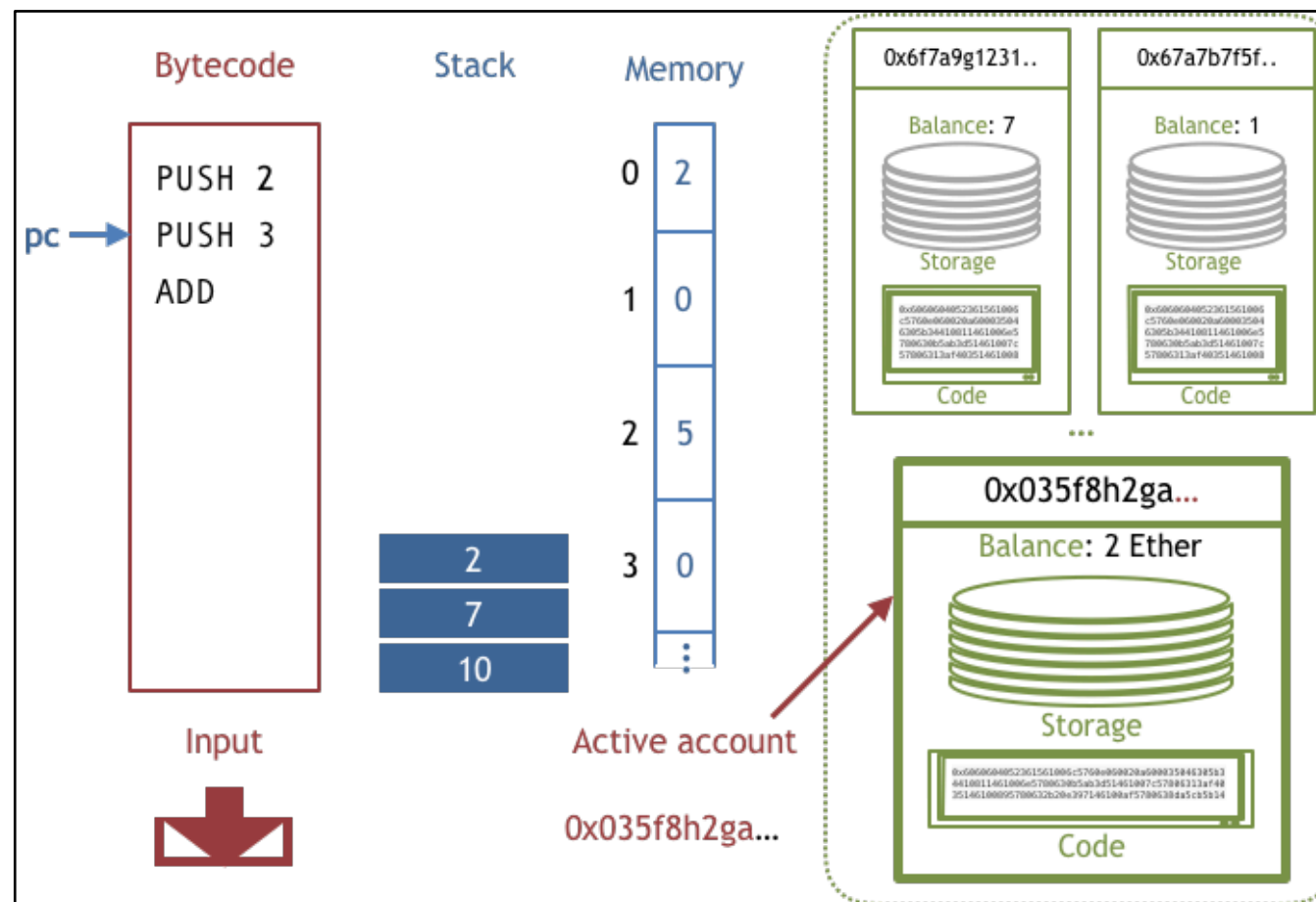




# Execution states



# Execution states



$$(\mu, \ell, \sigma)$$

machine state

execution environment

global state

$$(gas, pc, m, s)$$

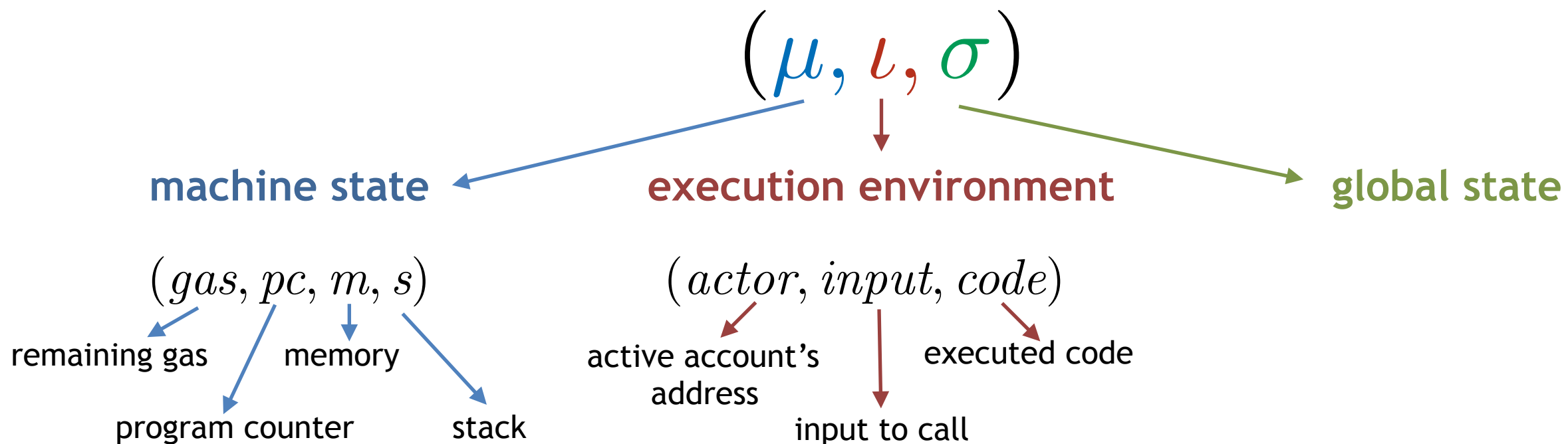
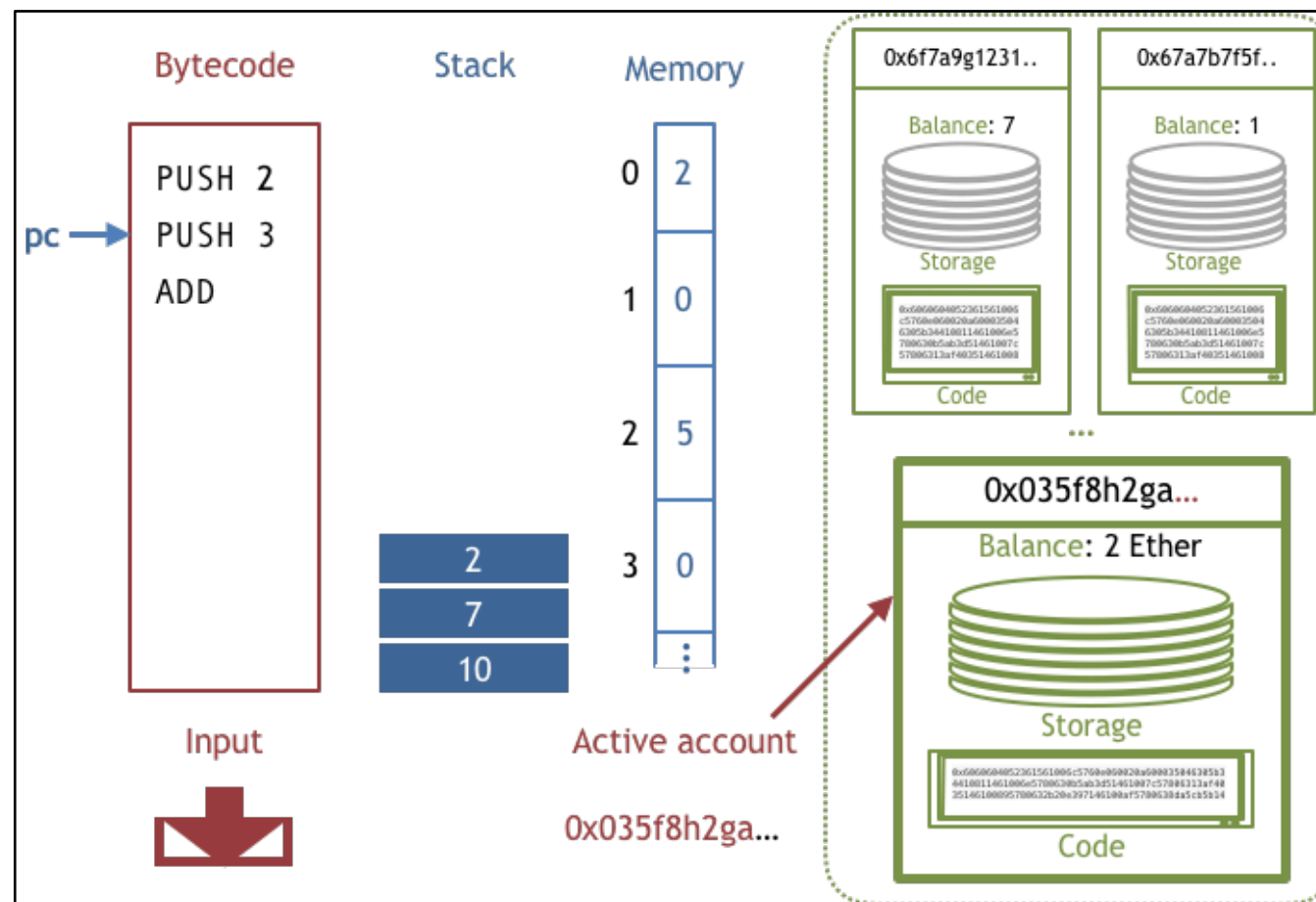
remaining gas

memory

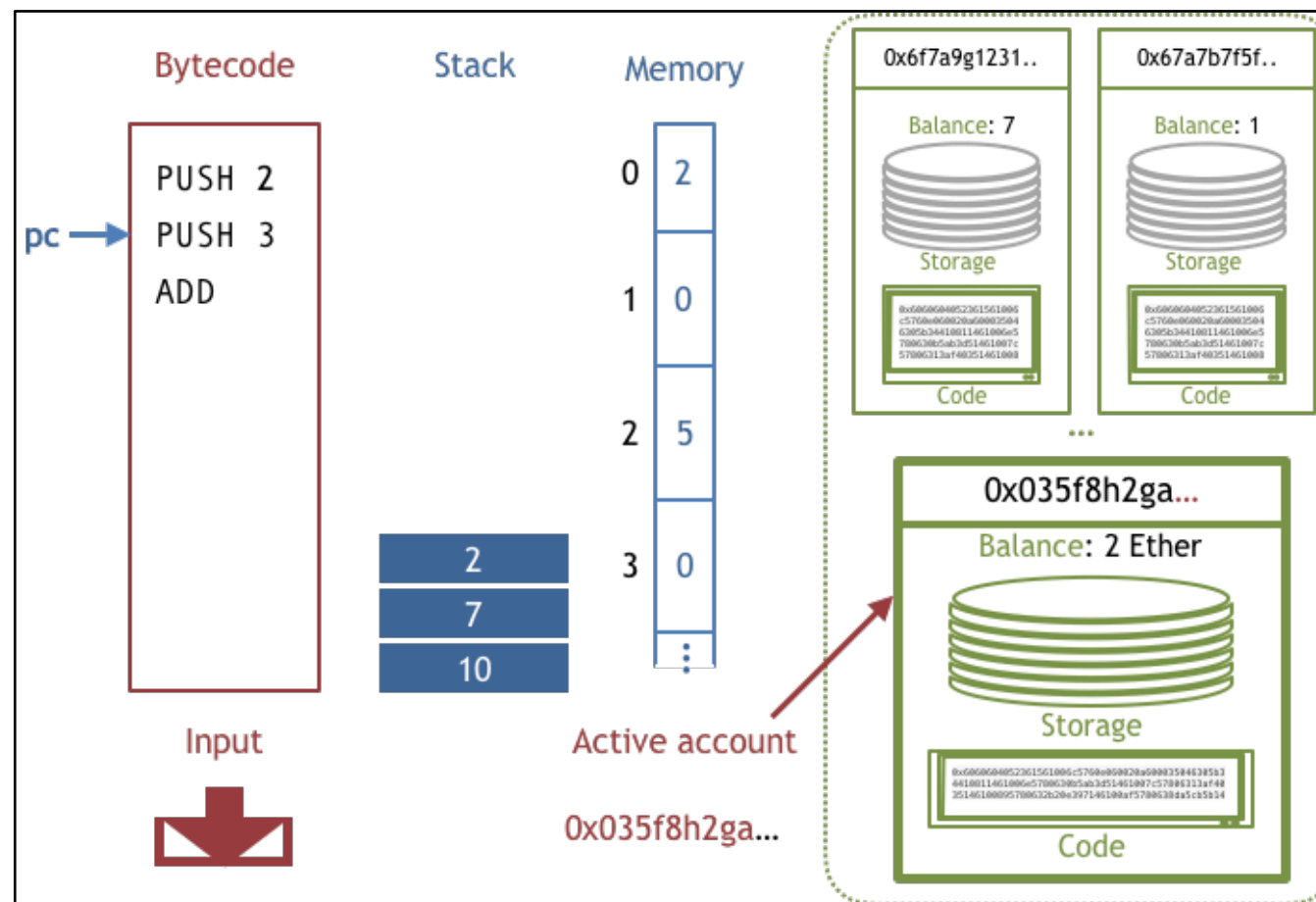
program counter

stack

# Execution states



# Execution states



$$(\mu, \iota, \sigma)$$

machine state

execution environment

global state

$$(gas, pc, m, s)$$

remaining gas

memory

program counter

stack

$$(actor, input, code)$$

active account's  
address

input to call

executed code

$$\sigma(a) = (b, stor, code)$$

account address

balance

storage

account code

# Small-step semantics

Call stacks	$\mathbb{S}$	$\ni$	$S$	$:=$	$EXC :: S_{plain} \mid HALT(\sigma, d, g) :: S_{plain} \mid S_{plain}$
Plain call stacks	$\mathbb{S}_{plain}$	$\ni$	$S_{plain}$	$:=$	$(\mu, \iota, \sigma) :: S_{plain} \mid \epsilon$
Transaction environments	$\mathcal{T}_{env}$	$\ni$	$\Gamma$	$:=$	$T$

# Small-step semantics

exceptional halting  
state

(might be entered e.g. as  
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 $\sigma$ , return value  $d$  and  
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block timestamp

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 \text{Transaction environments} & \mathcal{T}_{env} & \ni & \Gamma := \boxed{T}
 \end{array}$$

block timestamp

Small step relation

$$\Gamma \models S \rightarrow S'$$

describes how a call stack  $S$  evolves within one step of  
execution under transaction environment  $\Gamma$

# Simplified EVM bytecode

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- (Local) Memory instructions  
MSTORE, MLOAD

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(global state + execution environment + transaction environment)  
BALANCE, TIMESTAMP, INPUT, ADDRESS

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BALANCE, TIMESTAMP, INPUT, ADDRESS
- Contract Calls:  
CALL
- Halting:  
RETURN, STOP

# Simple stack operations

The instruction at  $\mu.pc$  of  
code  $\iota.code$  is ADD

$$\boxed{\mu.gas \geq 1 \quad \mu.s = a :: b :: s} \quad \boxed{\omega_{\mu,\iota} = \text{ADD}} \quad \mu' = \mu[s \rightarrow (a + b) :: s][pc += 1][gas -= 1]$$

preconditions are  
checked: enough gas  
available + enough  
element on the stack

$$\Gamma \models (\mu, \iota, \sigma) :: S \rightarrow (\boxed{\mu'}, \iota, \sigma) :: S$$

machine state is updated

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in case of a stack  
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$$\frac{\mu.gas < 1}{\Gamma \models (\mu, \iota, \sigma) :: S \rightarrow EXC :: S}$$

if the execution runs out of  
gas, the execution halts  
exceptionally  
(holds for all instructions)

# Memory Access

value on memory  
address  $a$  is written to  
the stack

$$\begin{array}{c}
 \omega_{\mu, \iota} = \text{MLOAD} \quad \mu.\text{gas} \geq 1 \quad \mu.s = a :: s \\
 v = \mu.m[a] \quad \mu' = \mu[s \rightarrow v :: s][\text{pc} += 1][\text{gas} -= 1] \\
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 \end{array}$$

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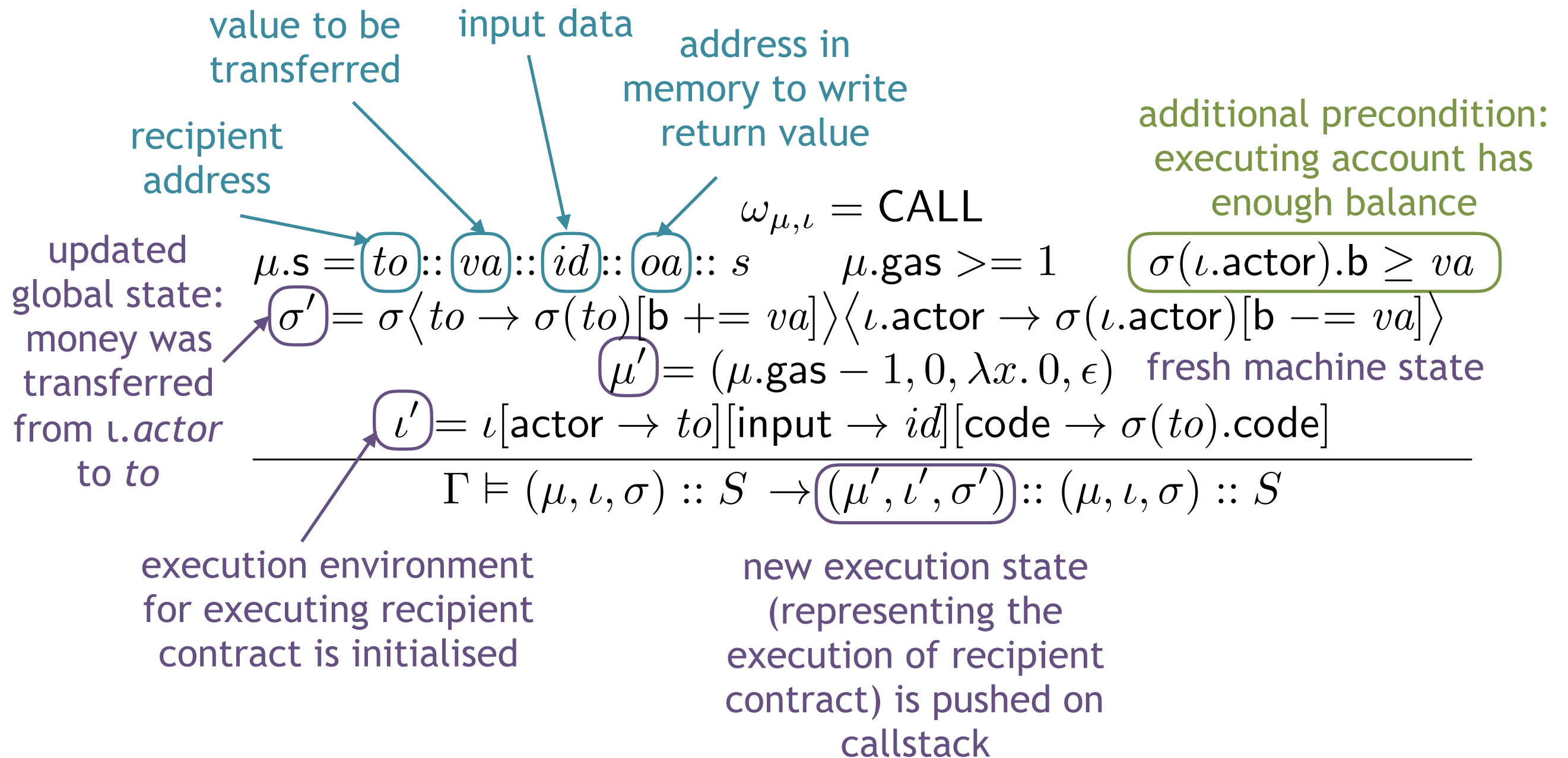
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 \end{array}$$

value  $b$  is written to  
memory address  $a$

$$\begin{array}{c}
 \omega_{\mu, \iota} = \text{MSTORE} \quad \mu.s = a :: b :: s \quad \mu.\text{gas} \geq 1 \\
 \mu' = \mu[m \rightarrow \mu.m[a \rightarrow b]][s \rightarrow s][\text{pc} += 1][\text{gas} -= 1] \\
 \hline
 \Gamma \models (\mu, \iota, \sigma) :: S \rightarrow (\mu', \iota, \sigma) :: S
 \end{array}$$

# Calling



# The DAO

```
contract DAO {  
    mapping (address => uint) donations;  
  
    function donate() {  
        donations[msg.sender] += msg.value;  
    }  
  
    function withdraw(){  
        if (donations[msg.sender] > 0)  
        { msg.sender.call.value(donations[msg.sender])();  
          donations[msg.sender] = 0;  
        }  
    }  
}
```

} mapping keeping track of the donations made by different addresses

} function for performing donations

} function for withdrawing donations

# The DAO

```
contract DAO {  
  mapping (address => uint) donations;
```

} mapping keeping track of the  
donations made by different  
addresses

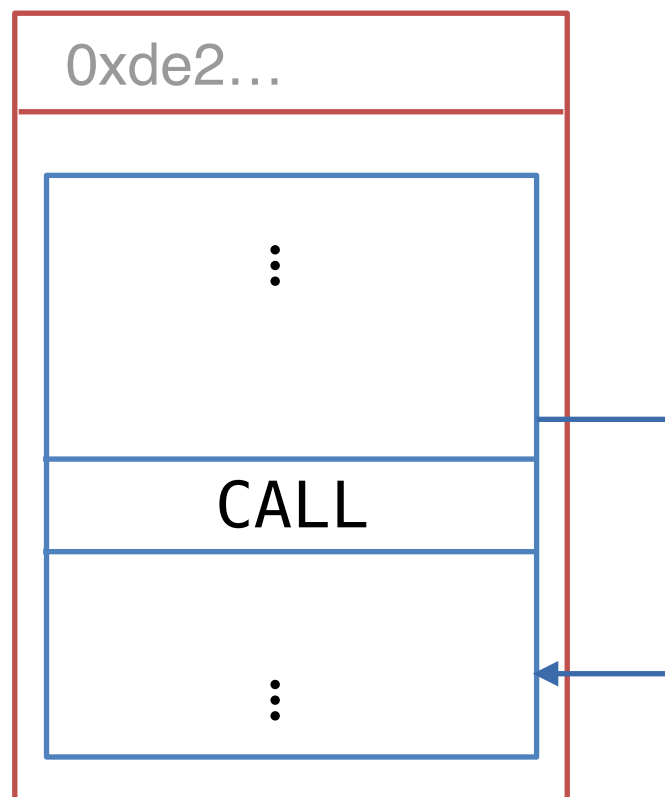
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}
```

} function for  
withdrawing  
donations

DAO contract



# The DAO

```
contract DAO {  
  mapping (address => uint) donations;
```

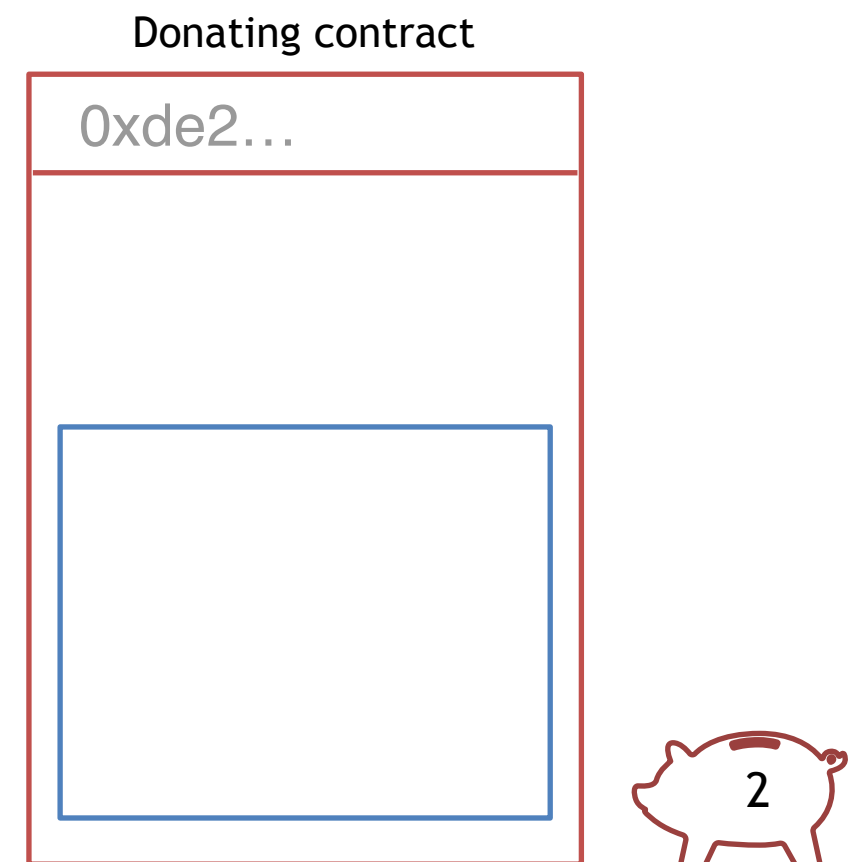
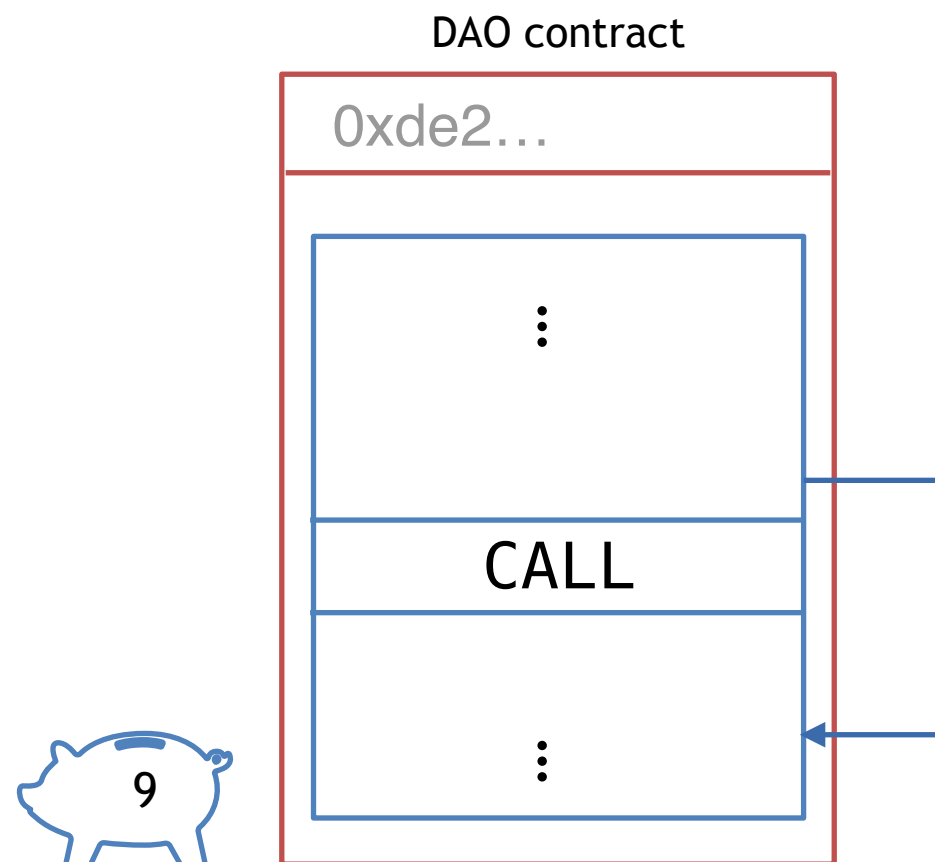
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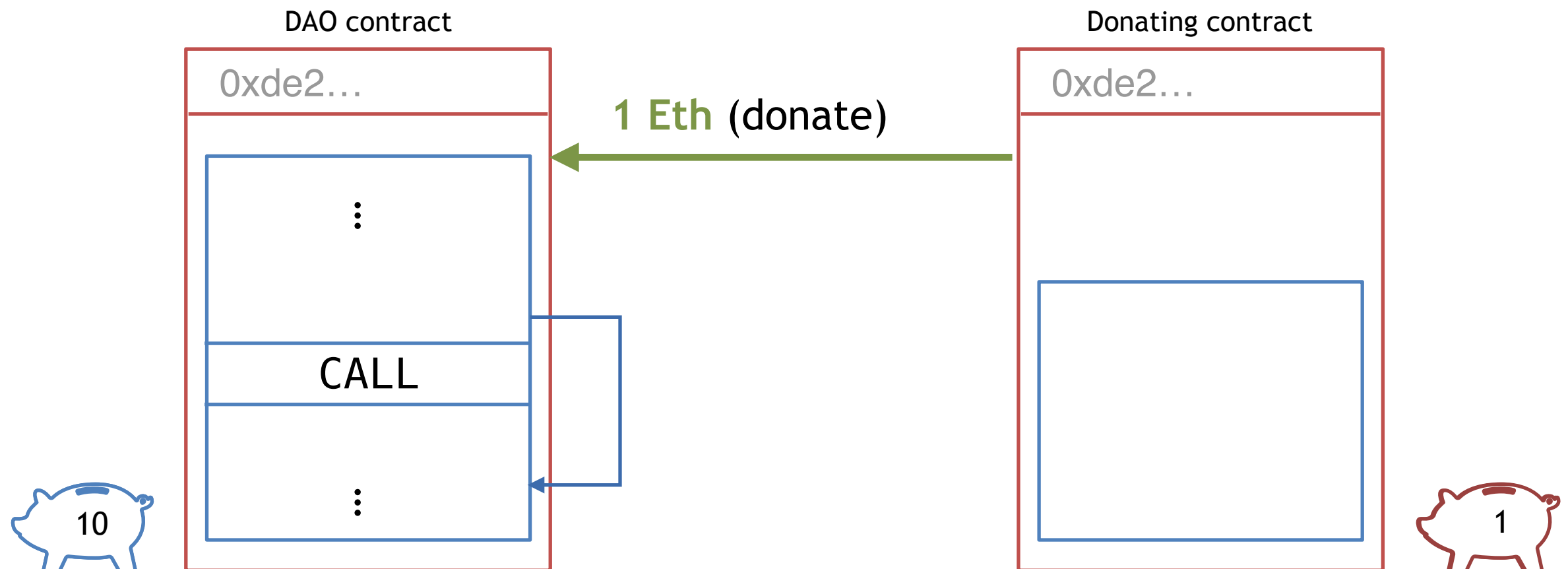
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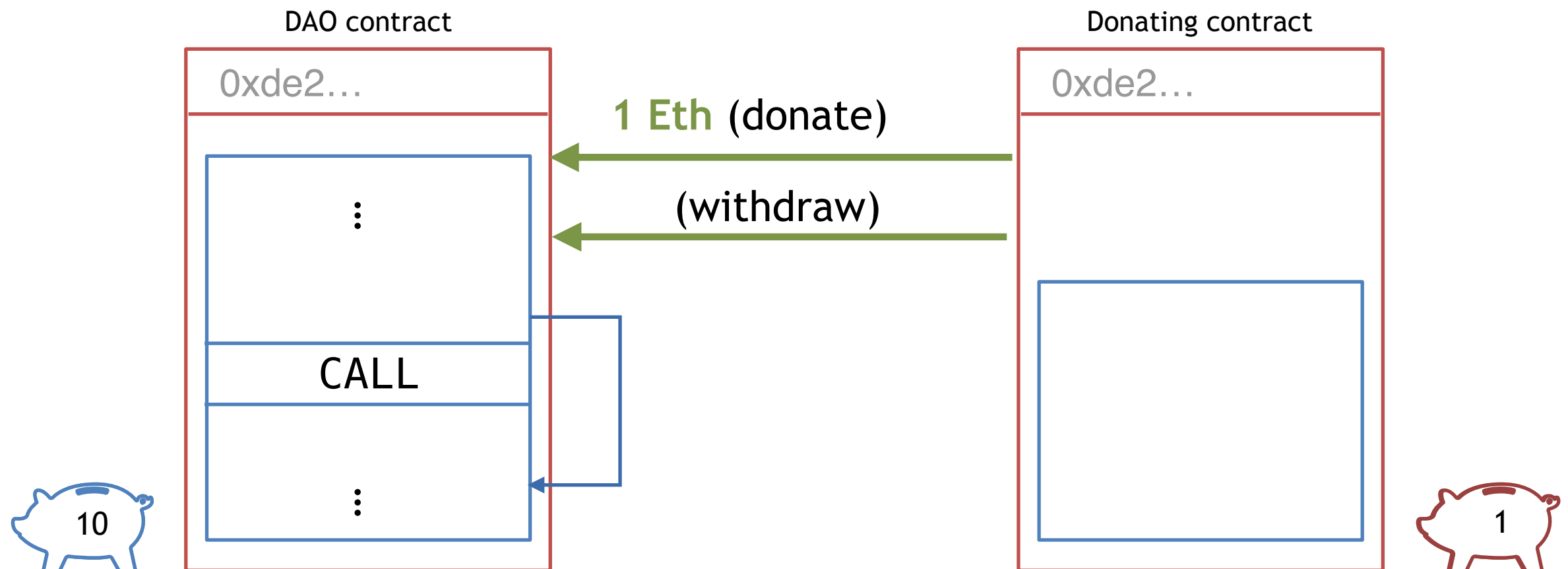
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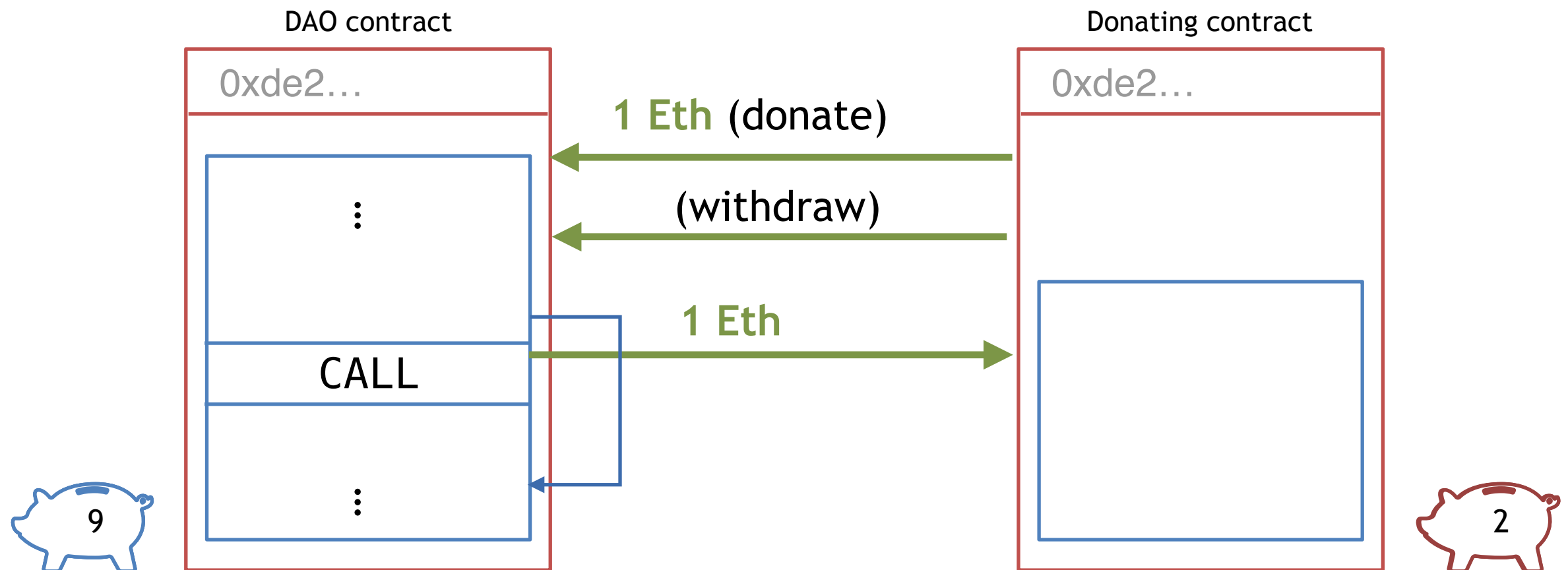
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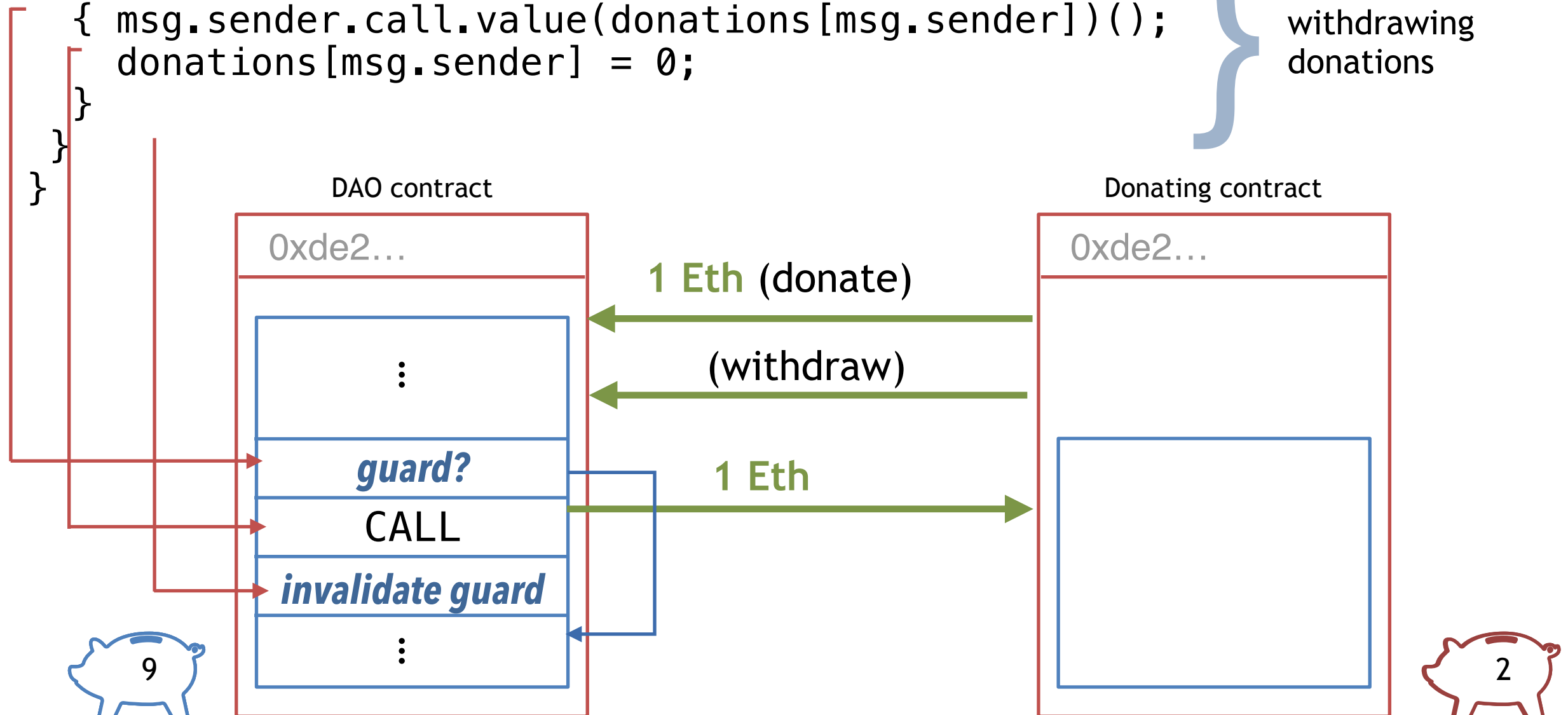
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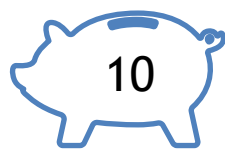
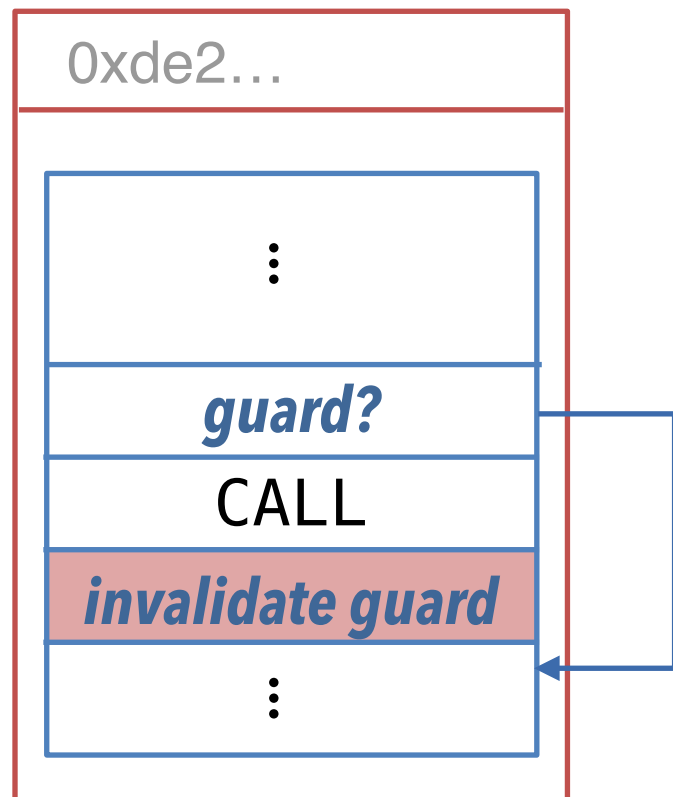
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# Attack on the DAO

```
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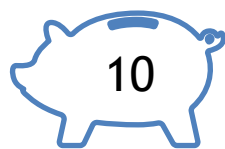
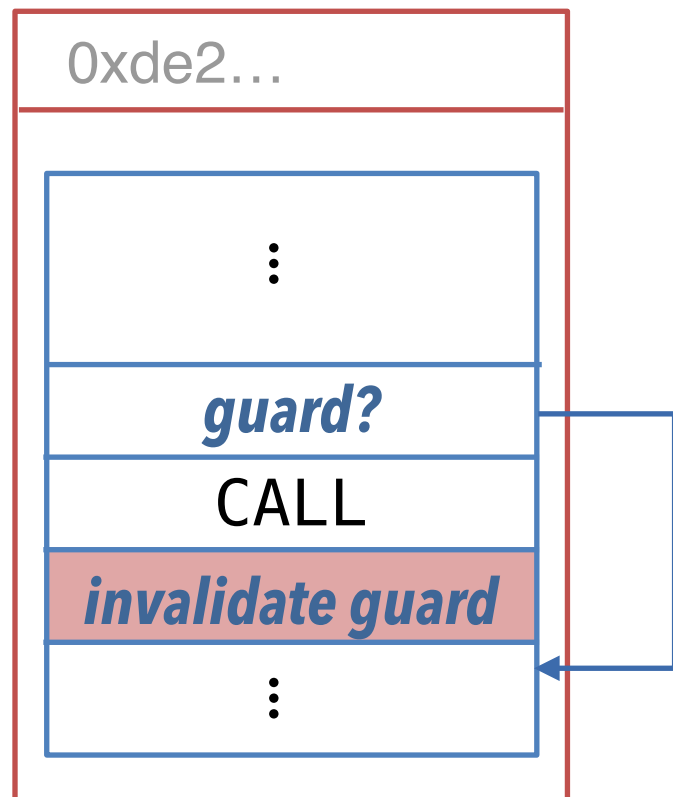
DAO contract



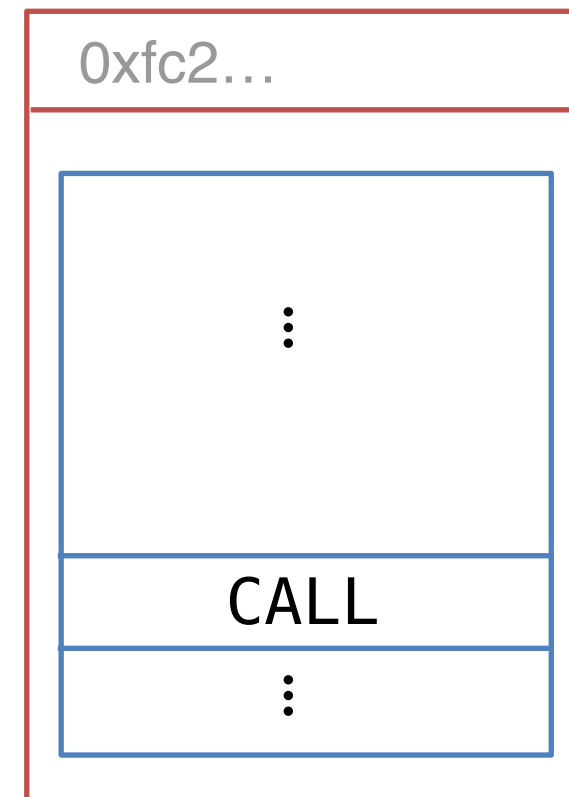
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DAO contract

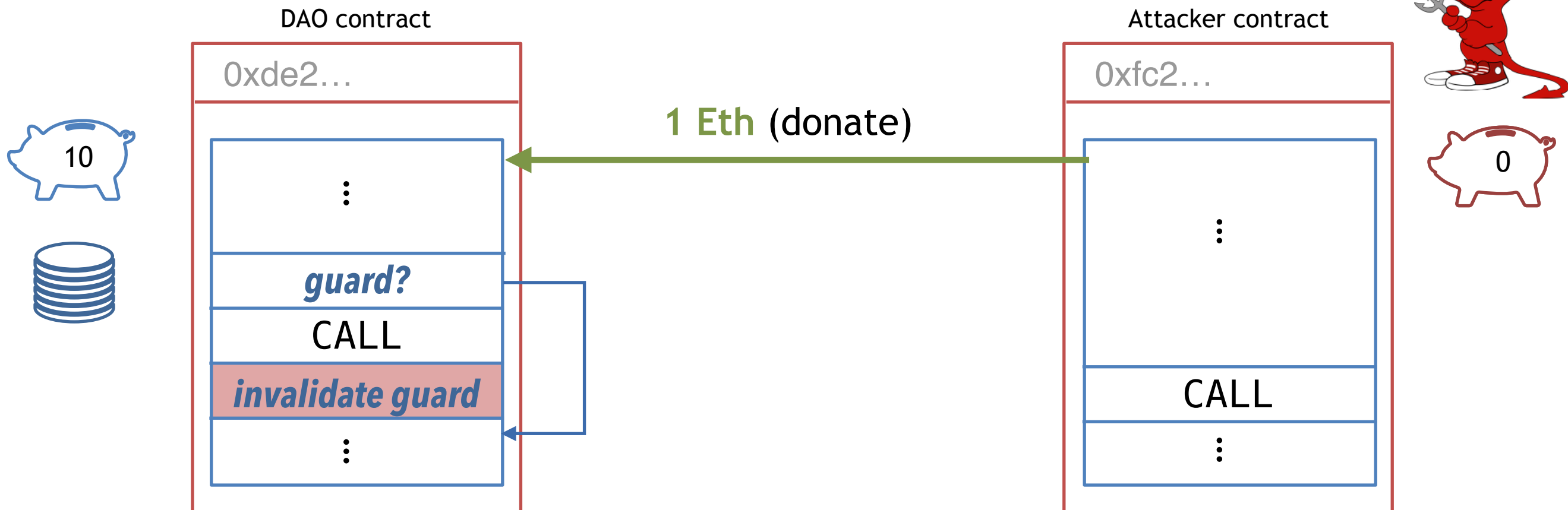


Attacker contract



# Attack on the DAO

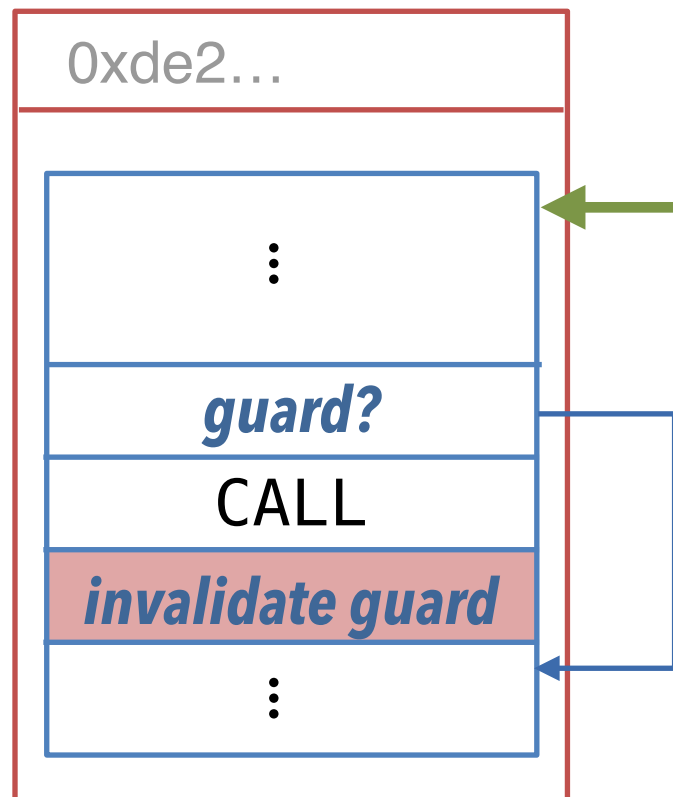
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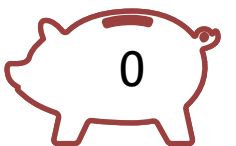
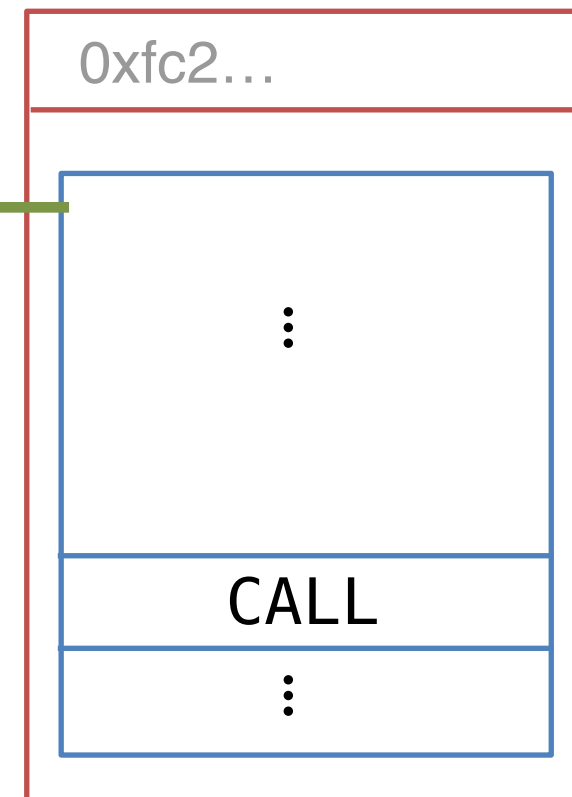
DAO contract



guard: true

1 Eth (donate)

Attacker contract





# Attack on the DAO

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DAO contract

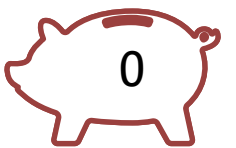
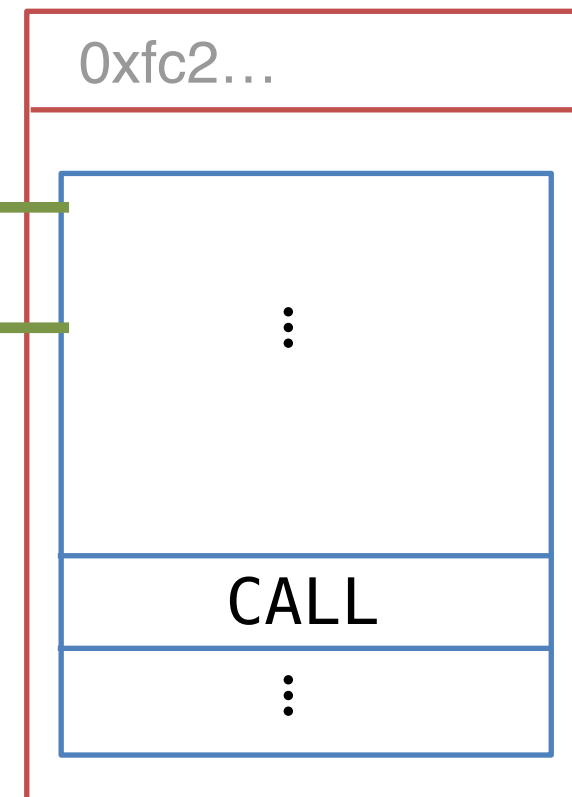


guard: true

1 Eth (donate)

(withdraw)

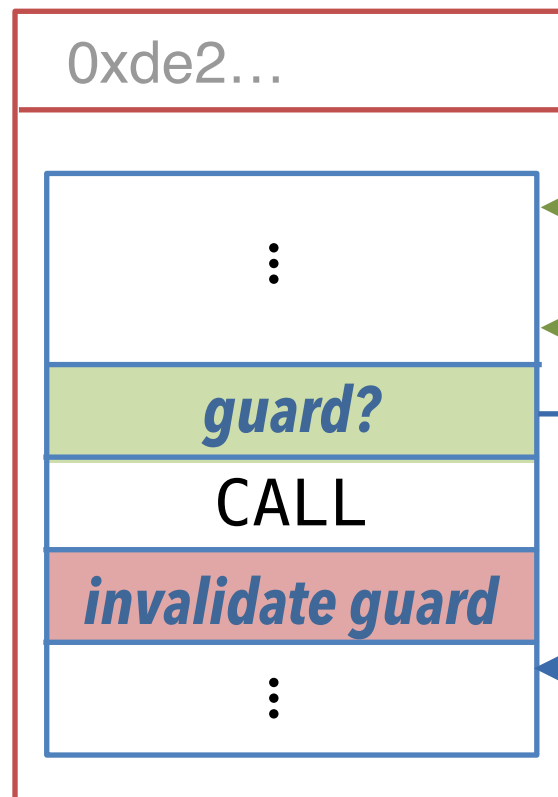
Attacker contract



# Attack on the DAO

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DAO contract

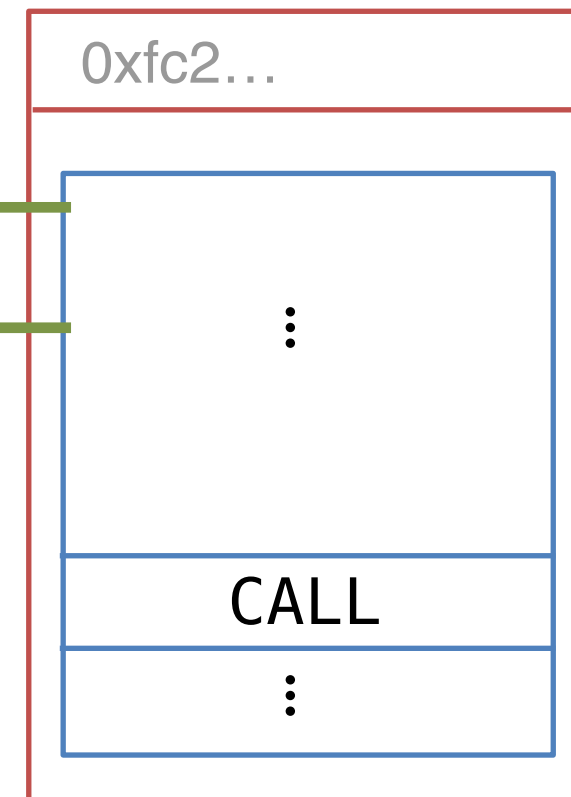


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1 Eth (donate)

(withdraw)

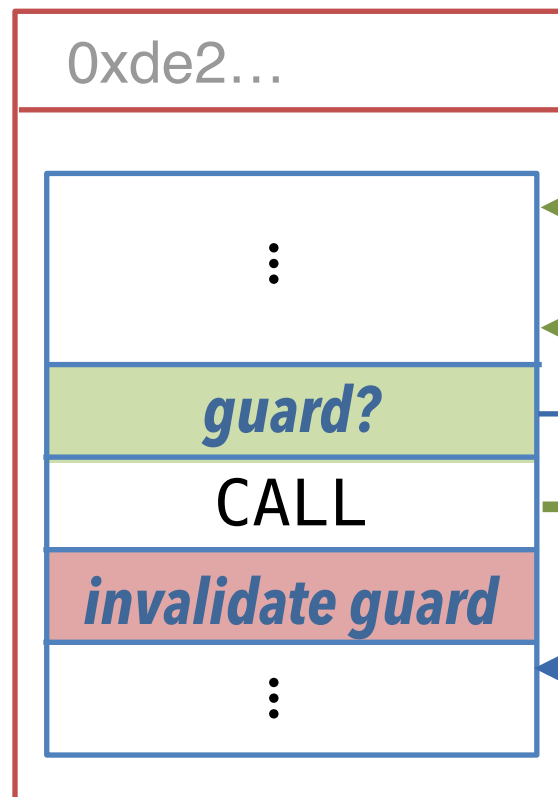
Attacker contract



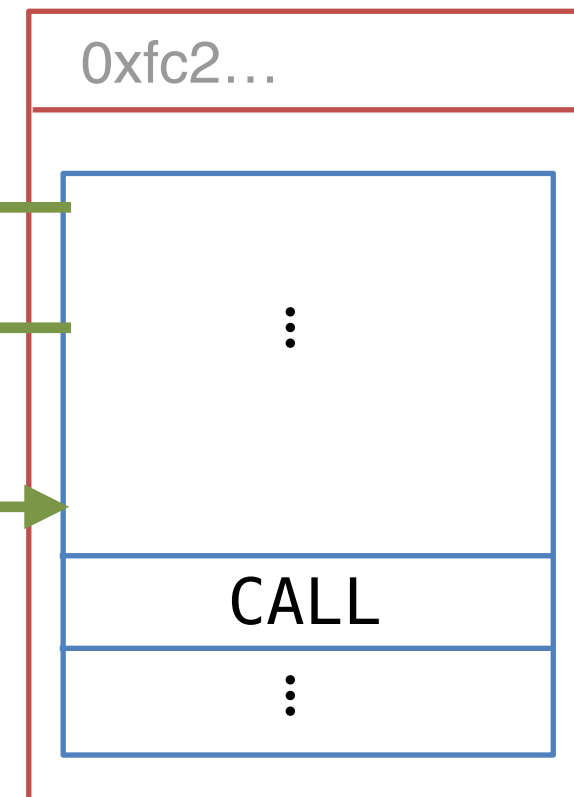
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DAO contract



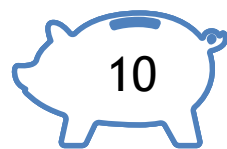
Attacker contract



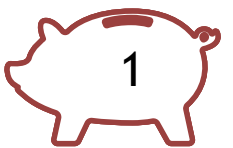
1 Eth (donate)

(withdraw)

1 Eth



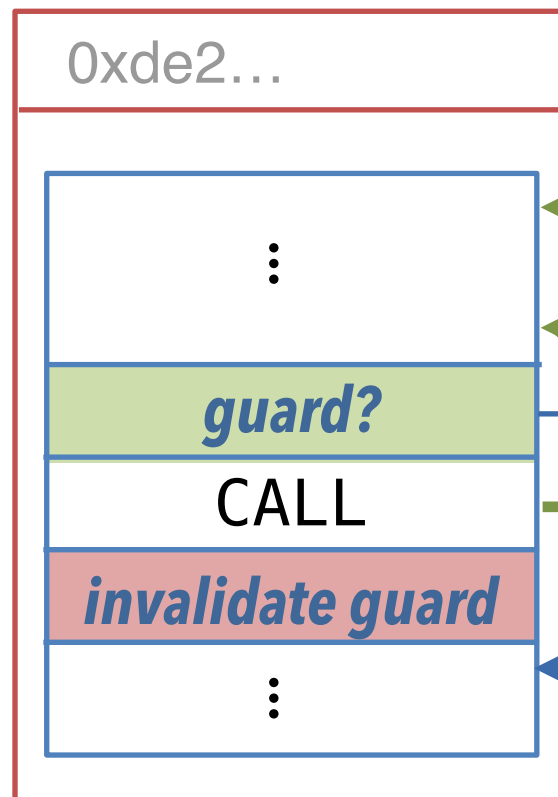
guard: true



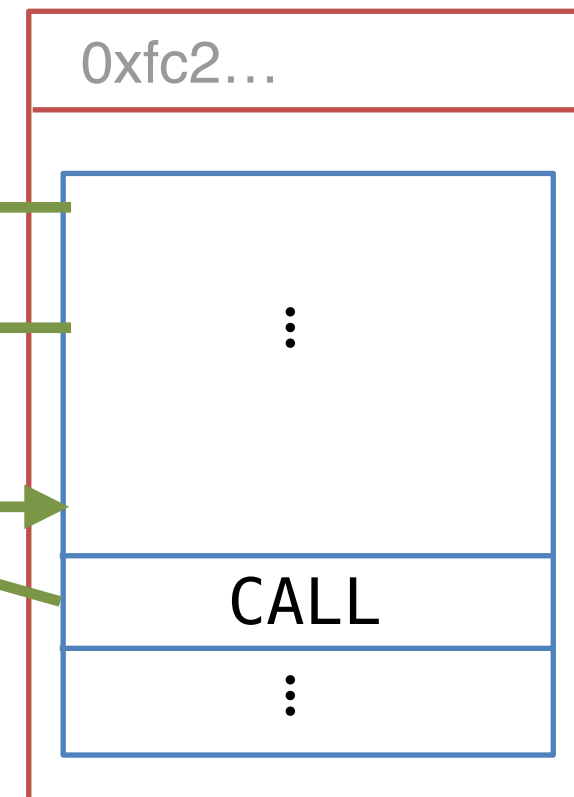
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DAO contract



Attacker contract

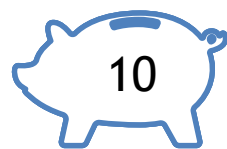


1 Eth (donate)

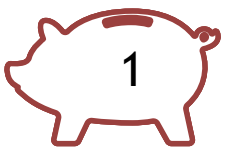
(withdraw)

(withdraw)

1 Eth



guard: true



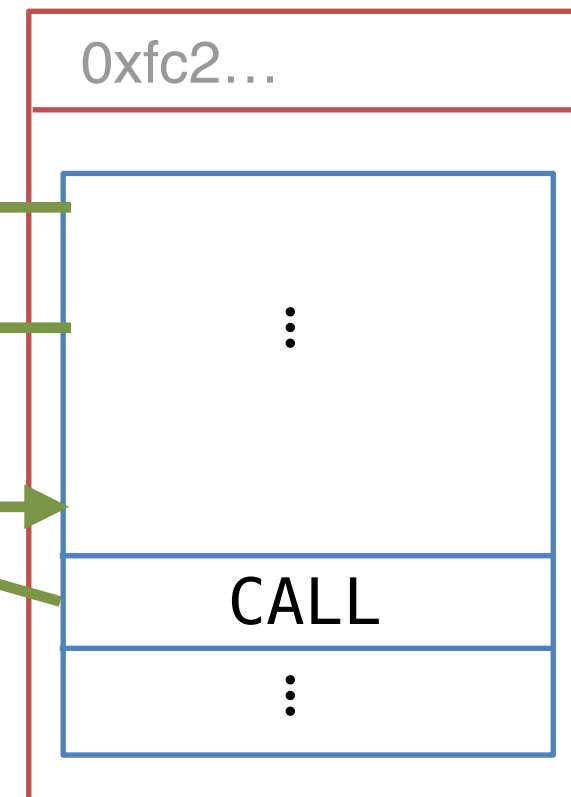
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DAO contract



Attacker contract

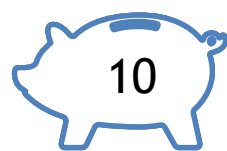


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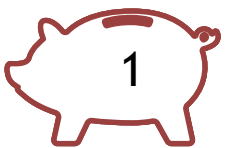
(withdraw)

(withdraw)

1 Eth



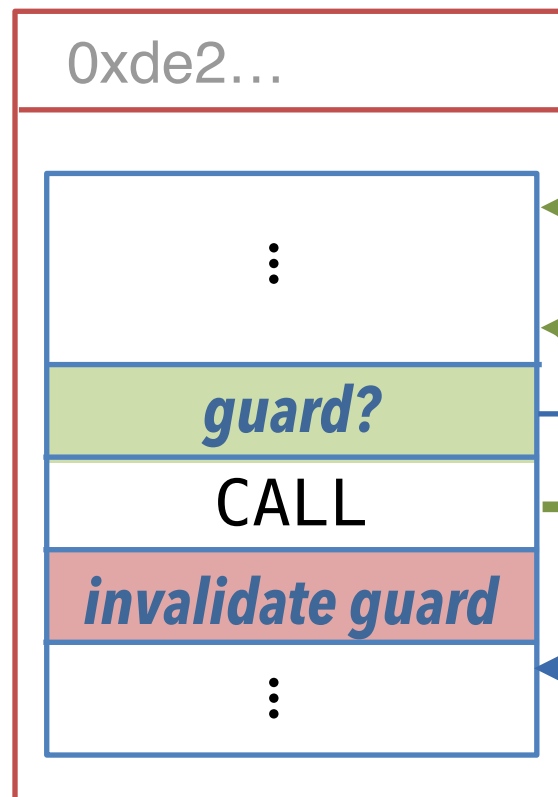
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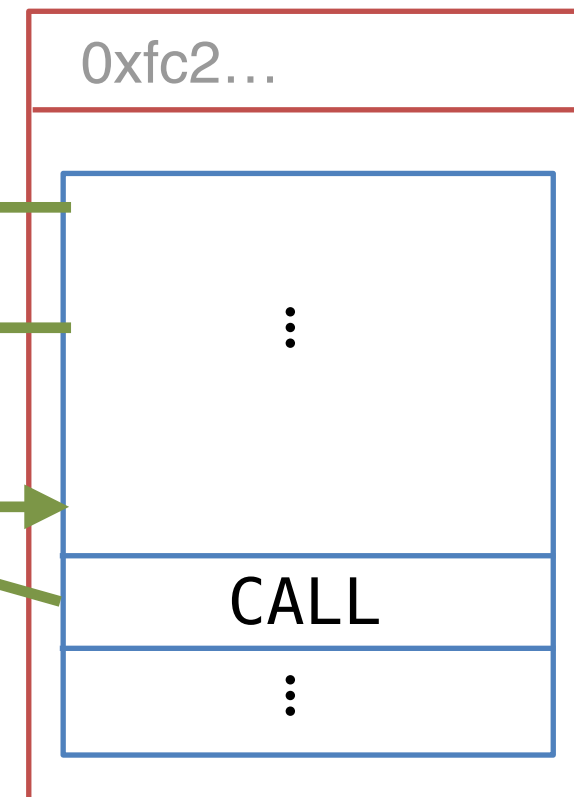
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DAO contract



Attacker contract



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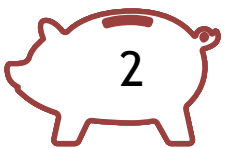
(withdraw)

(withdraw)

1 Eth



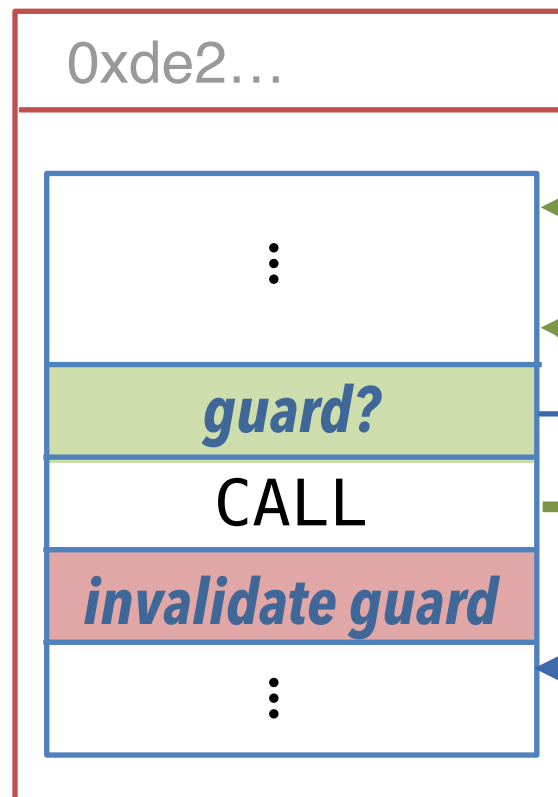
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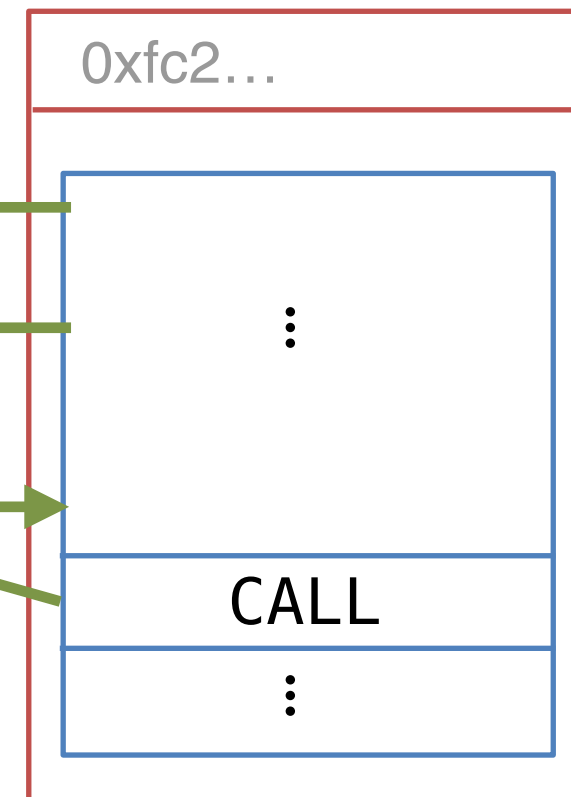
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DAO contract



Attacker contract



1 Eth (donate)

(withdraw)

(withdraw)

1 Eth

CALL

So, what did go wrong here?



# Common approach from the literature

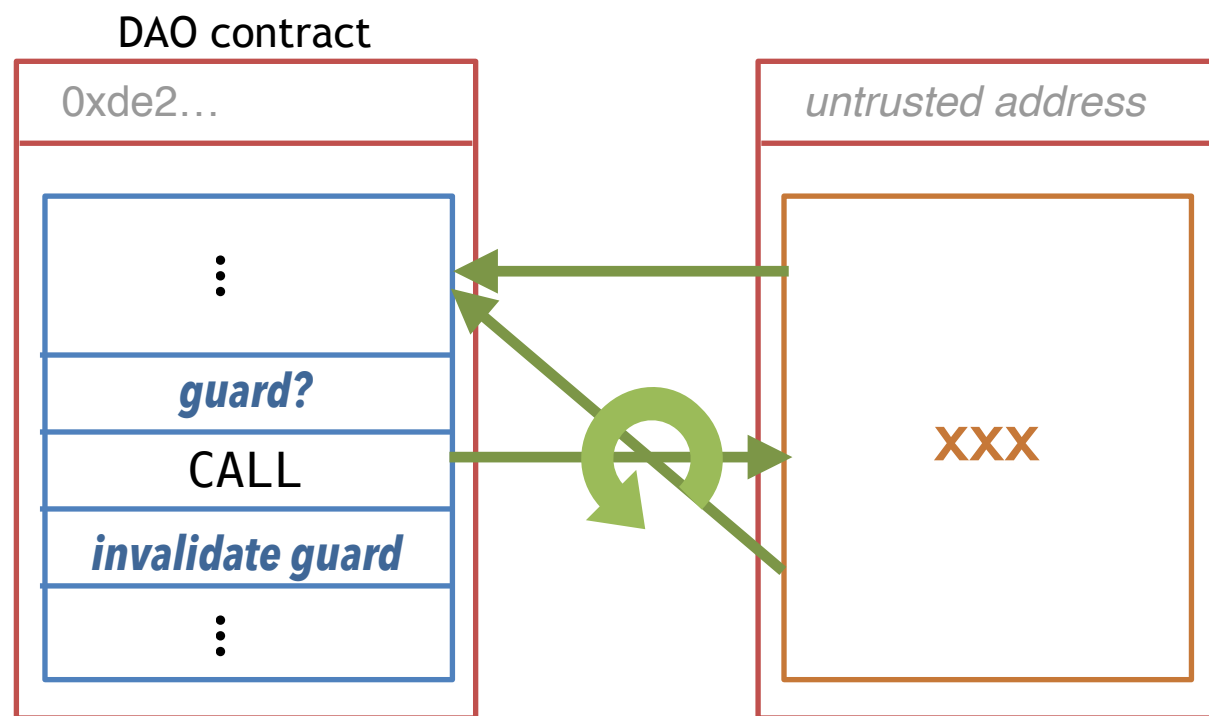
- “the guard should be invalidated before performing the call”
- Syntactic and program specific characterization
- What is the underlying semantic security property?

# Call integrity

- Reason for the DAO:  
untrusted contracts could influence the call flow of the contract (Call integrity)

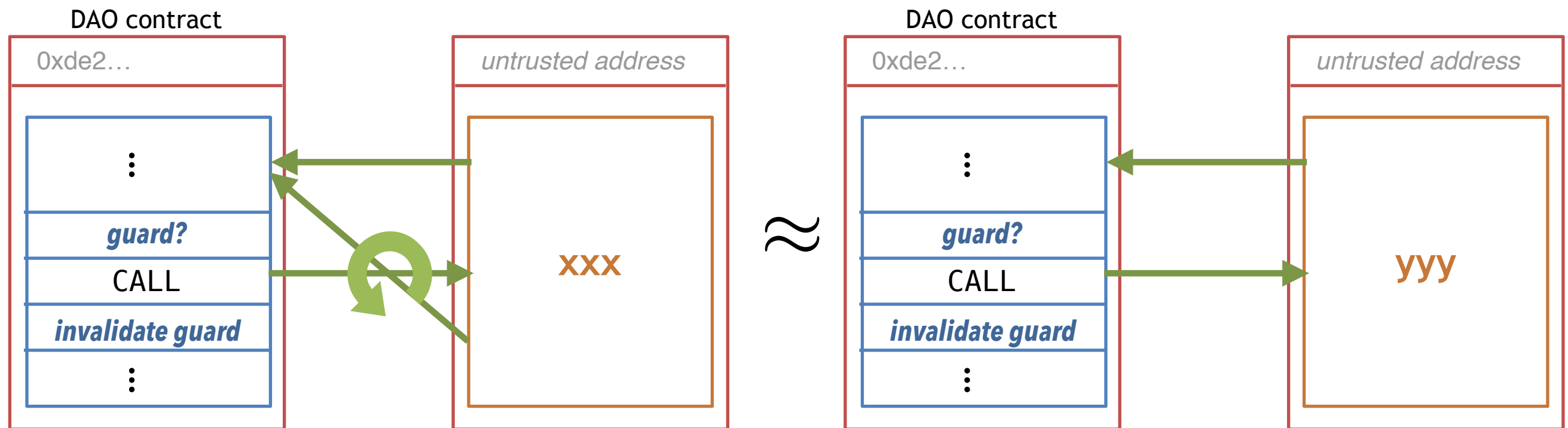
# Call integrity

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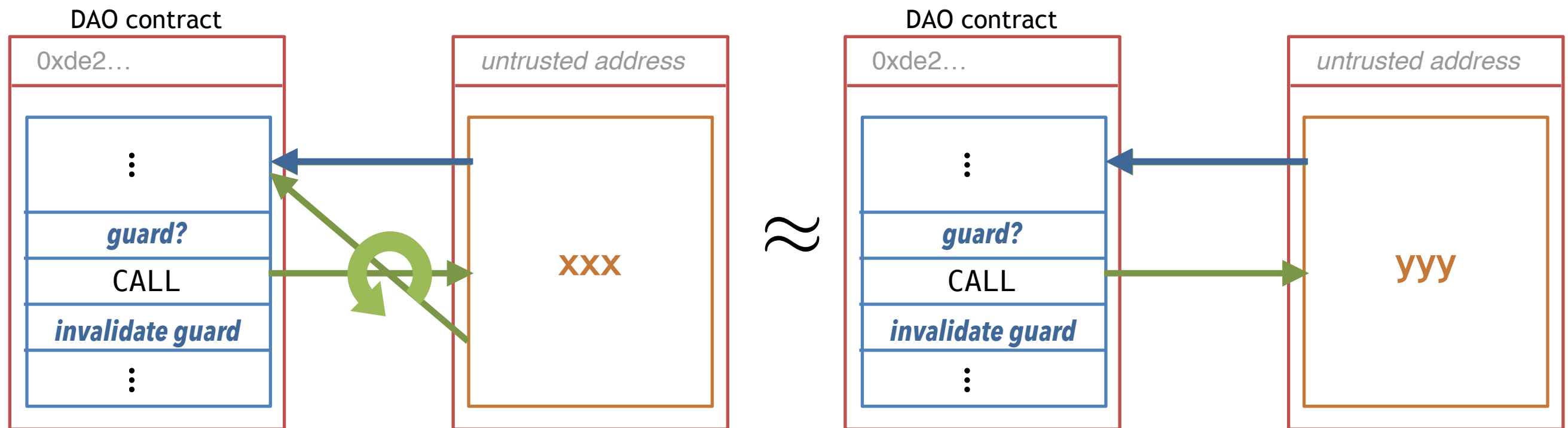
# Call integrity

- Reason for the DAO:  
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# Call integrity

- Reason for the DAO:  
untrusted contracts could influence the call flow of the contract (Call integrity)



$$\begin{aligned}
 & \Gamma \models s_c :: S \xrightarrow{\pi^*} t_c :: S \wedge \text{final}(t_c) \wedge \Gamma \models s'_c :: S' \xrightarrow{\pi'^*} t'_c :: S' \wedge \text{final}(t'_c) \\
 & \quad \xRightarrow{\quad} \underbrace{\pi \downarrow \text{calls}_c = \pi' \downarrow \text{calls}_c}_{\text{c should produce the same calls}}
 \end{aligned}$$

Differing only in codes of untrusted addresses  
 $\Rightarrow$  c is called in the same way

Note: we annotate execution states with the contract (pair of address + code) they are executing:  
 $S(l.\text{actor}, l.\text{code})$

**Hyper-Property**

# Single-entrancy

- Single-entrancy for c:  
“After being **re-entered**, contract c should perform **no more calls**”



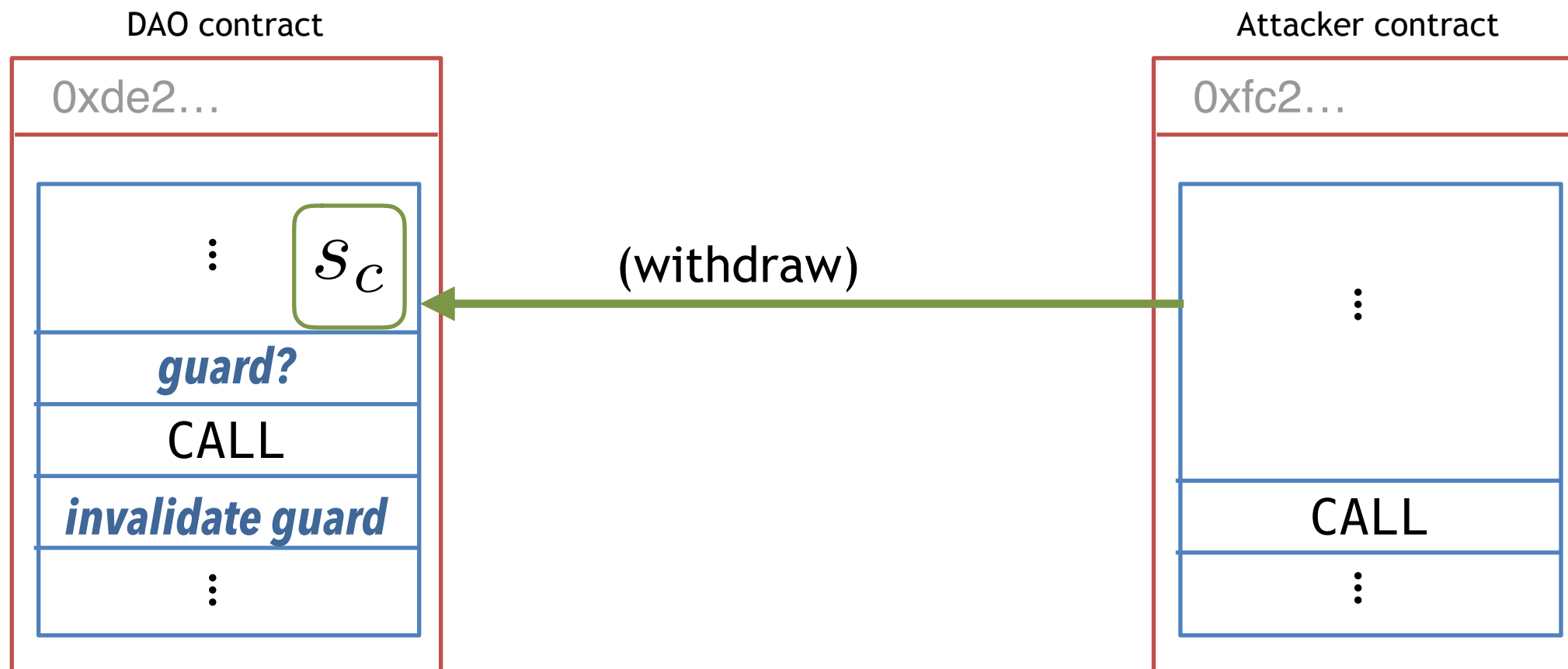
$$\neg \exists s'', c'. \Gamma \vdash s_c :: S \rightarrow^* \boxed{s''_{c'}} :: \boxed{s'_c} :: S' + + \boxed{s_c} :: S$$

The diagram shows a state transition sequence. A solid blue arrow points from the bottom of the  $\boxed{s'_c}$  box to the bottom of the  $\boxed{s''_{c'}}$  box. A dashed green arrow points from the top of the  $\boxed{s_c}$  box to the top of the  $\boxed{s'_c}$  box.

*Reachability property*

# Single-entrancy

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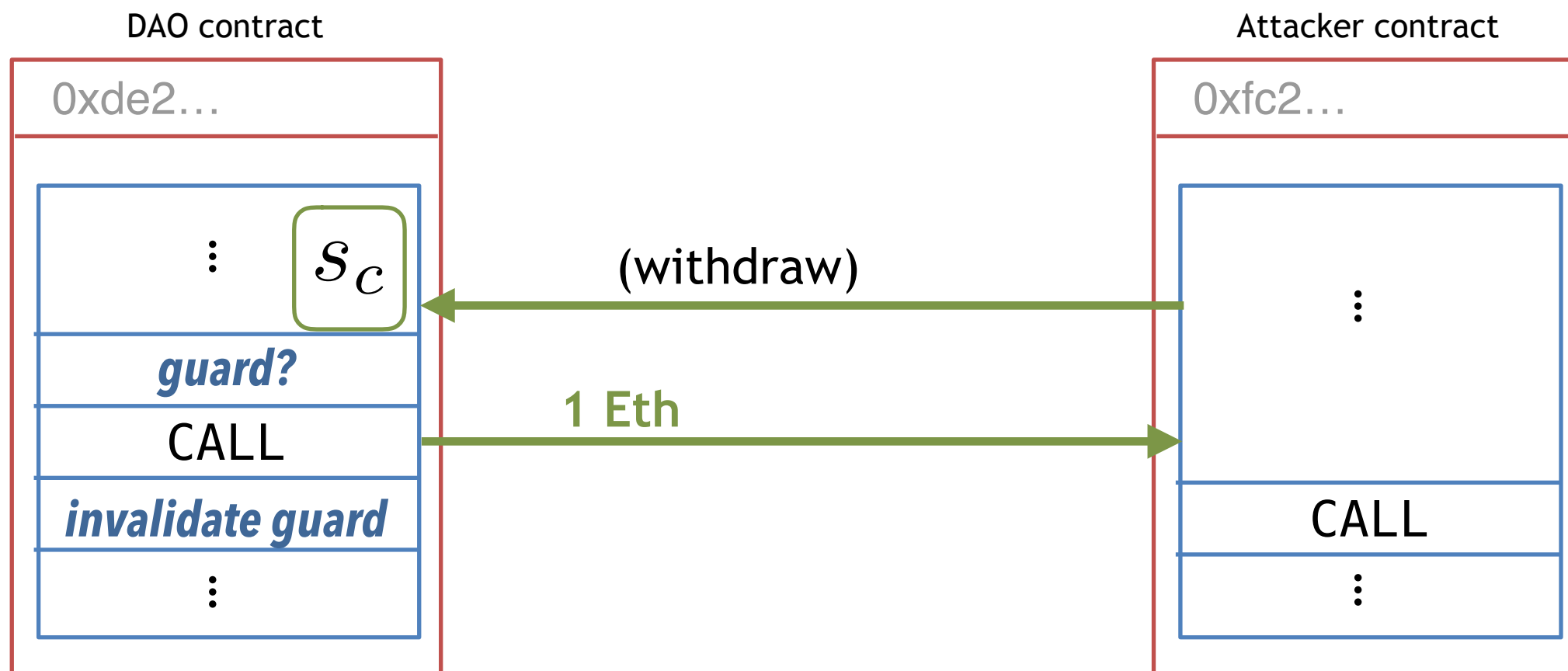
$$\neg \exists s'', c'. \Gamma \vdash s_c :: S \rightarrow^* \boxed{s''_{c'}} :: \boxed{s'_c} :: S' + + \boxed{s_c} :: S$$

The diagram shows a state transition graph for the formula. It starts with a red box  $s''_{c'}$ , which has a blue arrow pointing to a blue box  $s'_c$ . From  $s'_c$ , a blue arrow points back to  $s''_{c'}$  and a green dotted arrow points to a green box  $s_c$ . From  $s_c$ , a green dotted arrow points back to  $s'_c$ .

**Reachability property**

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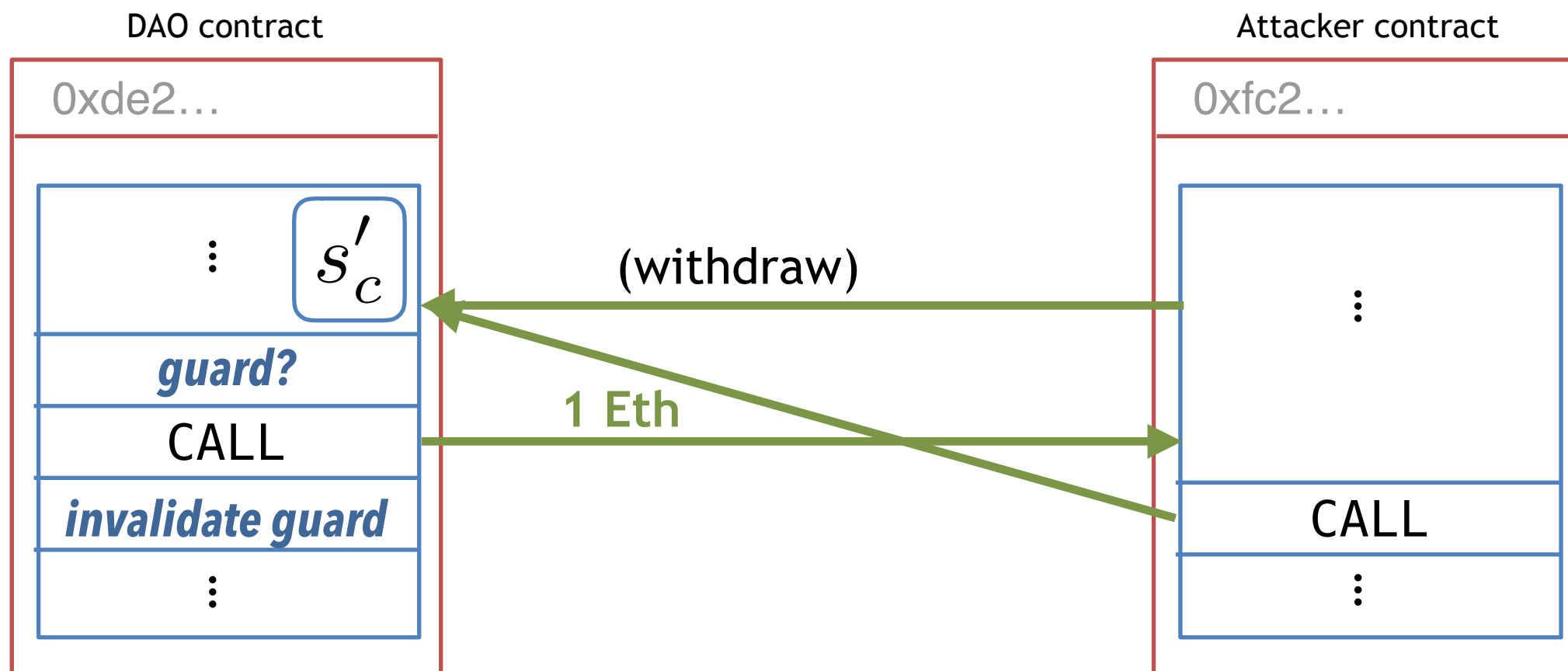
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*Reachability property*



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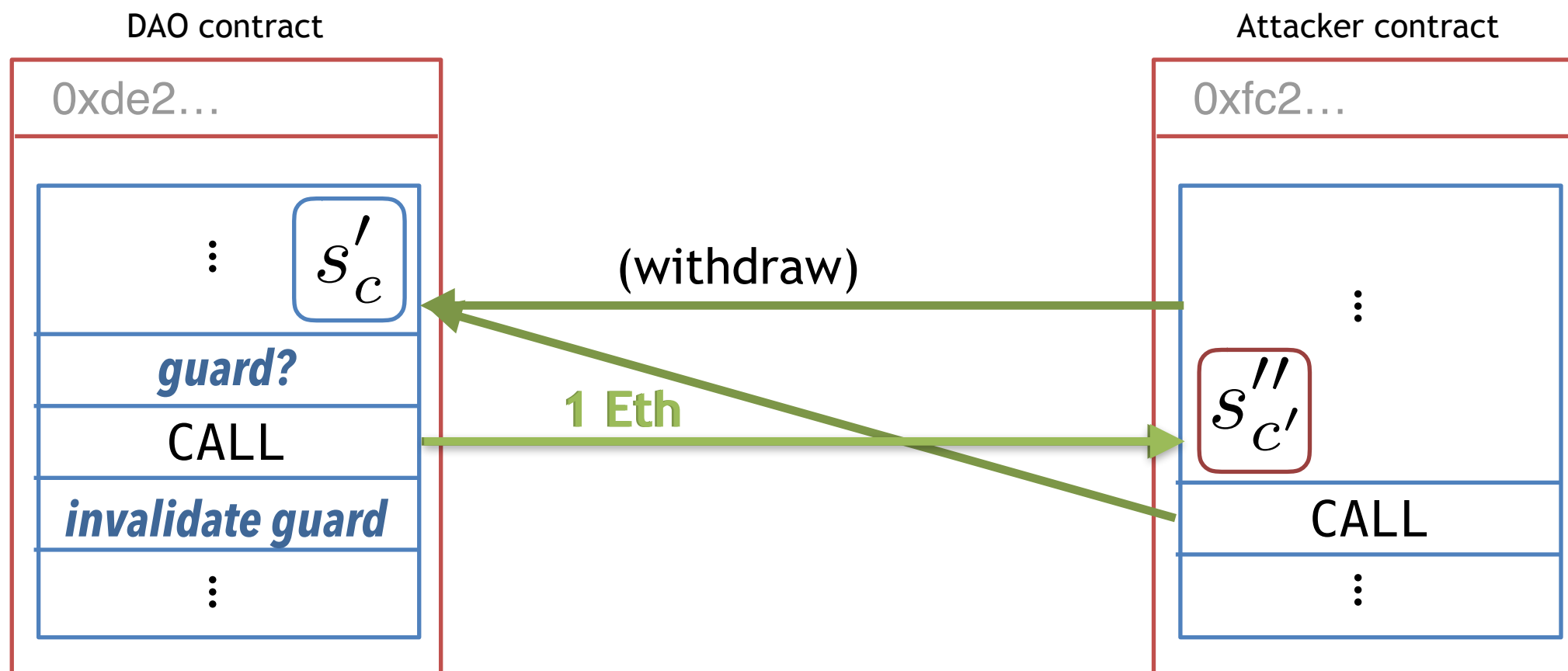


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**Reachability property**

# Single-entrancy

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**Reachability property**

# Proof technique for call integrity

**Single-entrancy**

“contract should not  
depend on return value of  
calls to untrusted  
contracts”

“contract should not  
depend on untrusted  
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accesses directly)”



**Call Integrity**

# Proof technique for call integrity

Single-entrancy

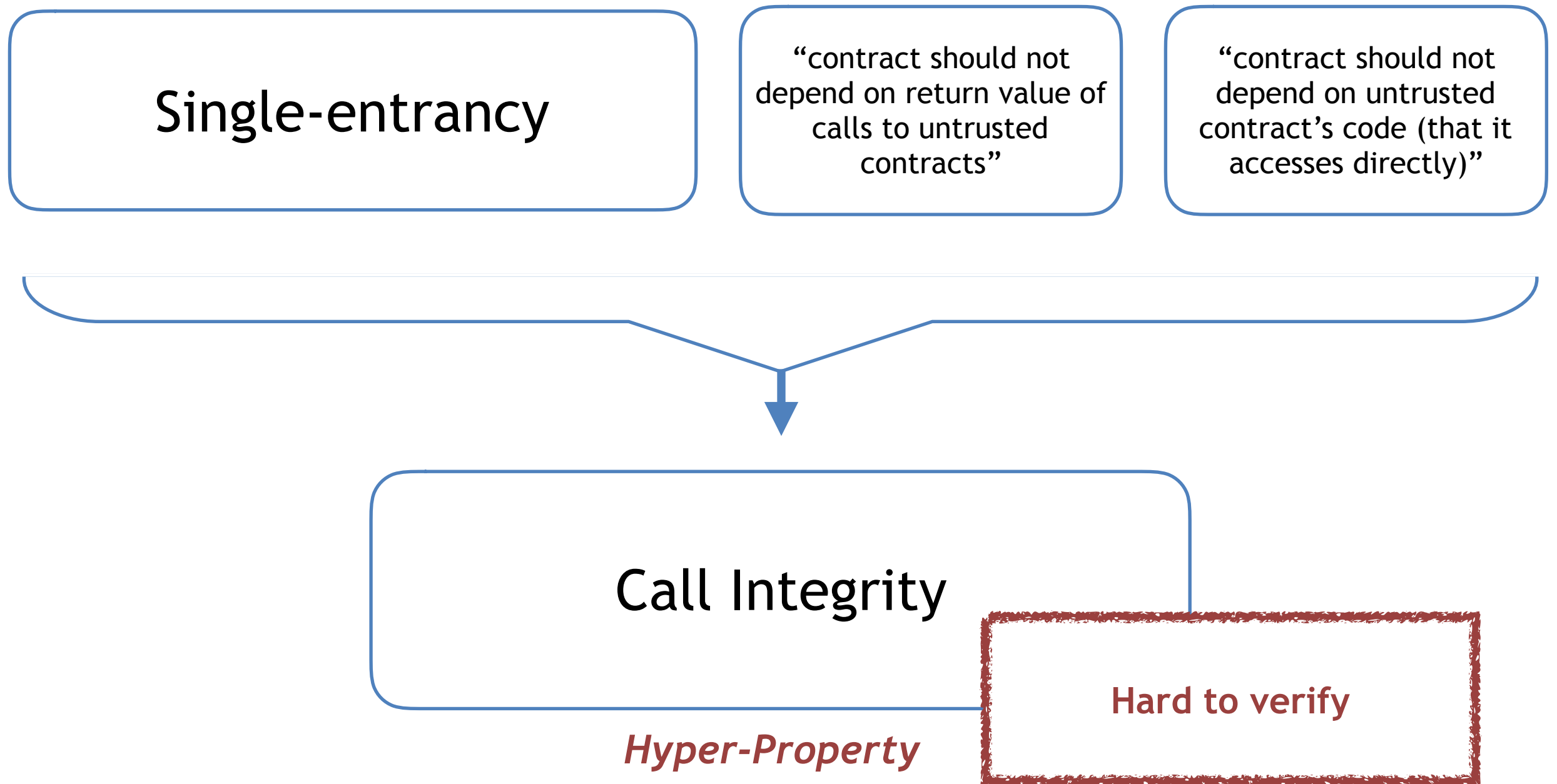
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Call Integrity

Hard to verify

*Hyper-Property*



# Proof technique for call integrity

## *Reachability Property*

Single-entrancy

## *Value-Dependency Properties*

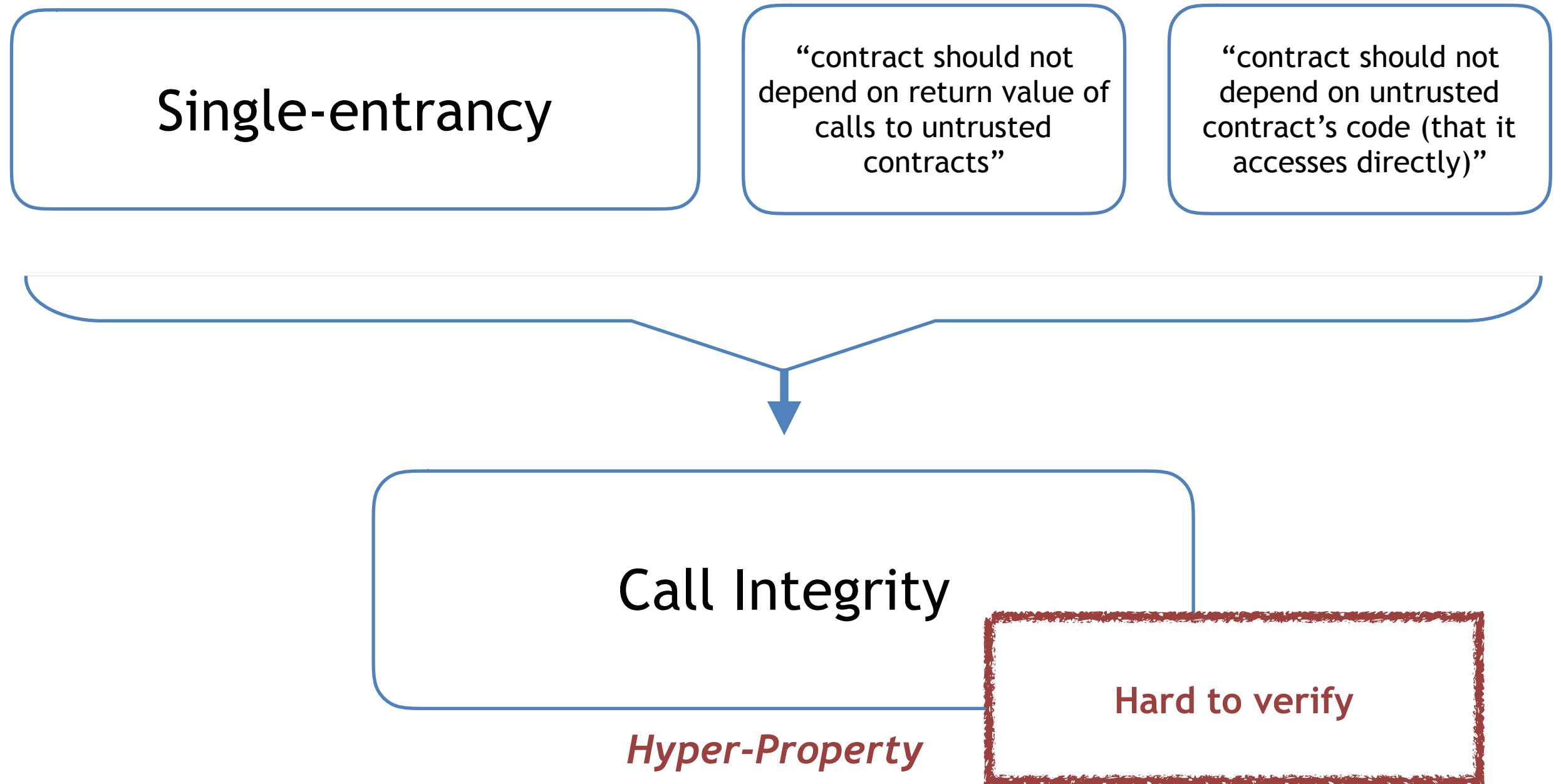
“contract should not depend on return value of calls to untrusted contracts”

“contract should not depend on untrusted contract’s code (that it accesses directly)”

Call Integrity

*Hyper-Property*

Hard to verify



# Proof technique for call integrity

## *Reachability Property*

Single-entrancy

## *Value-Dependency Properties*

“contract should not depend on return value of calls to untrusted contracts”

“contract should not depend on untrusted contract’s code (that it accesses directly)”

Provable by static analysis: EtherTrust



Call Integrity

Hard to verify

*Hyper-Property*

# Atomicity

- Inconsistencies due to unhandled gas exceptions

```
contract DAO {
  mapping (address => uint) donations;

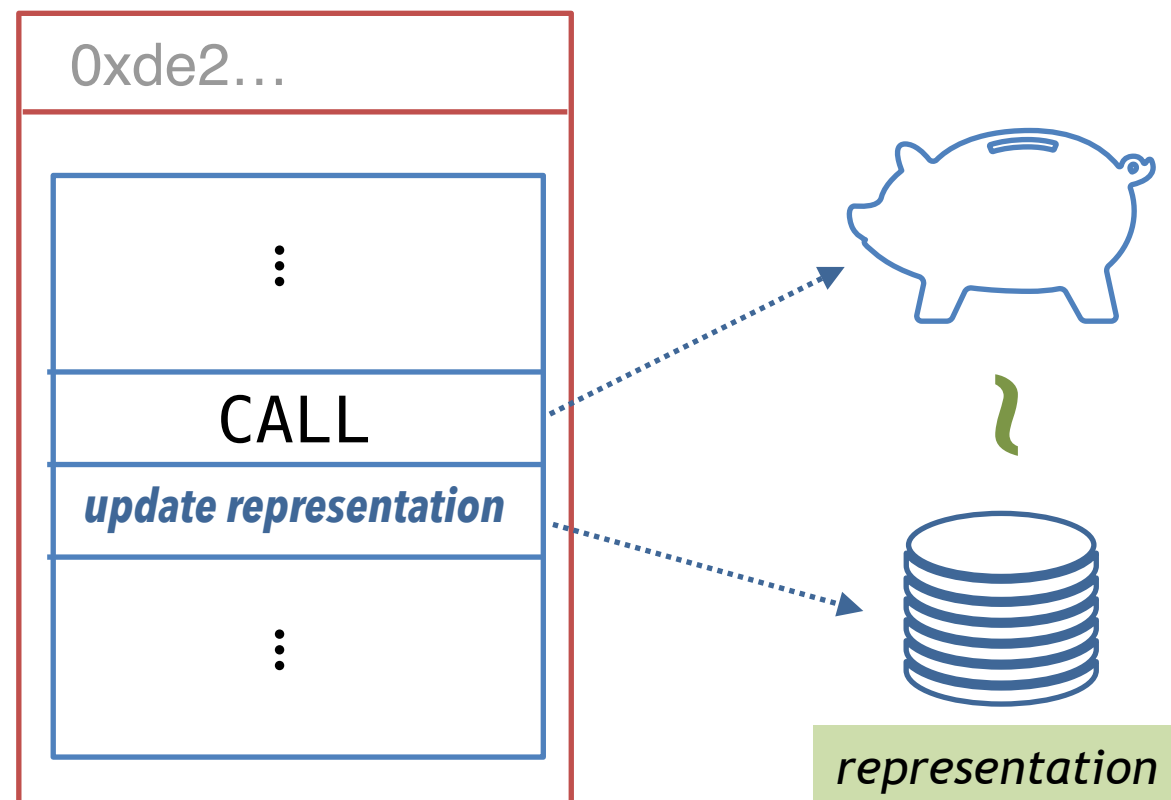
  function donate() {
    donations[msg.sender] += msg.value;
  }

  function withdraw(){
    msg.sender.call.value(donations[msg.sender])();
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  }
}
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# Atomicity

- Inconsistencies due to unhandled gas exceptions

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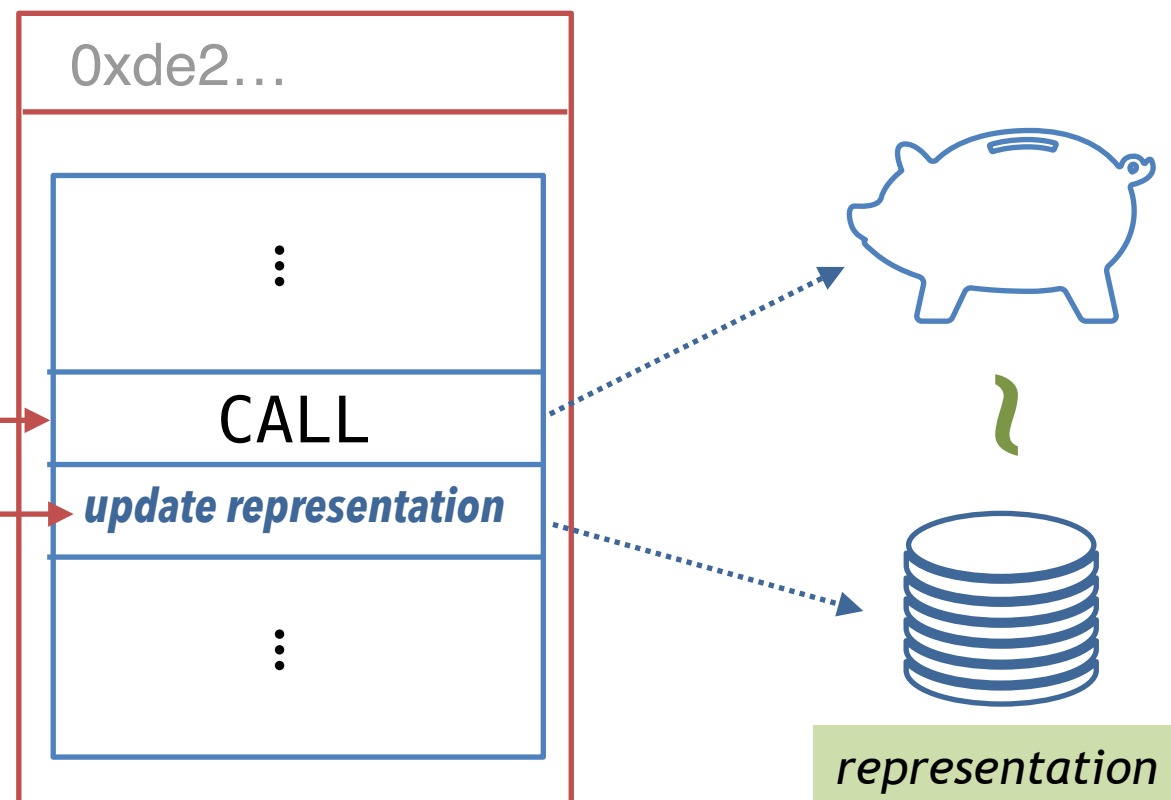




# Atomicity

- Inconsistencies due to unhandled gas exceptions

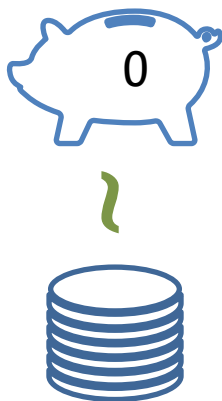
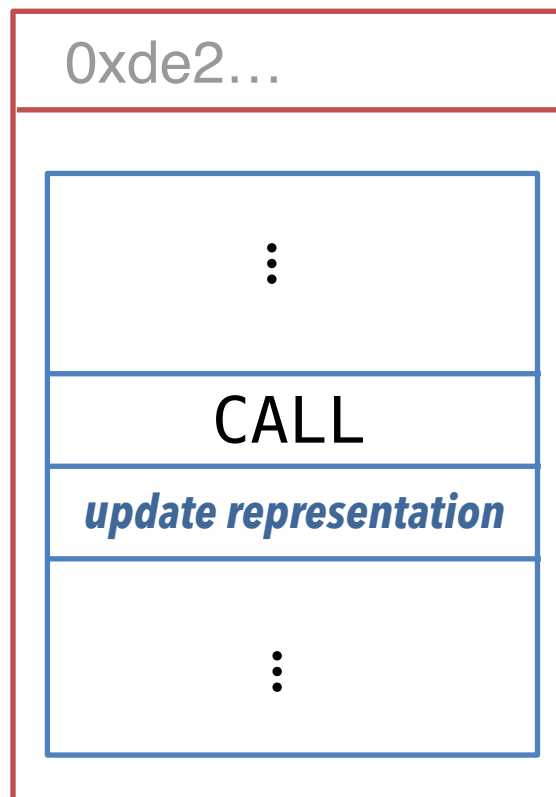
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# Contract inconsistencies

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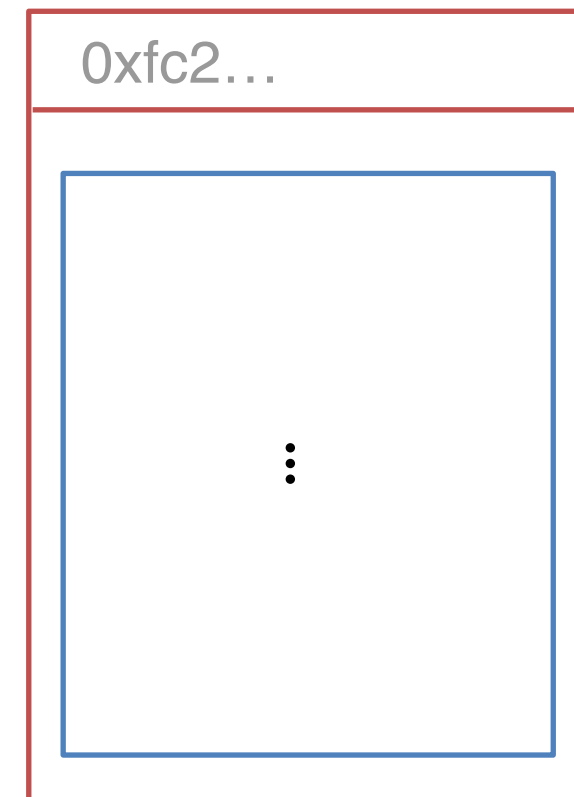
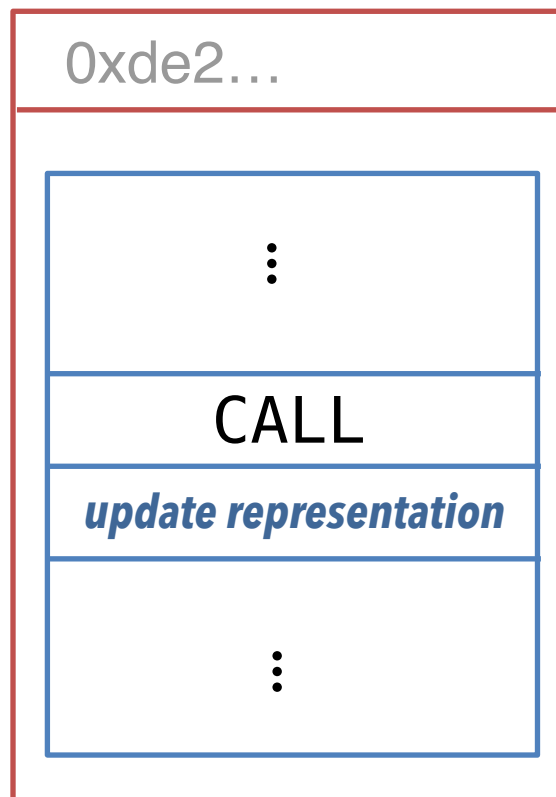
DAO contract



# Contract inconsistencies

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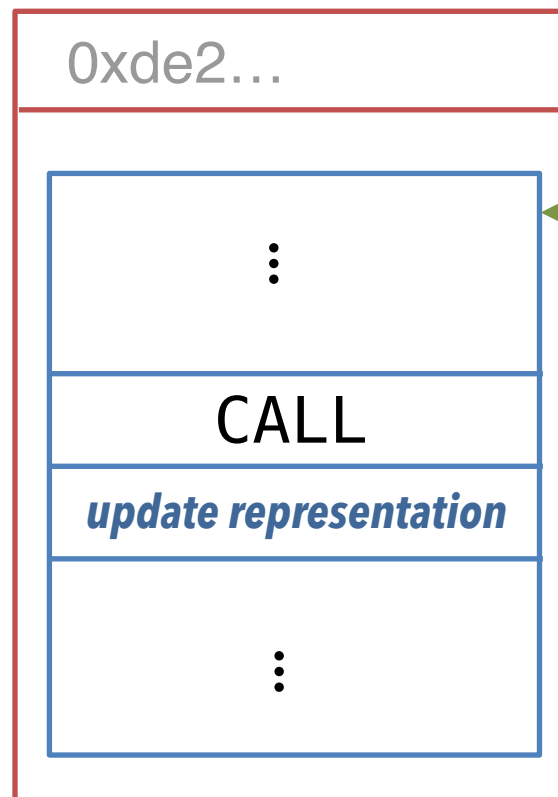
DAO contract



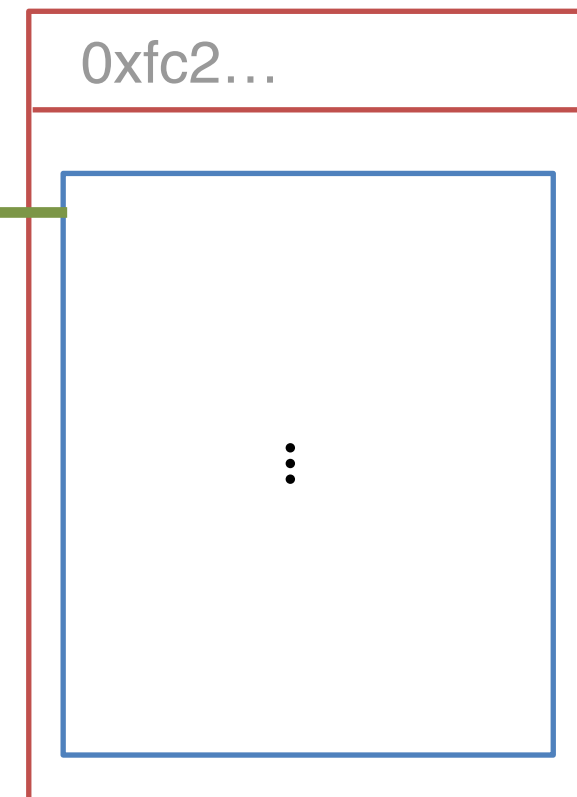
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```

DAO contract



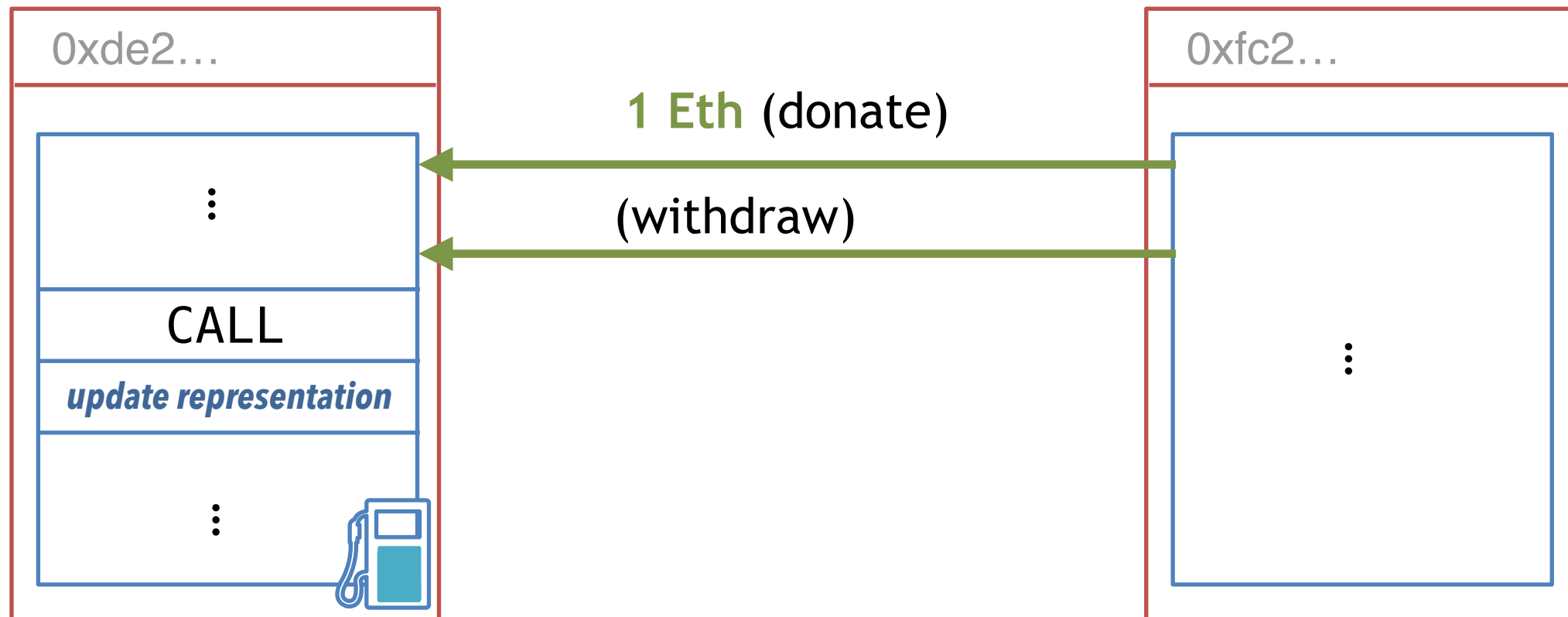
1 Eth (donate)



# Contract inconsistencies

```
contract DAO {  
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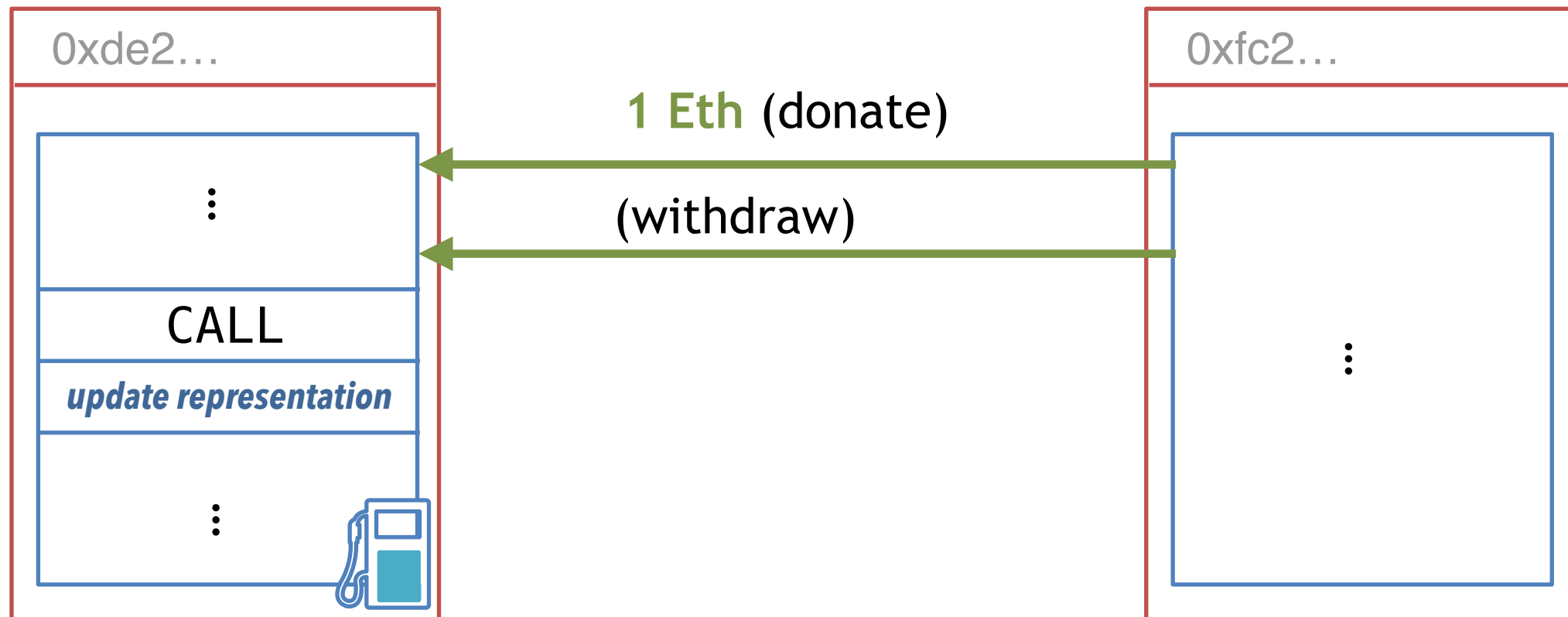
DAO contract



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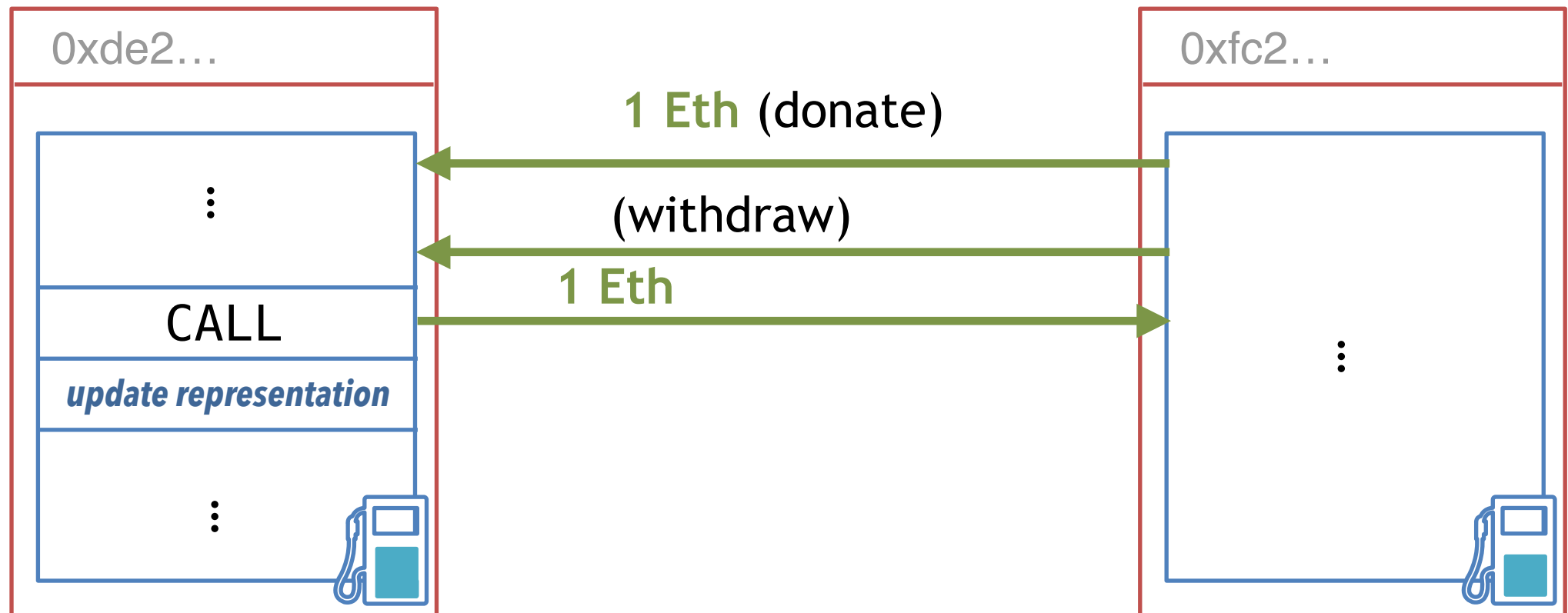
DAO contract



# Contract inconsistencies

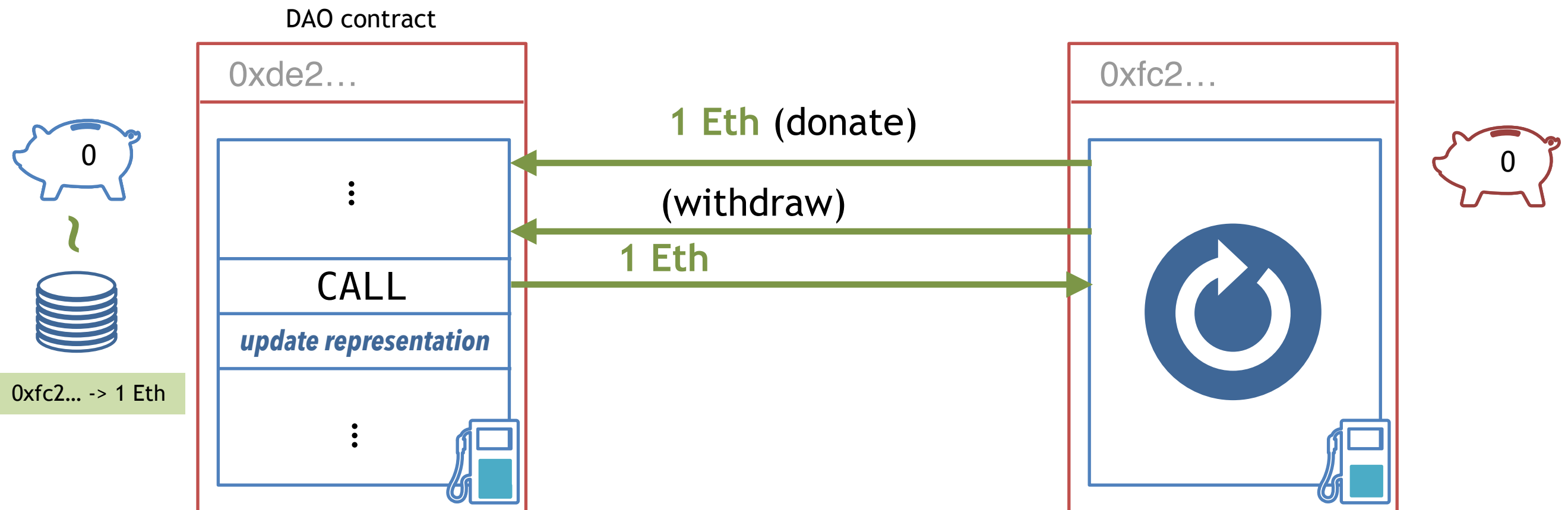
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DAO contract



# Contract inconsistencies

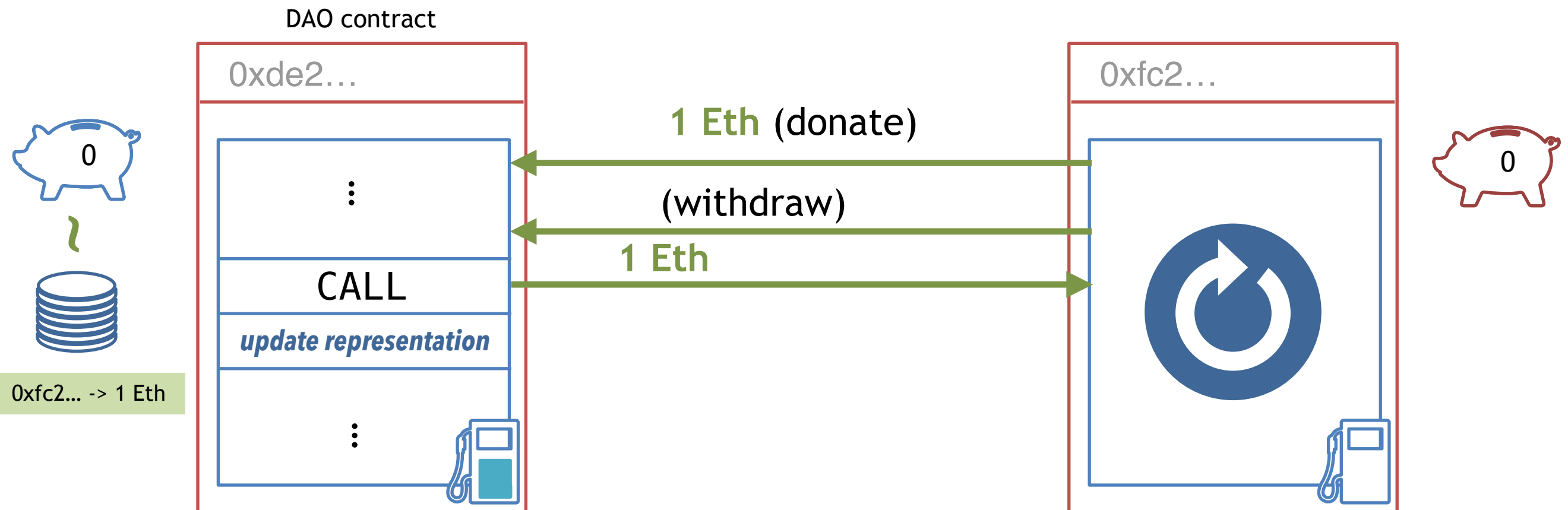
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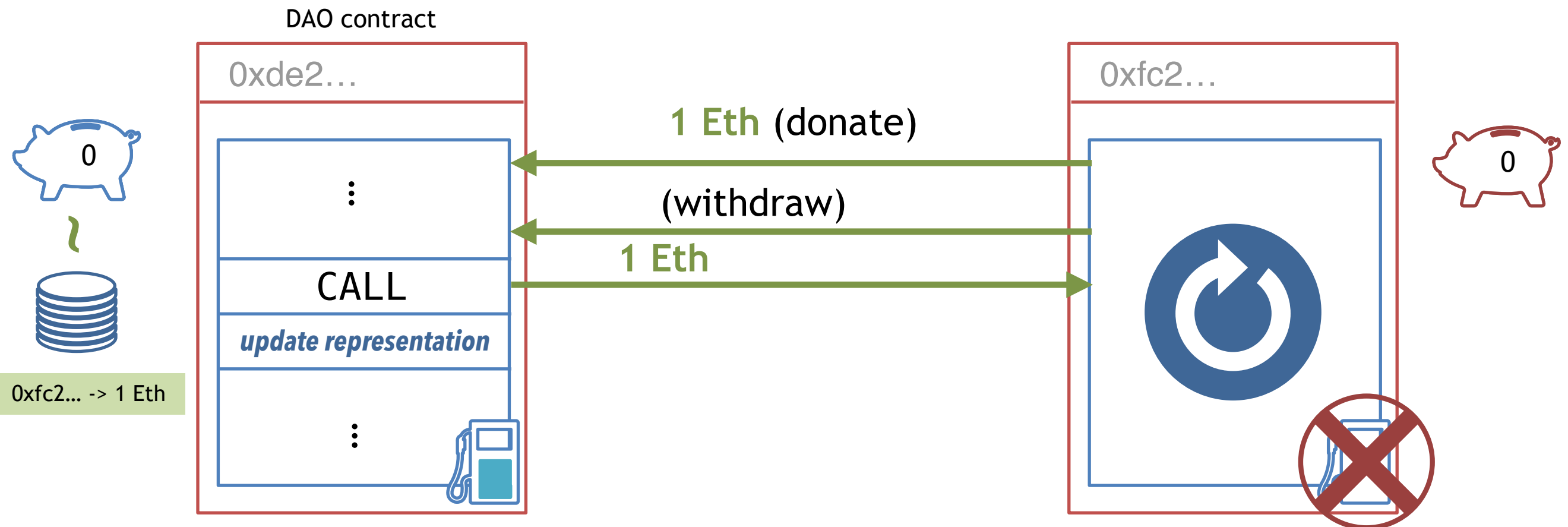
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# Contract inconsistencies

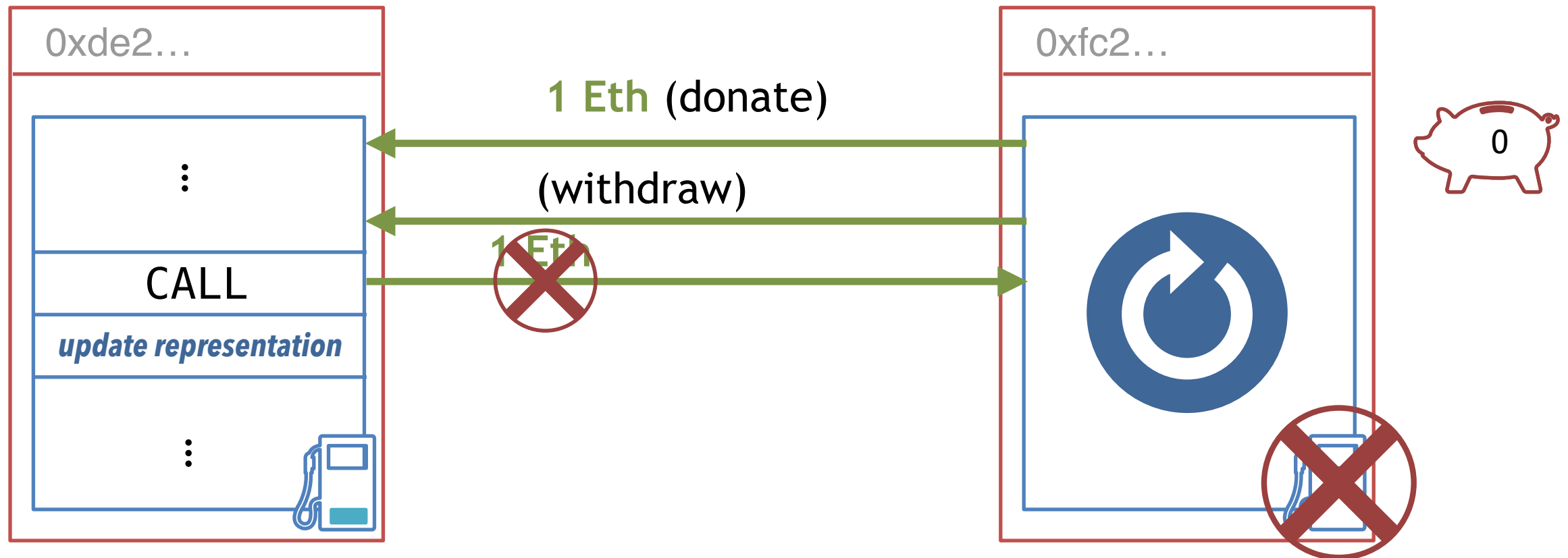
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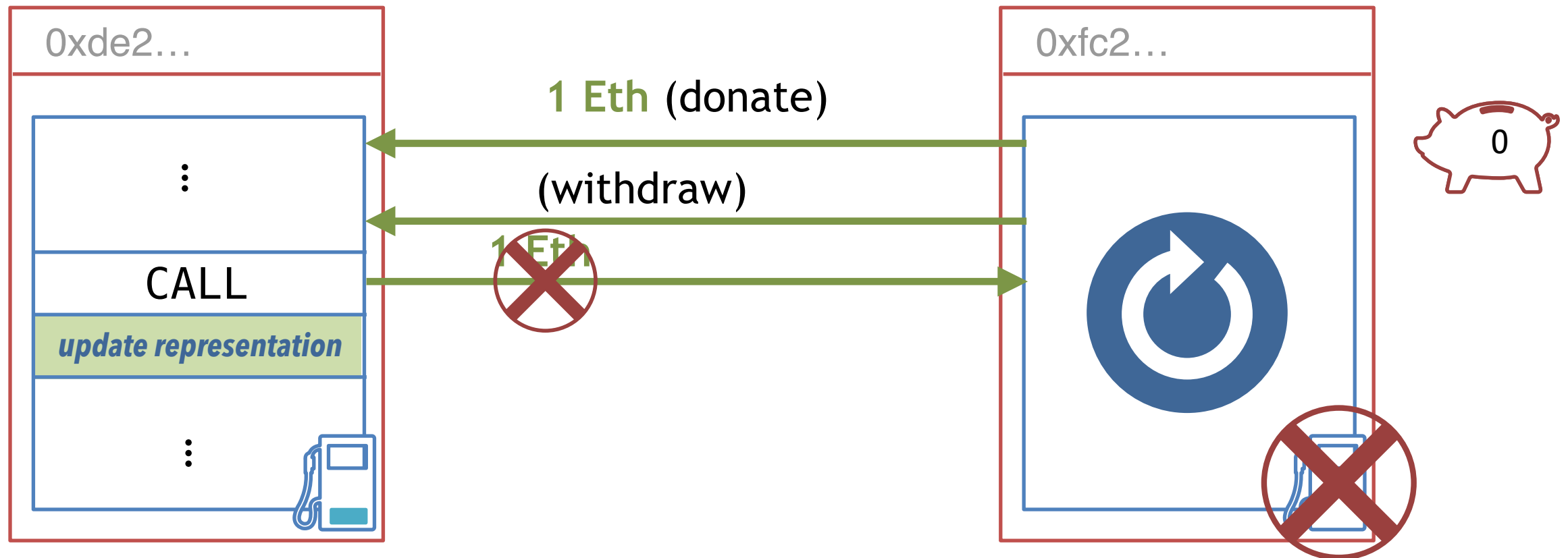
DAO contract



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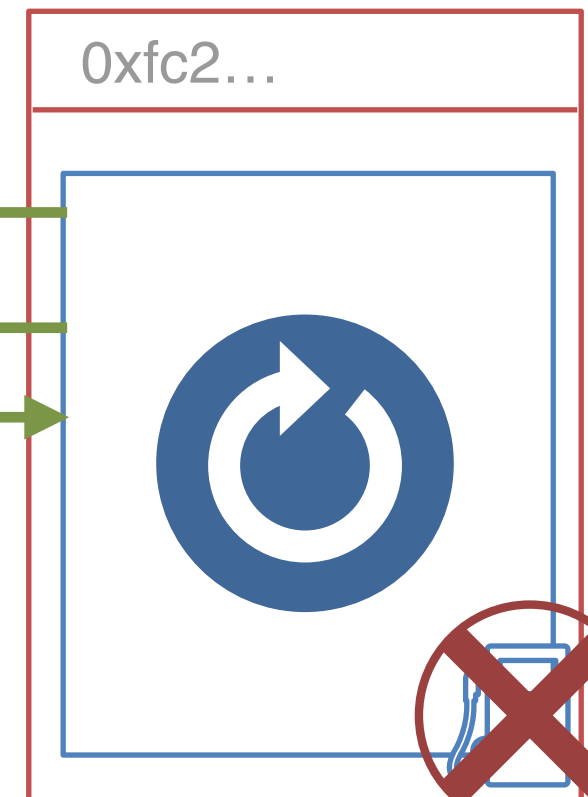
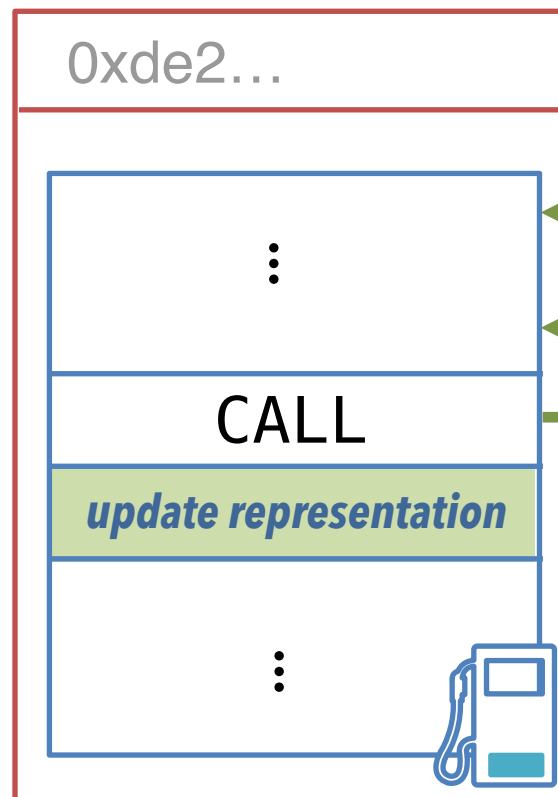
DAO contract



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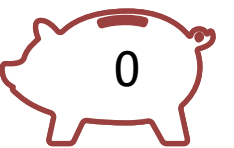
DAO contract



1 Eth (donate)

(withdraw)

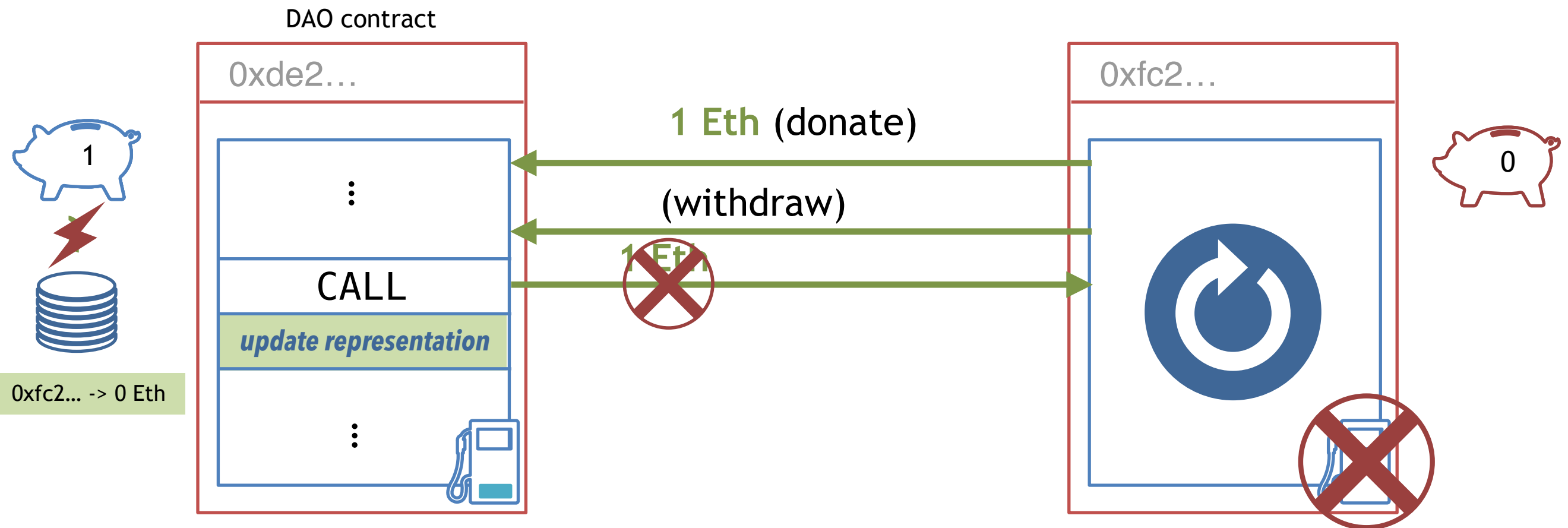
1 Eth



0xfc2... -> 0 Eth

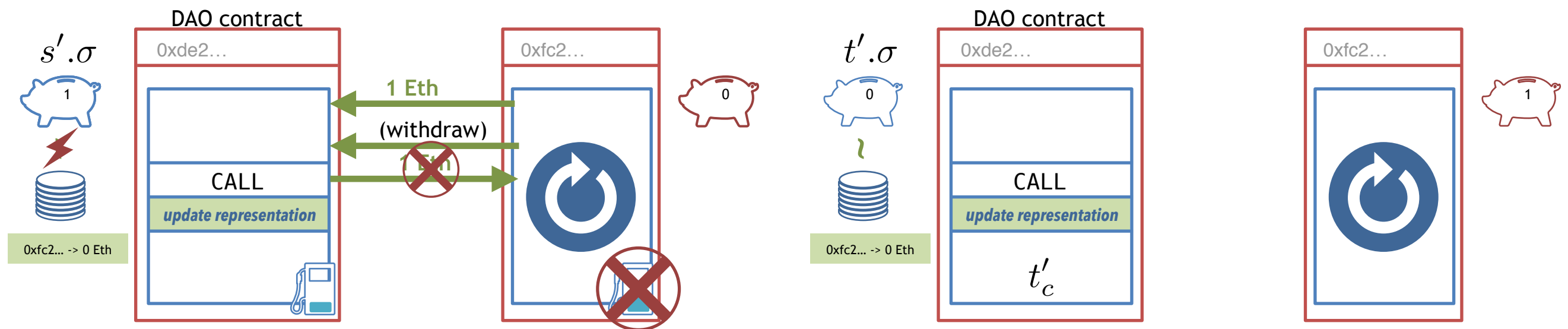
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```



# Atomicity

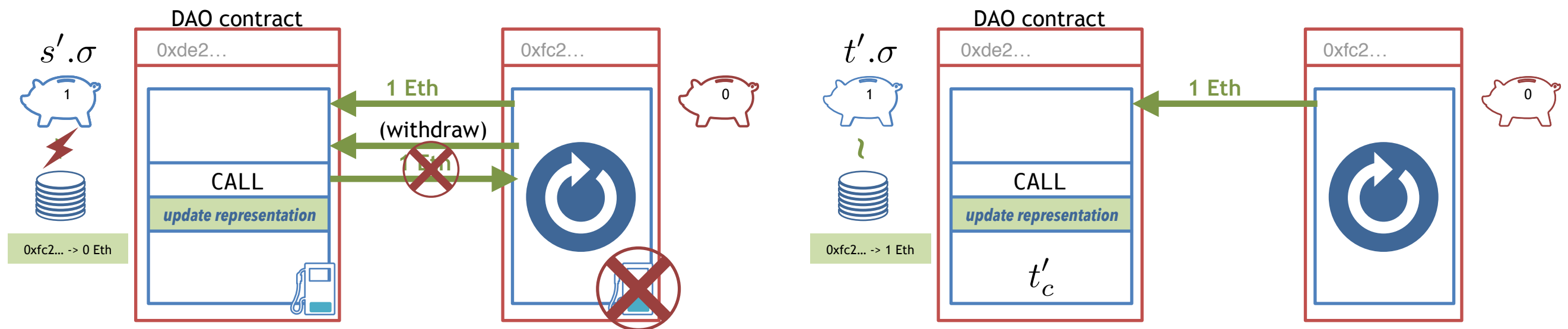
- Reason for inconsistency: the (effects of) a contract's execution should not depend on the amount of gas given for execution



$$\Gamma \models s_c :: S \rightarrow^* s'_c :: S \wedge final(s') \wedge \Gamma \models t_c :: S \rightarrow^* t'_c :: S \wedge final(t') \\ \Rightarrow s'.\sigma = t'.\sigma \vee s.\sigma = s'.\sigma \vee t.\sigma = t'.\sigma$$

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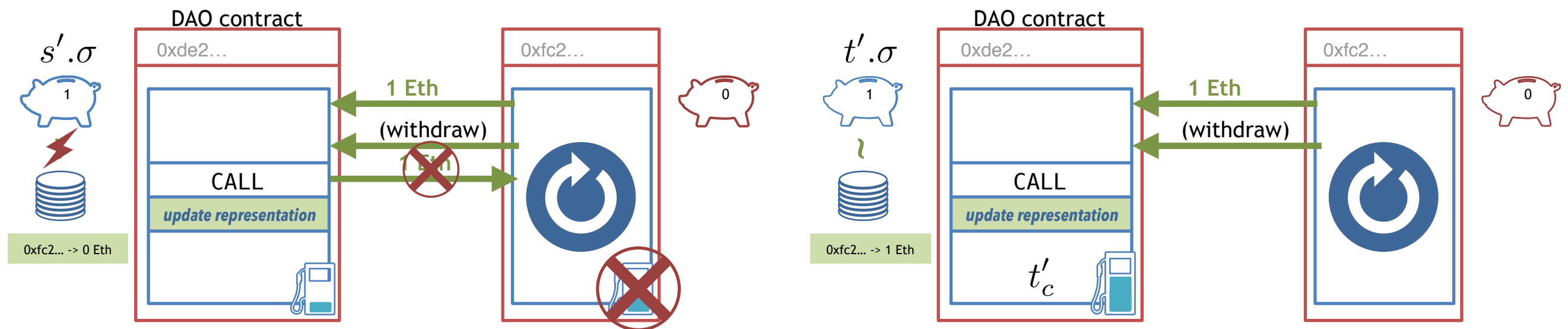
Initial states only  
differing in gas

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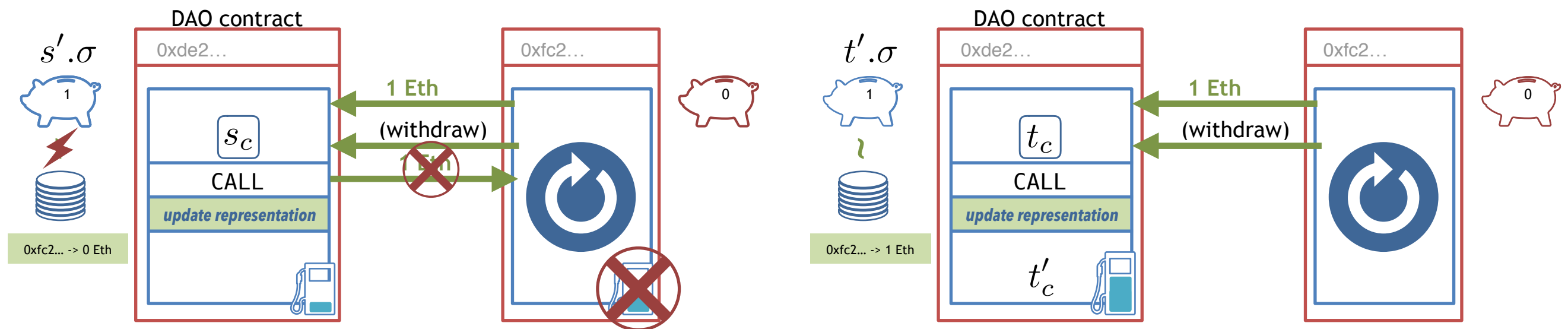


Initial states only  
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Initial states only  
differing in gas

$$s.\sigma = t.\sigma$$

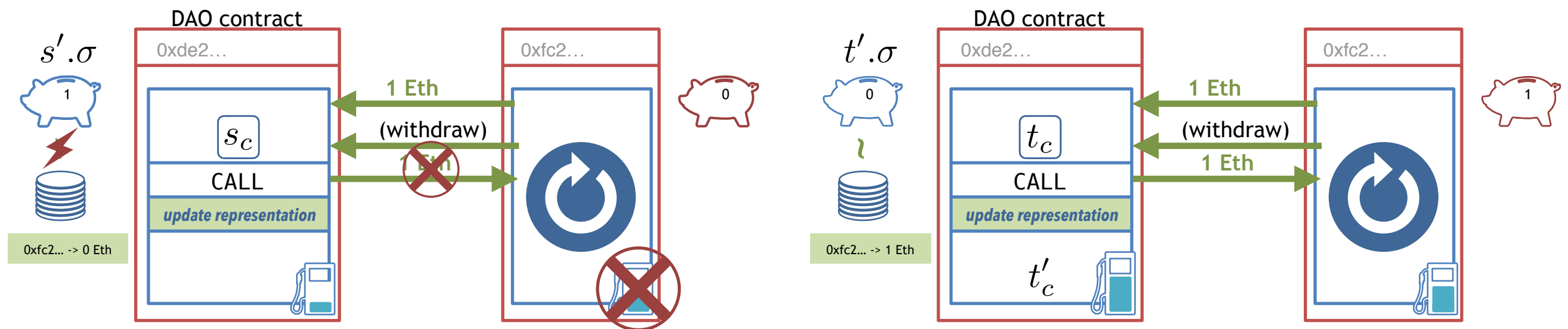


$$0xfc2... \rightarrow 1 \text{ Eth}$$

$$\Gamma \models [s_c] :: S \rightarrow^* s'_c :: S \wedge final(s') \wedge \Gamma \models [t_c] :: S \rightarrow^* t'_c :: S \wedge final(t') \\ \Rightarrow s'.\sigma = t'.\sigma \vee s.\sigma = s'.\sigma \vee t.\sigma = t'.\sigma$$

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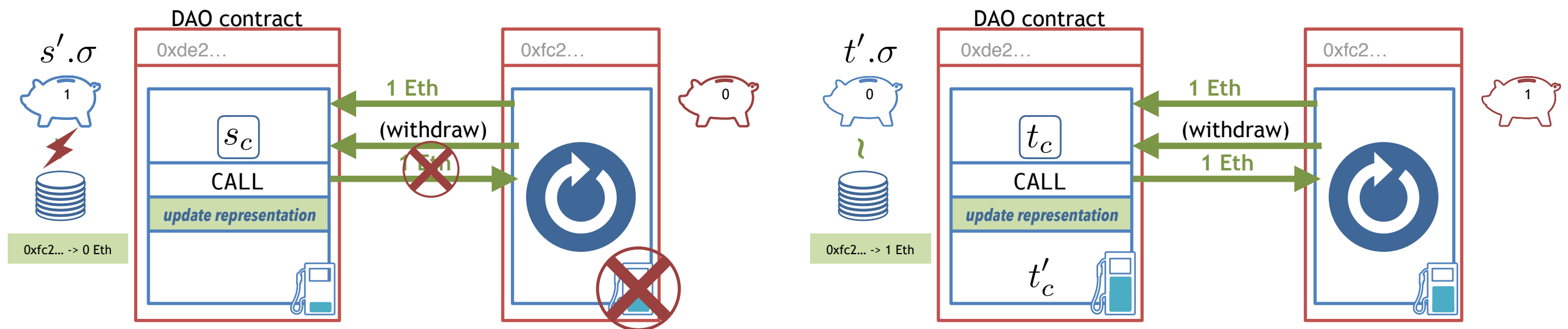


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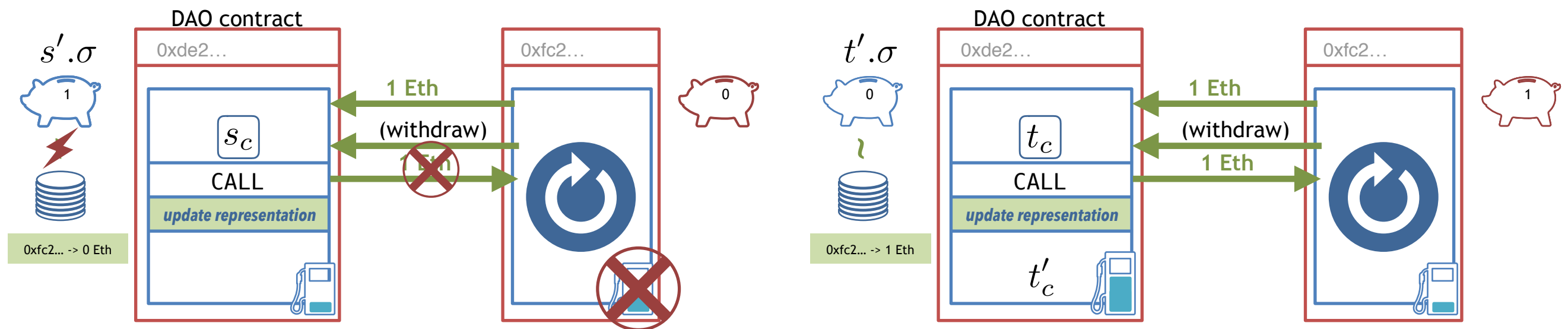


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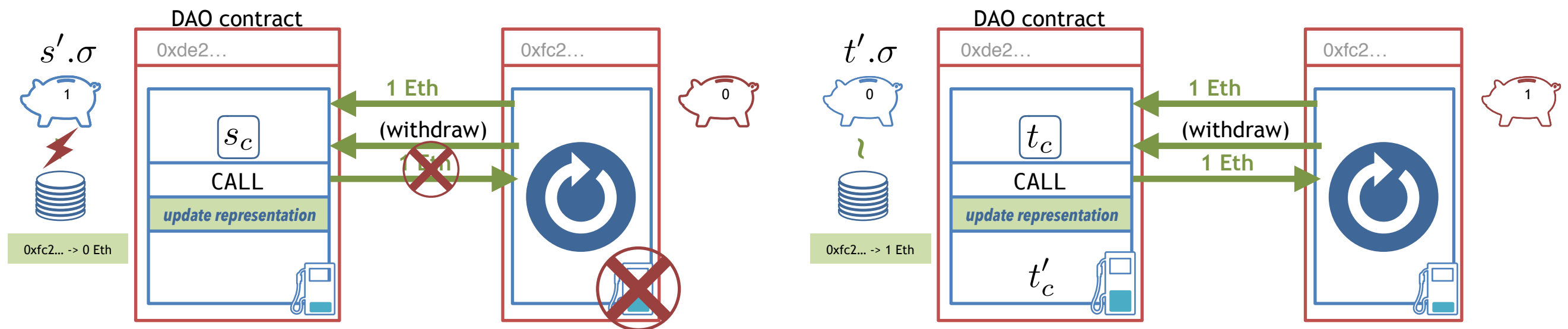


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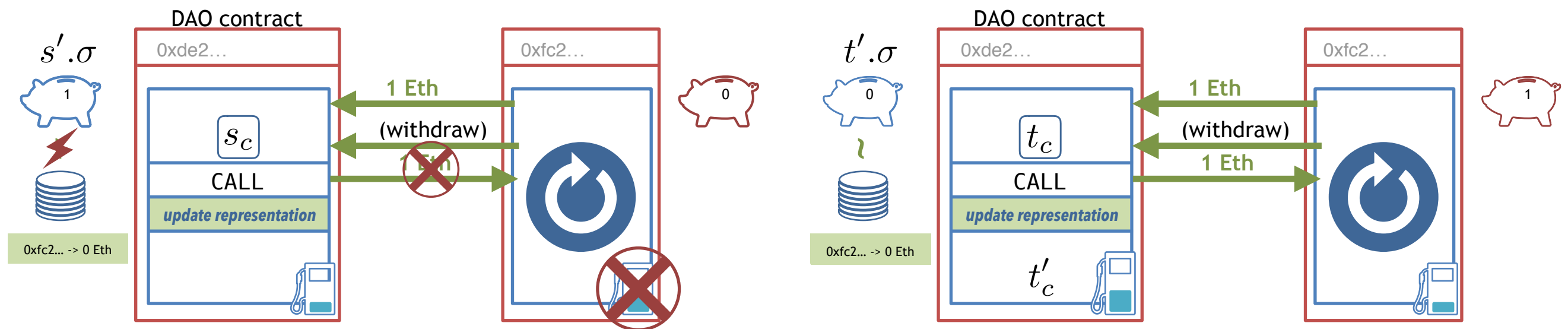


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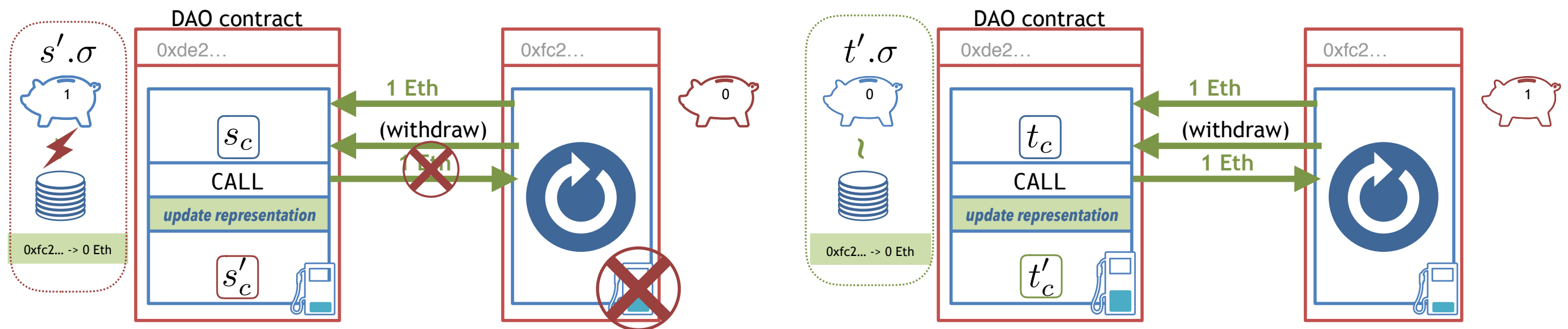


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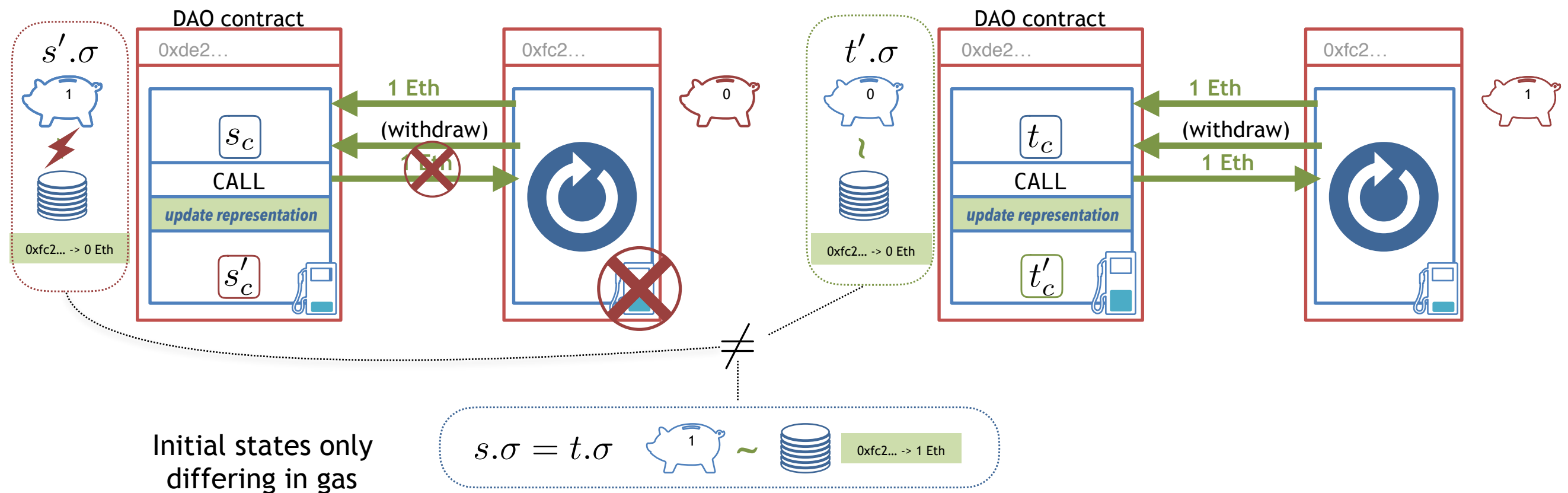
$$0xfc2... \rightarrow 1 \text{ Eth}$$

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How can all of that be  
checked automatically?

# Outline

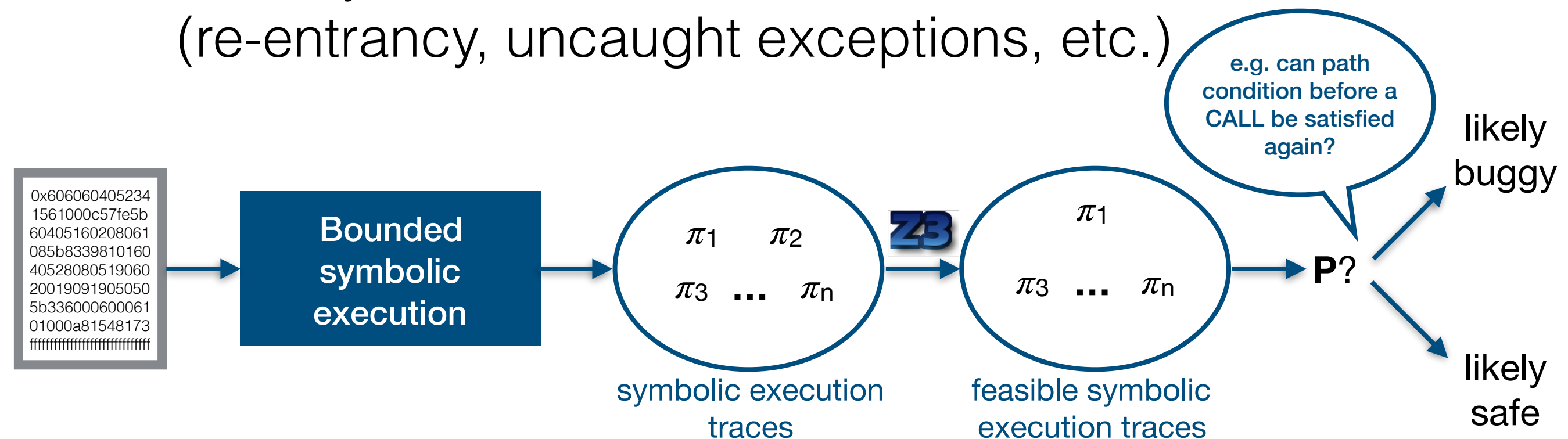
Introduction to Ethereum

Semantics of EVM bytecode

Static Analysis of EVM bytecode

# Oyente[1]

- Tool for finding common smart contract bugs in EVM bytecode (re-entrancy, uncaught exceptions, etc.)



- Evaluated on ~19000 real world contracts (low false positive rate: 6,4%)

# Oyente

- **Pros**

- Fast + scalable

- **Cons**

- Only works for pre-defined properties
- Produces false positives + false negatives

- Based on flawed semantics:  $\langle S, \sigma \rangle \rightarrow \langle S', \sigma' \rangle$

global state is assumed to be monotonically updated (never reverted) during execution

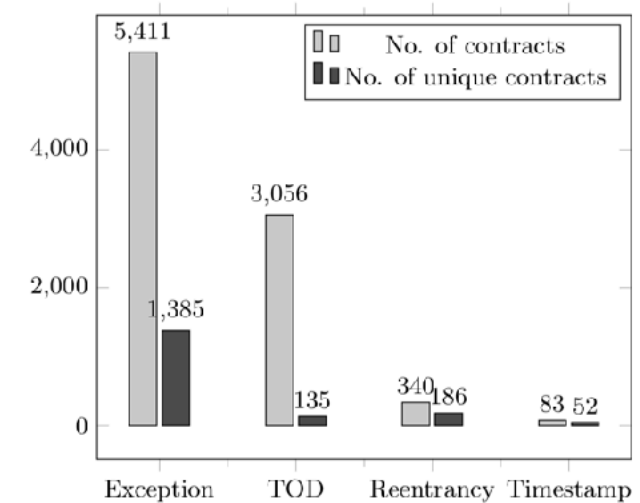


Figure 12: Number of buggy contracts per each security problem reported by OYENTE.

# Oyente

- **Pros**

*Fully Automated*

- Fast + scalable

- **Cons**

- Only works for pre-defined properties
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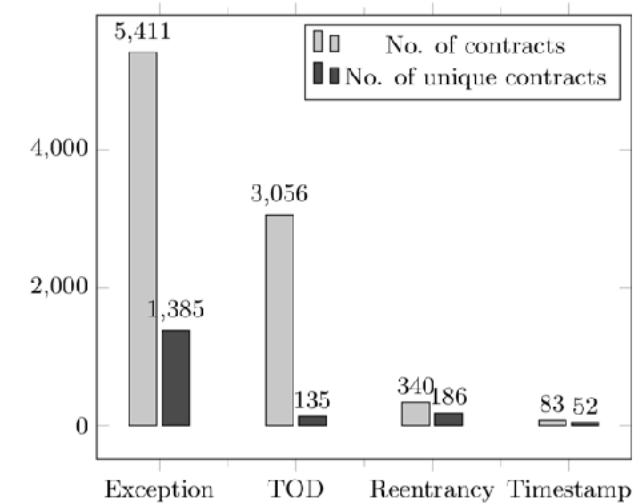


Figure 12: Number of buggy contracts per each security problem reported by OYENTE.

# Oyente

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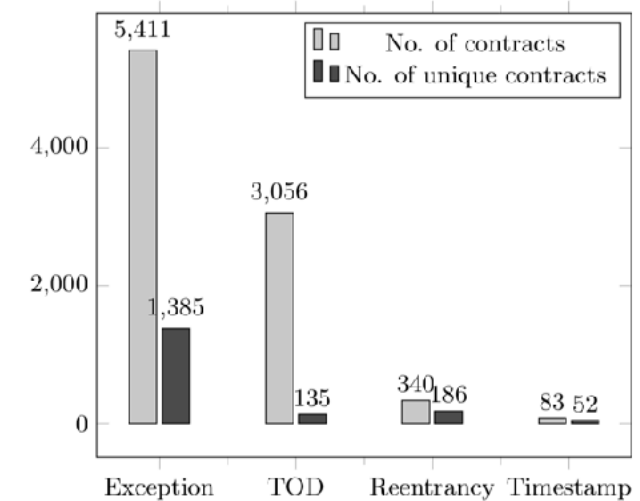


Figure 12: Number of buggy contracts per each security problem reported by OYENTE.

Not sound

# KEVM[2]

- Implementation of EVM bytecode semantics is in the  $\mathbb{K}$  framework (rewrite-based executable semantic framework)
- Analysis tools automatically derived from the semantics:
  - Semantic Debugger
  - Program Verifier (for reachability claims)



# KEVM

- **Pros**

- Based on fully fledged (and tested) semantics of EVM bytecode
- Allows for Hoare-style-like reasoning

- **Cons**

- Analysis tool requires the user to specify invariants (semi-automated)
- No domain-specific over-approximations (e.g. for calling unknown contracts)

# KEVM

- **Pros**



*Provably sound*

- Based on fully fledged (and tested) semantics of EVM bytecode
- Allows for Hoare-style-like reasoning

- **Cons**

- Analysis tool requires the user to specify invariants (semi-automated)
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# KEVM

- **Pros**

*Provably sound*

- Based on fully fledged (and tested) semantics of EVM bytecode
- Allows for Hoare-style-like reasoning

- **Cons**

*Only semi-automated*

- Analysis tool requires the user to specify invariants (semi-automated)
- No domain-specific over-approximations (e.g. for calling unknown contracts)

# KEVM

- **Pros**

*Sound by construction*

- Based on fully fledged (and tested) semantics of EVM bytecode
- Allows for Hoare-style-like reasoning

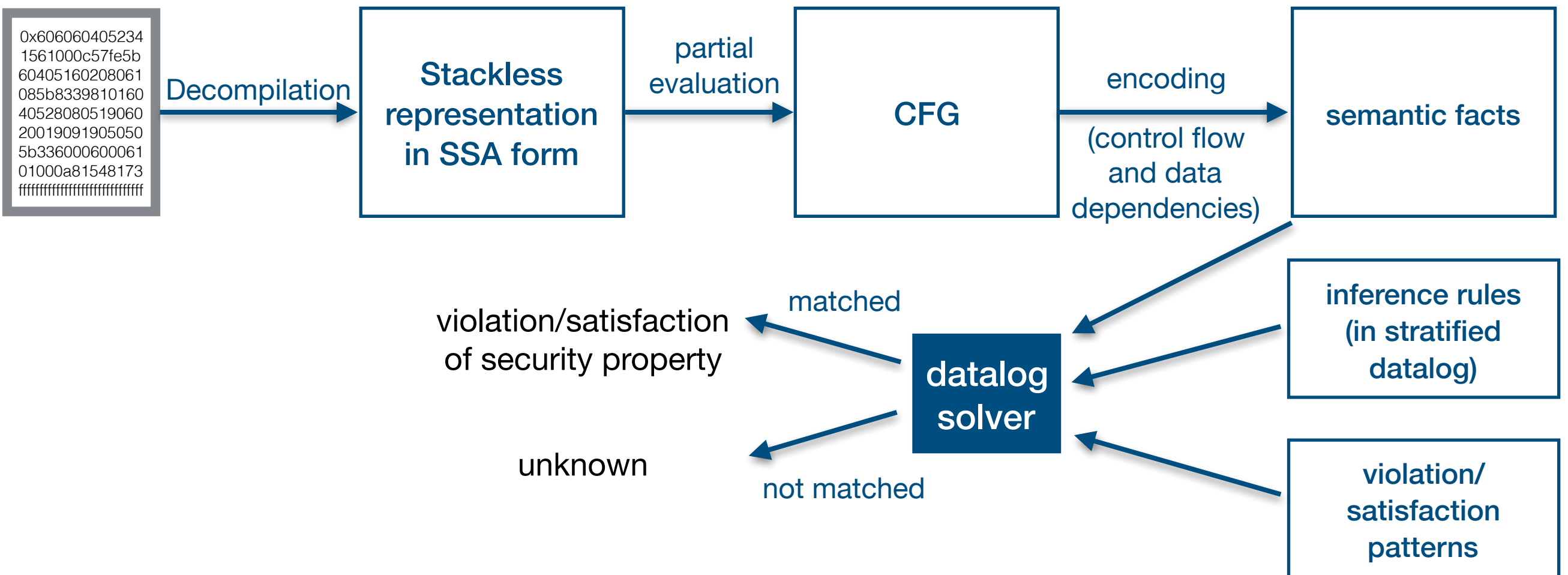
- **Cons**

*Only semi-automated*

- Analysis tool requires the user to specify invariants (semi-automated)
- No domain-specific over-approximations (e.g. for calling unknown contracts)

# Securify[3]

- Static smart contract analyser for EVM bytecode based on 'semantic fact checking'



- Evaluated on ~25000 real world contracts

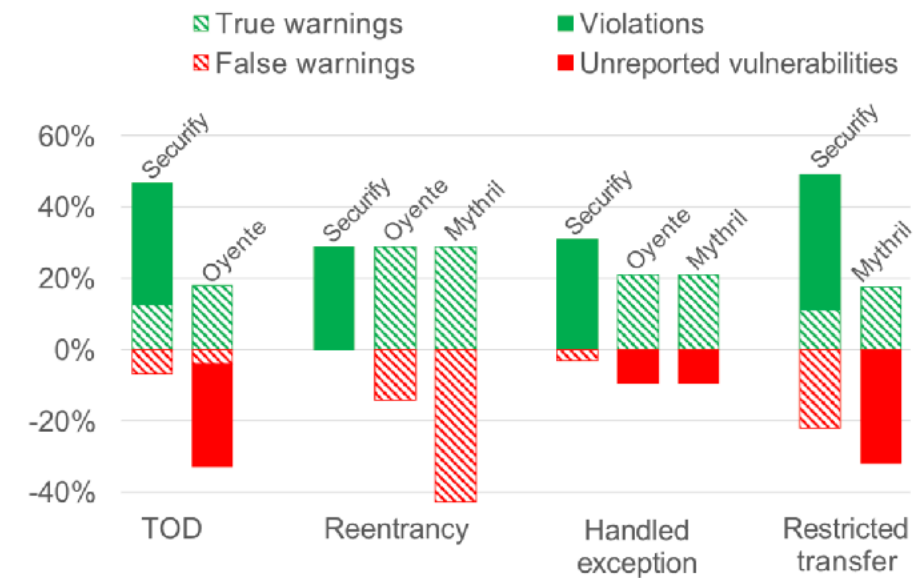
# Securify

- **Pros**

- Fast + scalable
- Shows good accuracy thanks to classification into (confirmed) violations and compliances

- **Cons**

- Decompilation is not guaranteed to succeed
- No soundness proof (neither for the dependency analysis nor for the security patterns)



# Securify

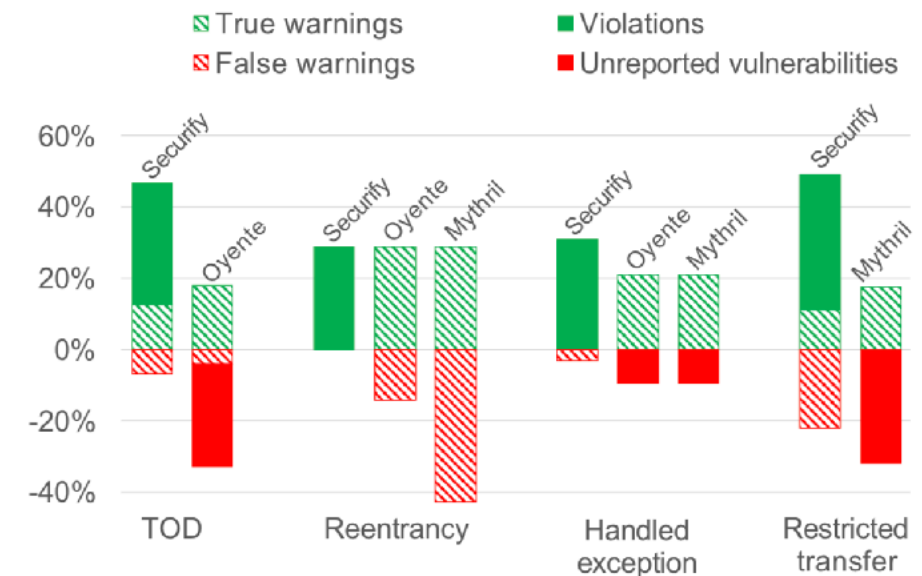
- **Pros**

*Fully Automated*

- Fast + scalable
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- **Cons**

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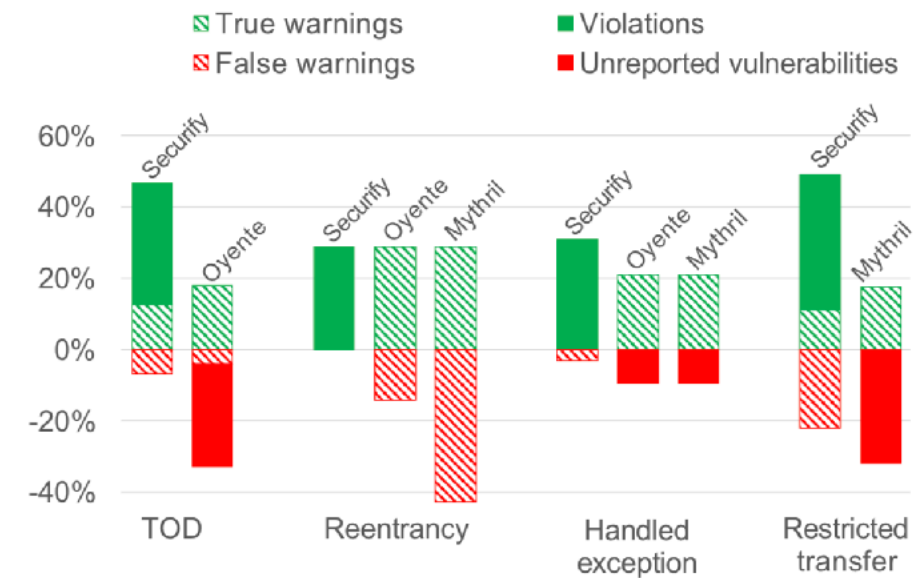


# Securify

- **Pros**

*Fully Automated*

- Fast + scalable
- Shows good accuracy thanks to classification into (confirmed) violations and compliances



- **Cons**

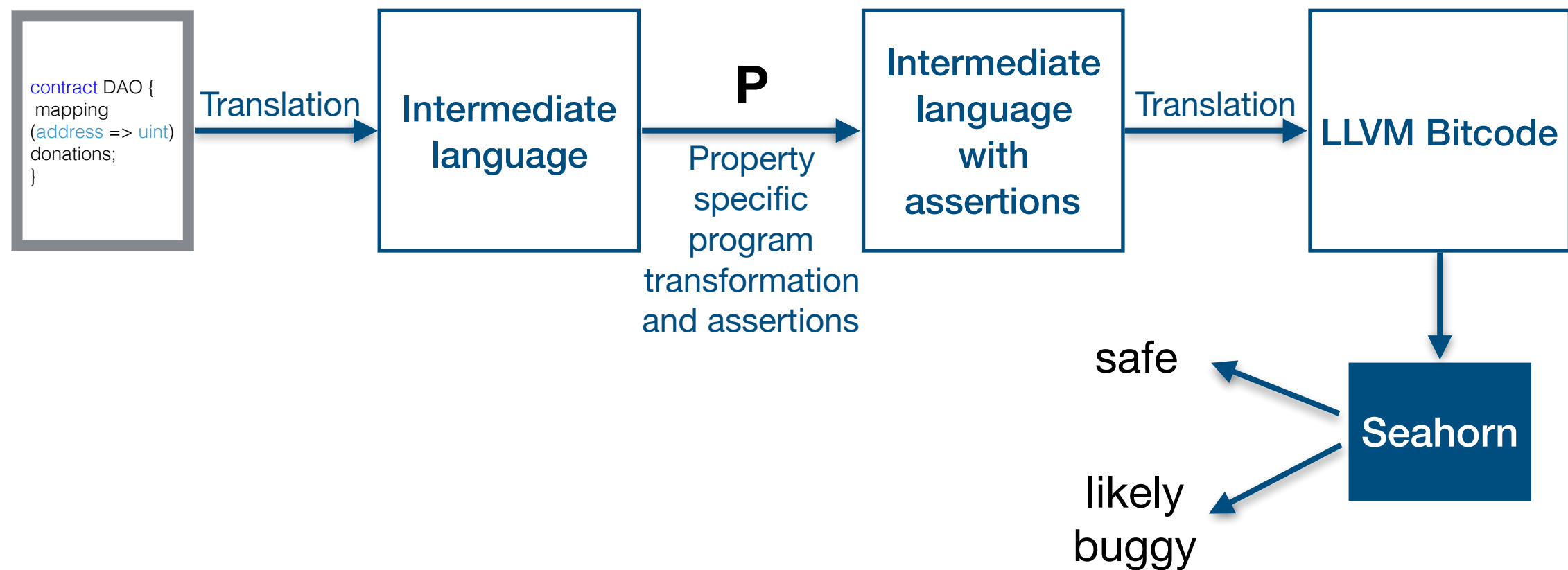
*No soundness proof*

- Decompilation is not guaranteed to succeed
- No soundness proof (neither for the dependency analysis nor for the security patterns)



# ZEUS[4]

- Static analyser for Solidity code



- Evaluated on ~22500 real-world contracts

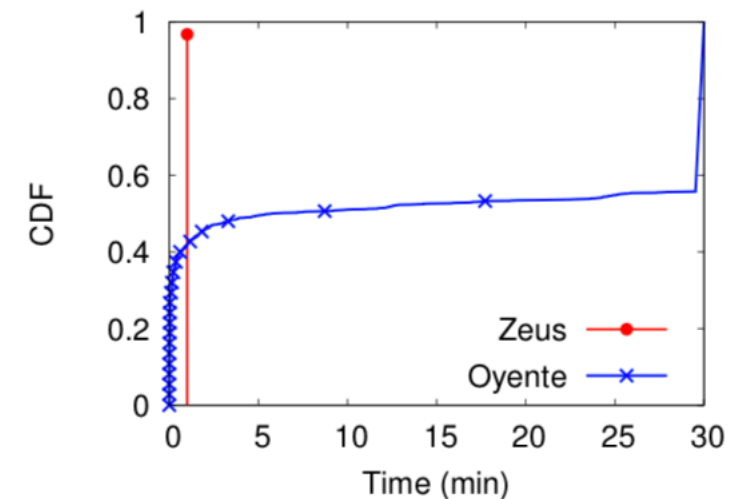
# ZEUS

- **Pros**

- Fast + scalable

- **Cons**

- Only works on Solidity code (not on bytecode)
- Only works for pre-defined properties
- Does not give soundness guarantees (transformations are not semantics preserving + security invariants are not proven sound)
- Based (as Oyente) on flawed semantics



(d) Verification time in minutes.

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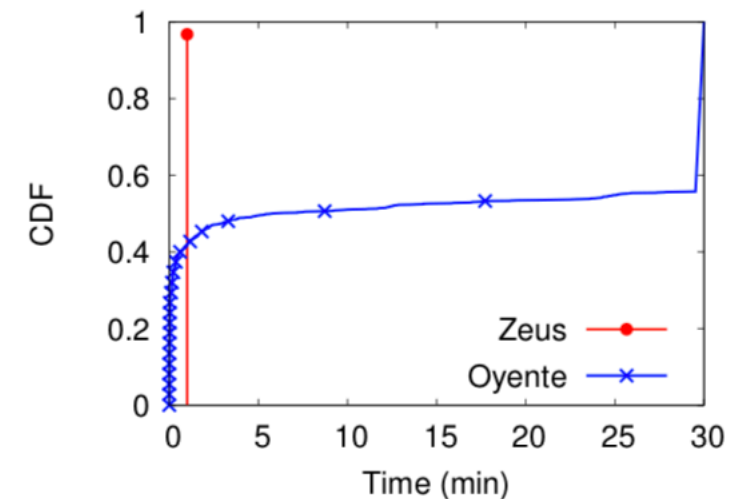
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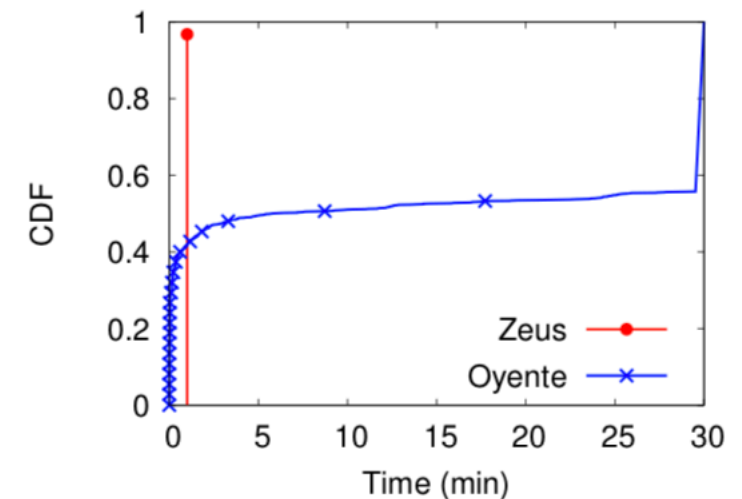
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# EtherTrust

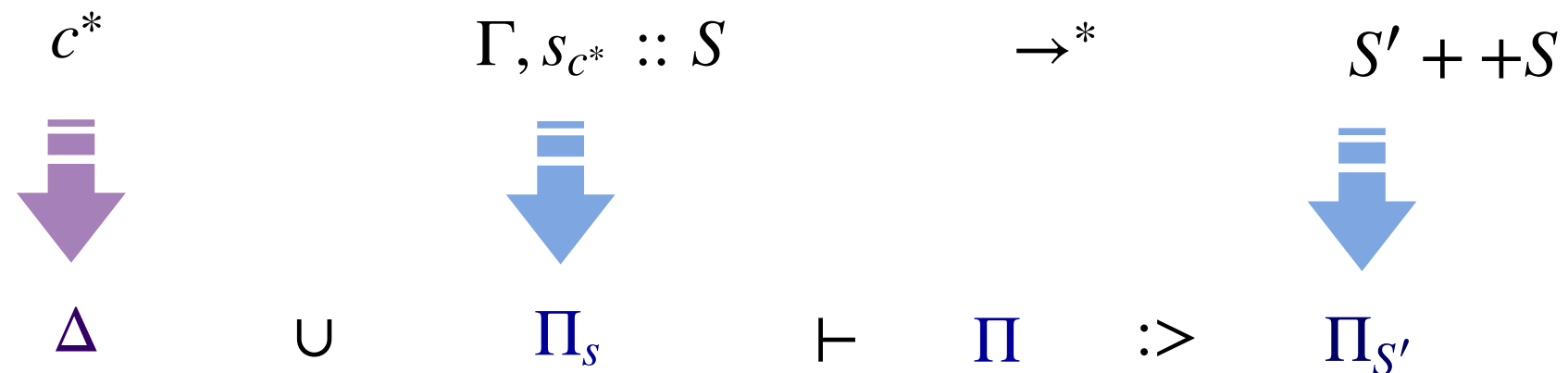
<https://www.netidee.at/ethertrust>

- First **provably sound** static analyzer for Ethereum smart contracts (i.e., it returns security guarantees)
  - previous ones focus on bug finding
- Outperforms the competitors in precision and performance
- **Reachability analysis**: suffices to check various interesting security properties

**Specific application domain abstractions:** T for unknown values,  $\alpha$  for address of running contract, abstract memory representation, and most notably *calls to unknown contracts*

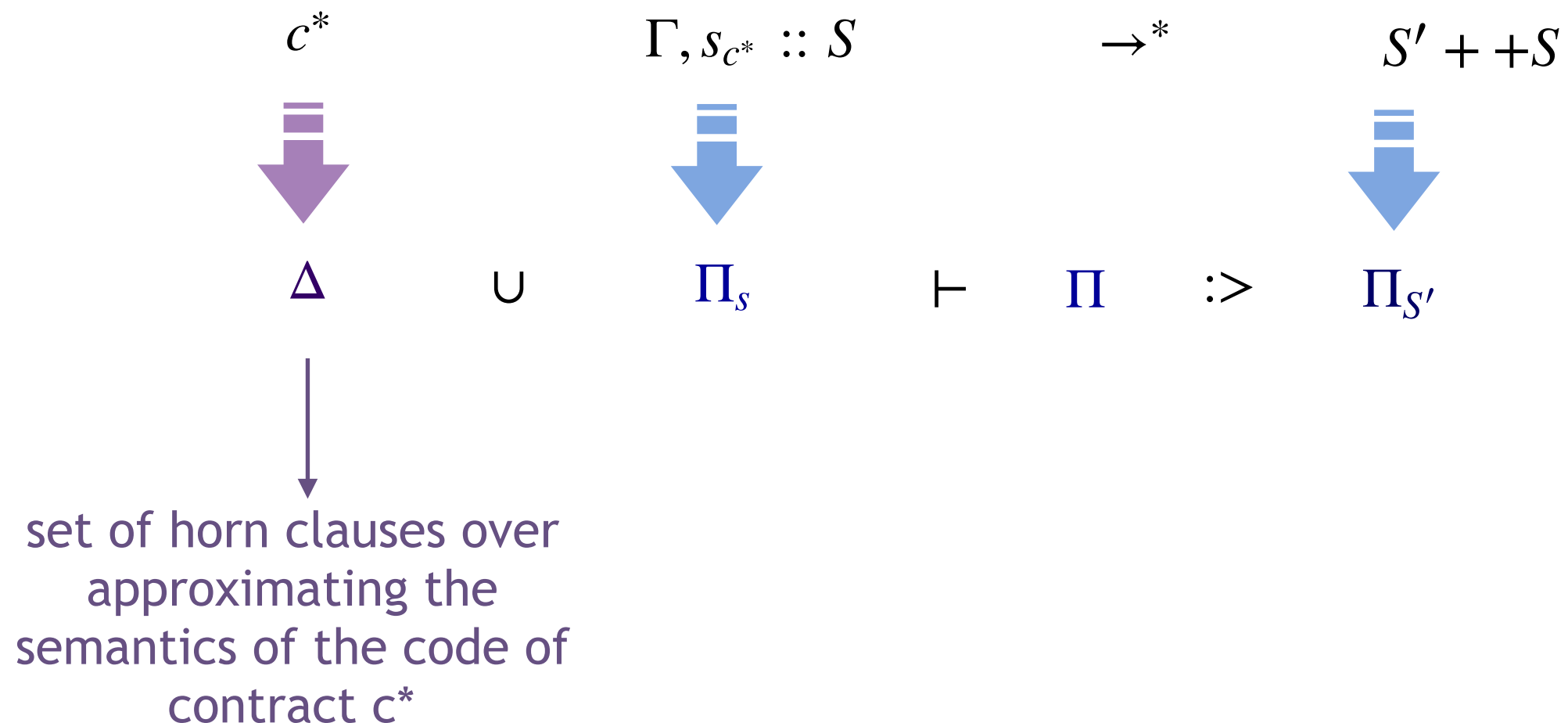
# Static analysis for Ethereum smart contracts

- Approach: abstract the EVM small-step semantics into Horn clauses that can be analysed using Z3



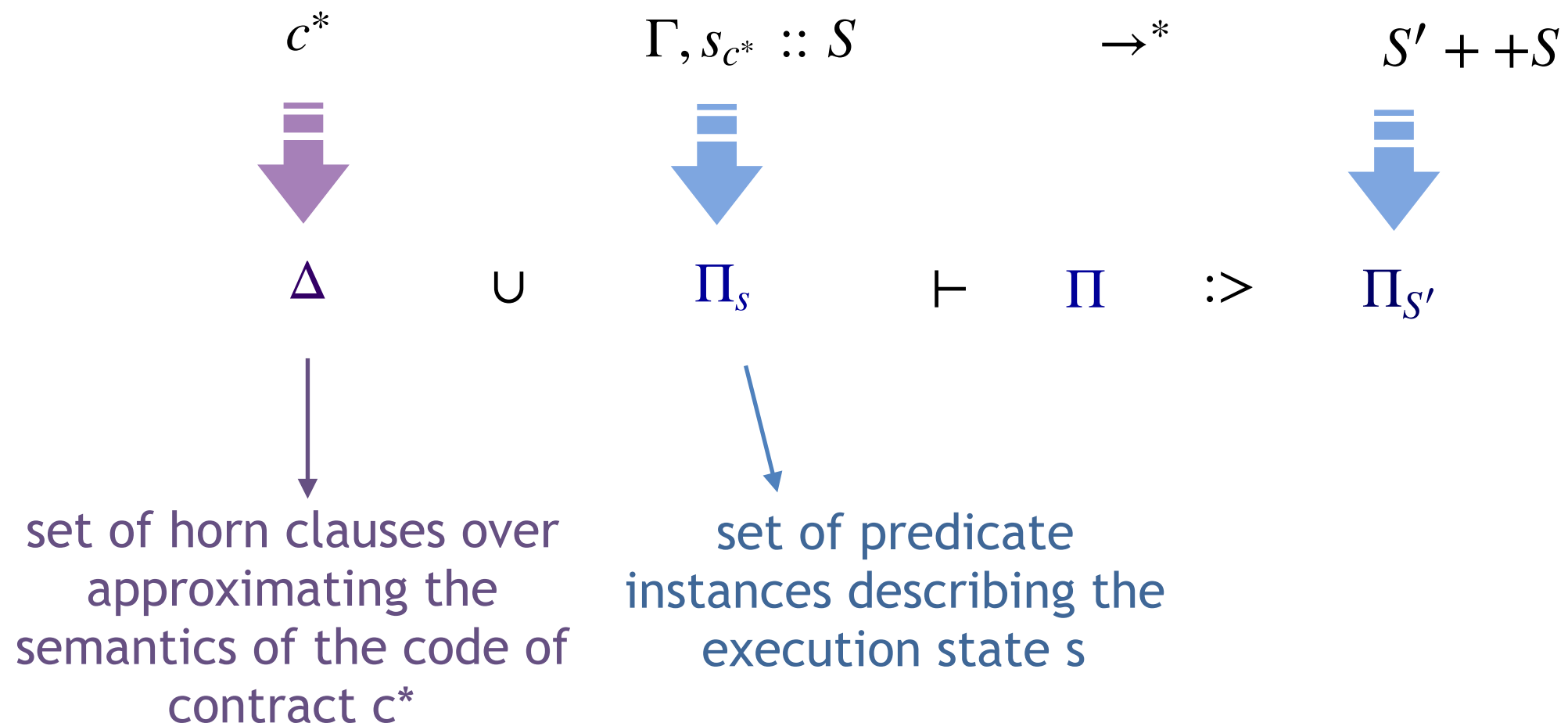
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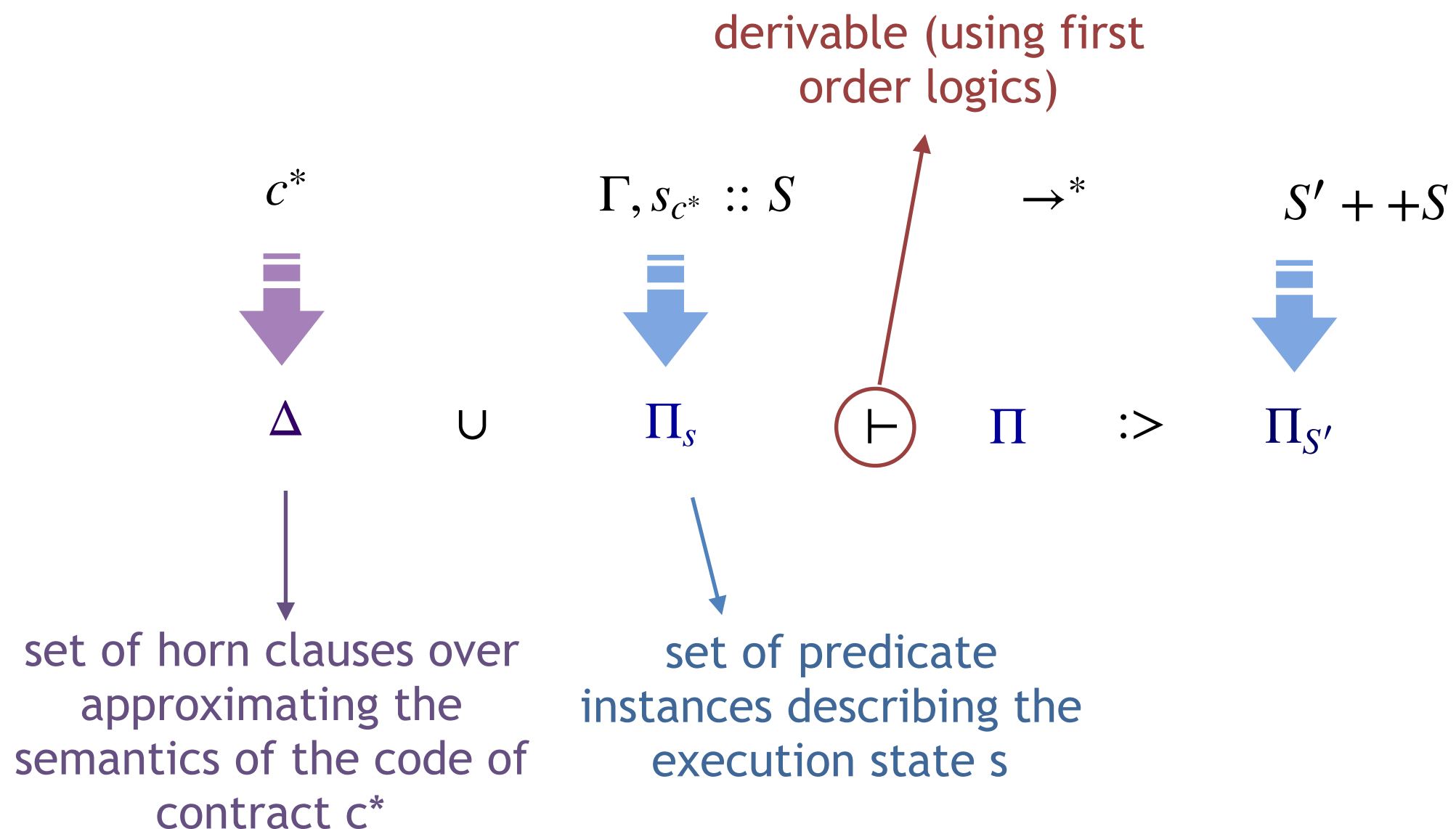
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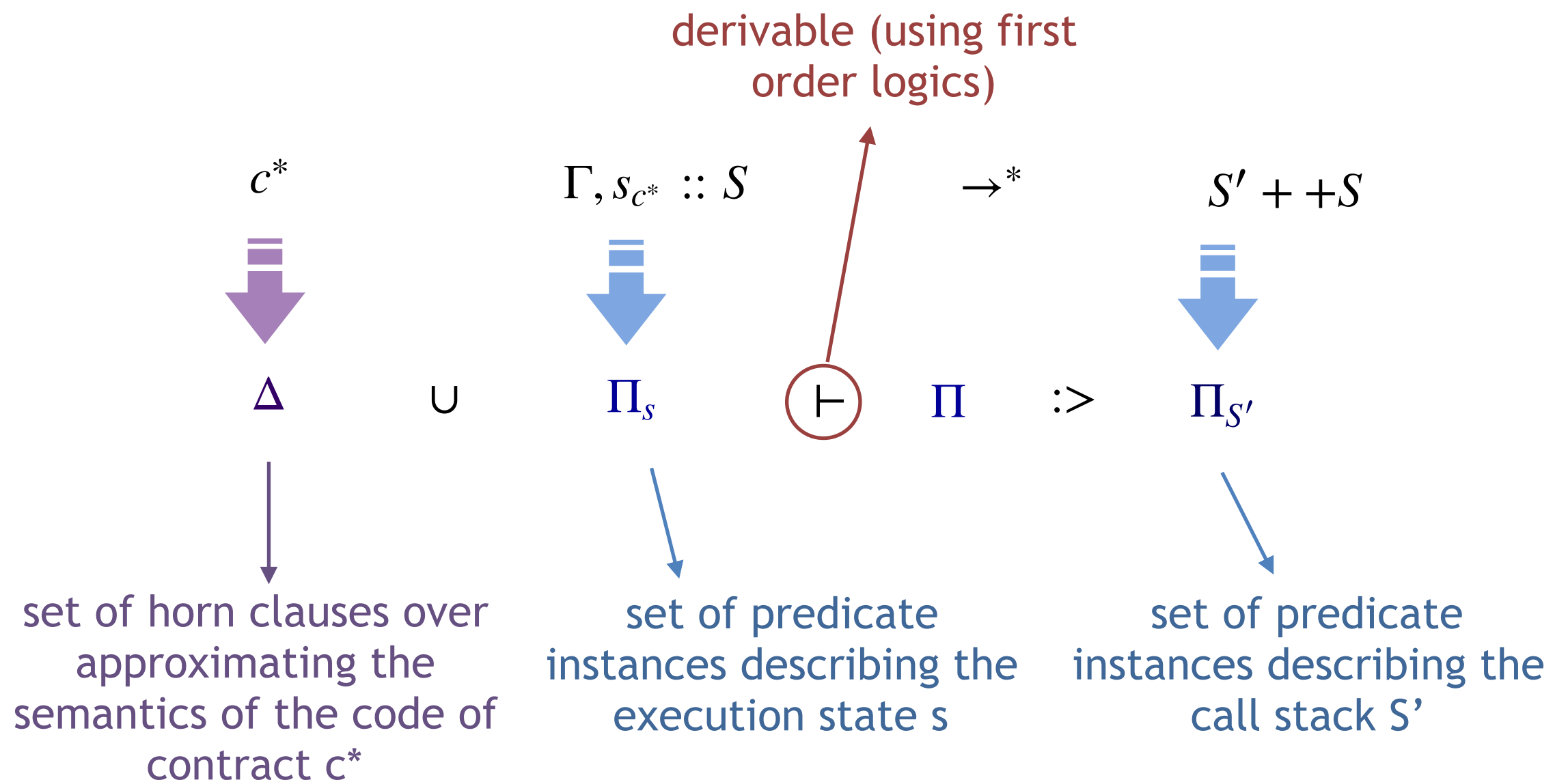
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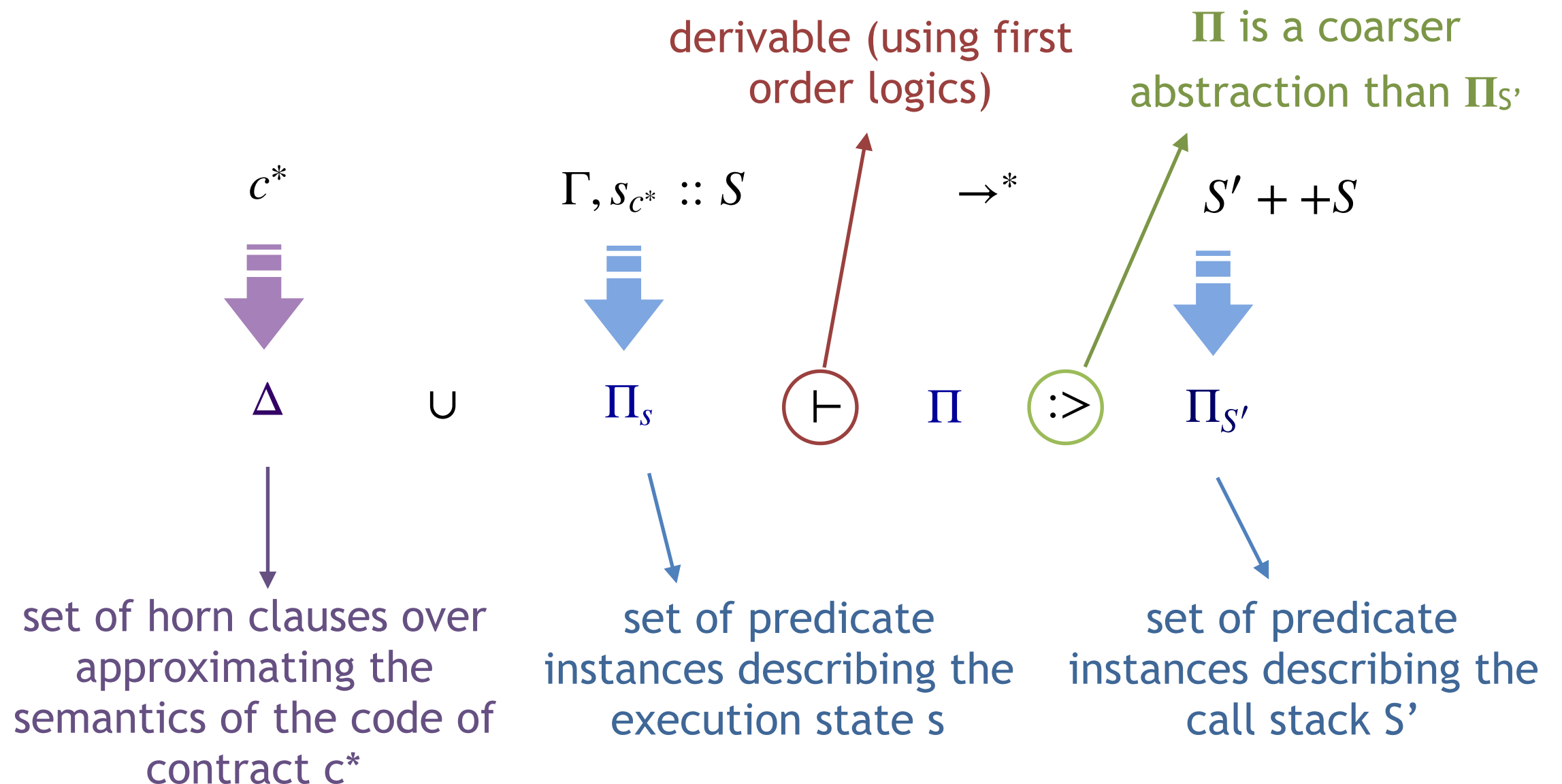
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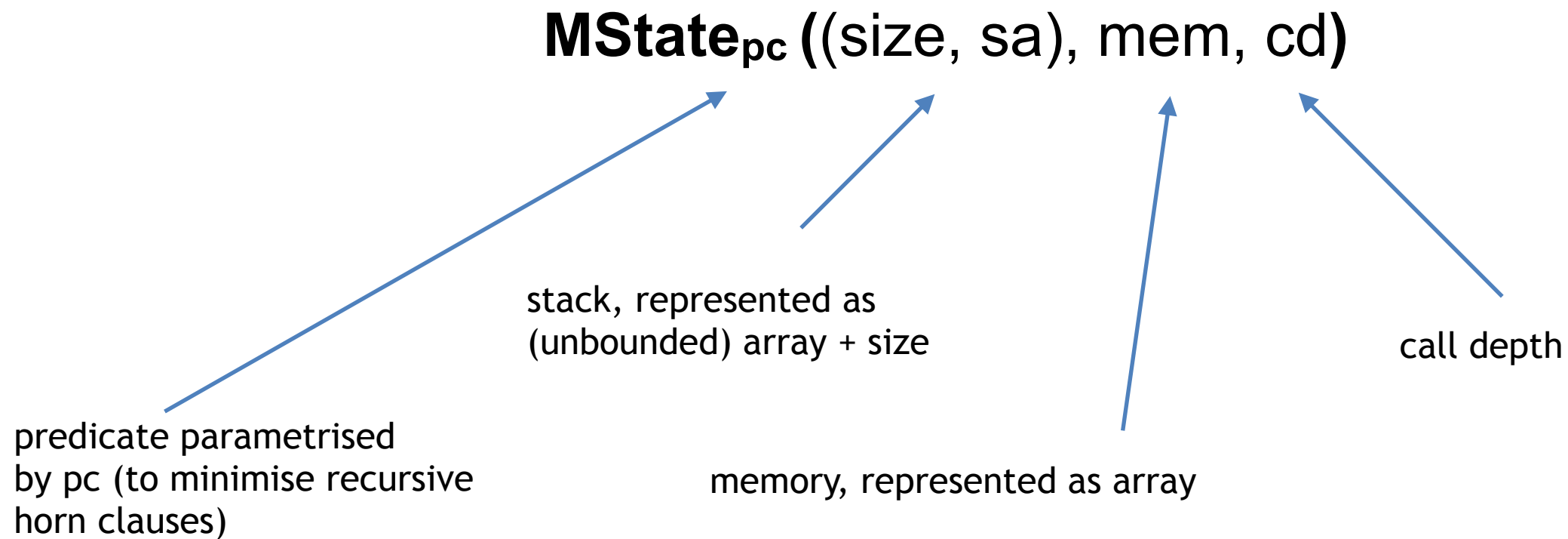


# Static analysis for Ethereum smart contracts

- Approach: abstract the EVM small-step semantics into Horn clauses that can be analysed using Z3



# State abstraction



- Similar predicates for
  - global state
  - execution environment

# Horn clause encoding

- Execution steps modelled as Horn clauses
  - Horn clauses are generated according to the opcodes located at each pc
  - Example: Machine state rule for pc with opcode **ADD**

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**MState**<sub>pc</sub>((size, sa), aw, cd)

$\wedge \text{size} \geq 2$

$\wedge x = \text{sa}[\text{size}-1]$

$\wedge y = \text{sa}[\text{size}-2]$

$\Rightarrow \mathbf{MState}_{pc+1}((\text{size}-1, \text{sa}[\text{size}-2 \rightarrow x+y]), \text{mem}, \text{cd})$

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$\wedge \text{size} \geq 2$   simple range check

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It's a bit more complicated  
than that

# Abstract Domain

$$\text{MState}_{pc} ((size, \boxed{sa}), ma, cd) \\ \in \mathbb{N} \rightarrow \hat{D}$$

**Abstract domain**  $\hat{D} = \mathbb{Z} \cup \{\alpha\} \cup \{\top\}$

represents  
concretely known  
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represents the  
address of the  
account under  
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represents all  
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# Abstract Domain

$$\text{MState}_{pc} ((size, \boxed{sa}), ma, cd) \\ \in \mathbb{N} \rightarrow \hat{D}$$

Common technique  
from abstract  
interpretation

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TIMESTAMP, PUSH 2, ADD ?

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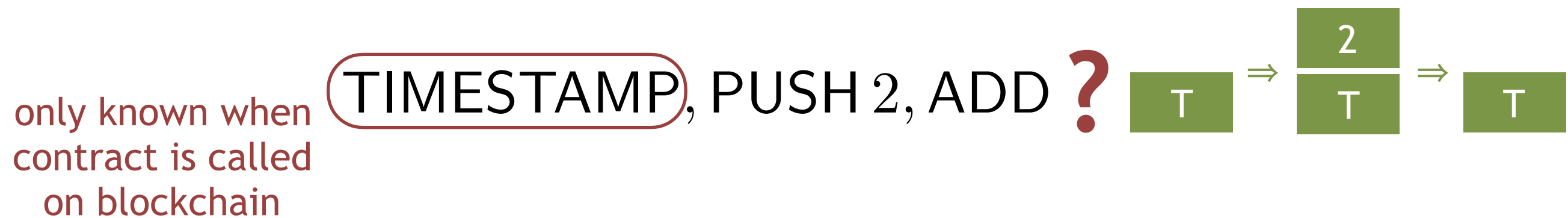
- There are a lot of values that we do not know statically:

only known when  
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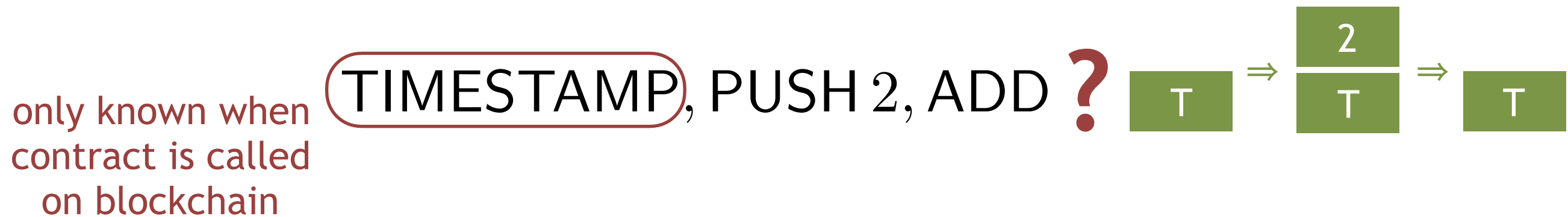
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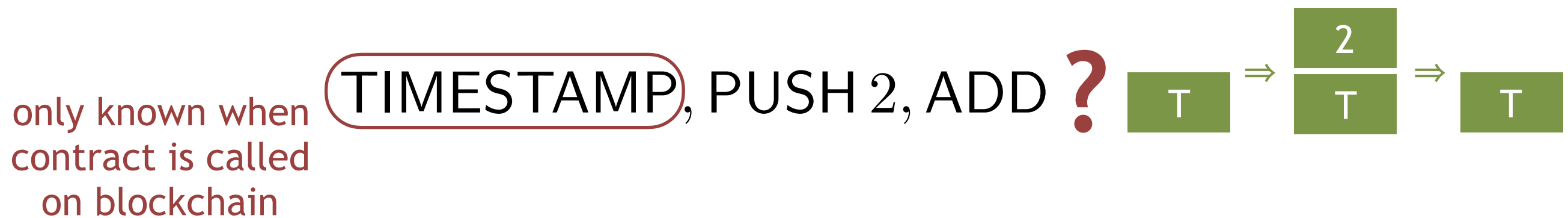


- Sometimes we still want to be precise:

ADDRESS, BALANCE

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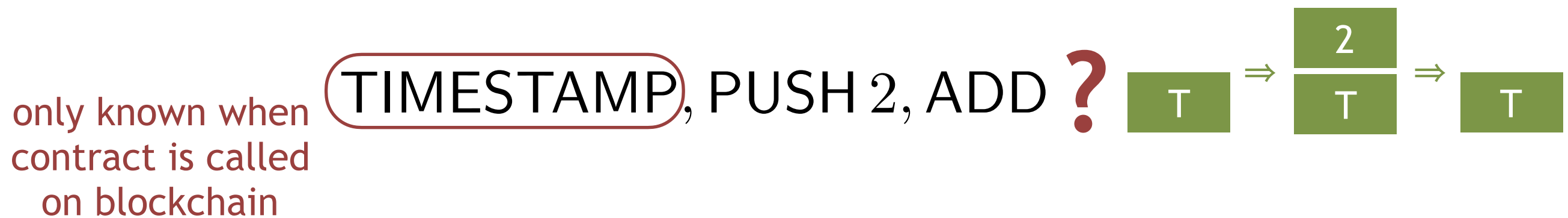
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takes address as argument and returns the balance of the corresponding account

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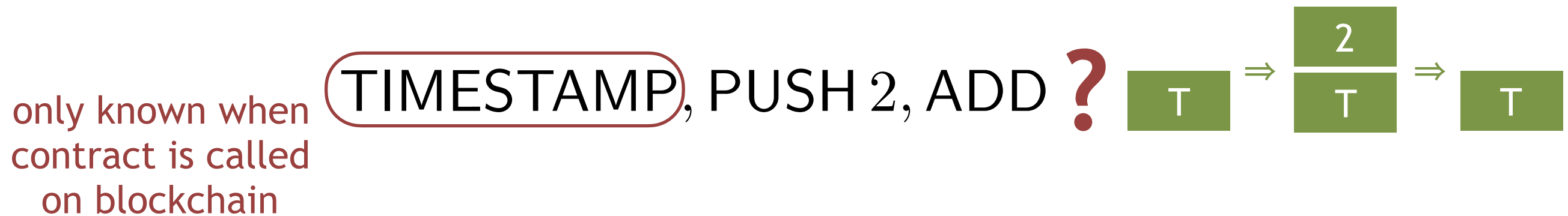
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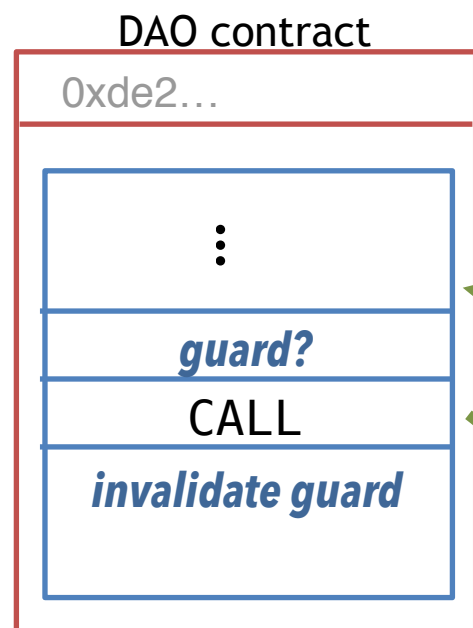
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# Abstracting calls - Intuition

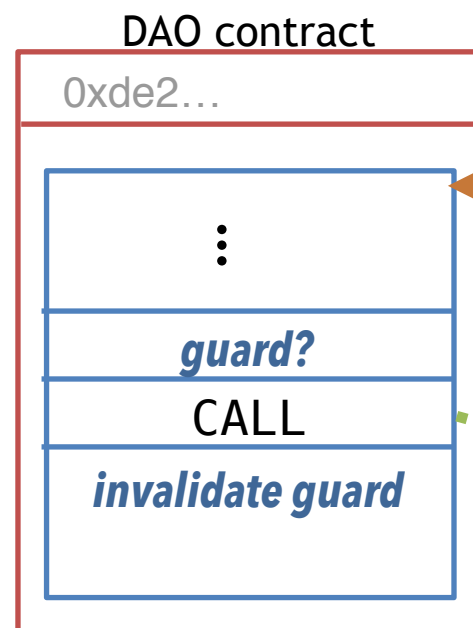
- For analysing a specific contract all its executions need to be approximated

tight approximation for  
call depth **0**

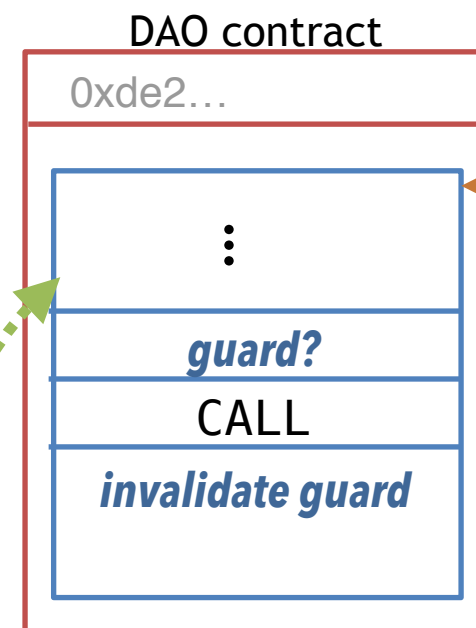


**x**

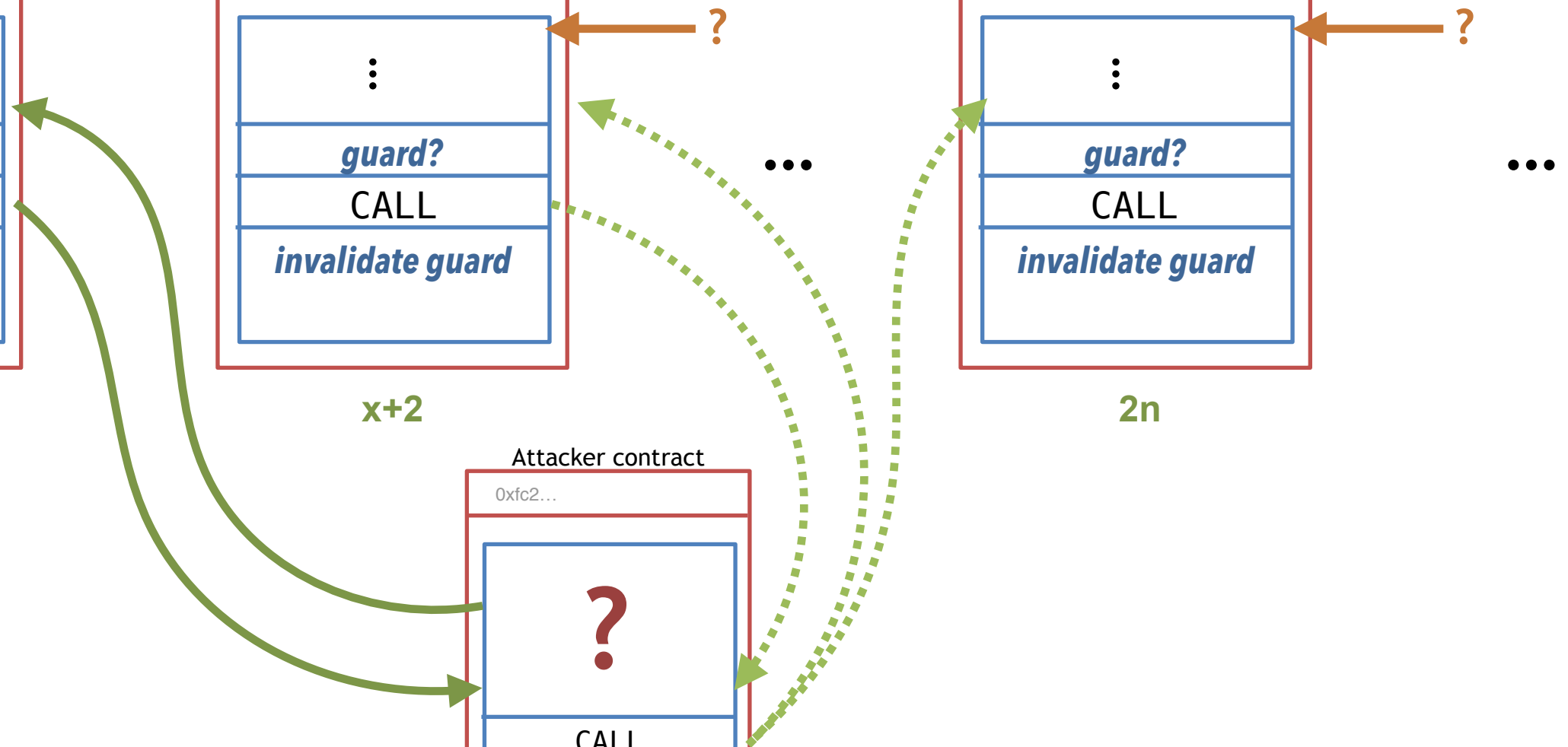
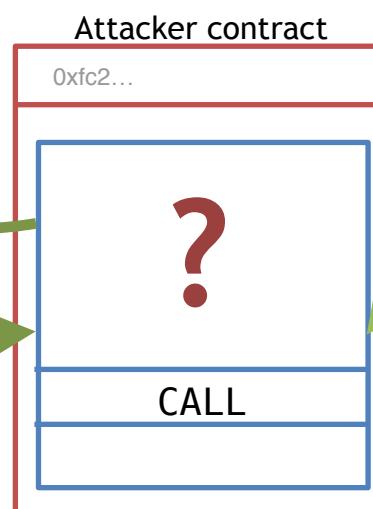
coarse approximation for  
call depth **y > 0**



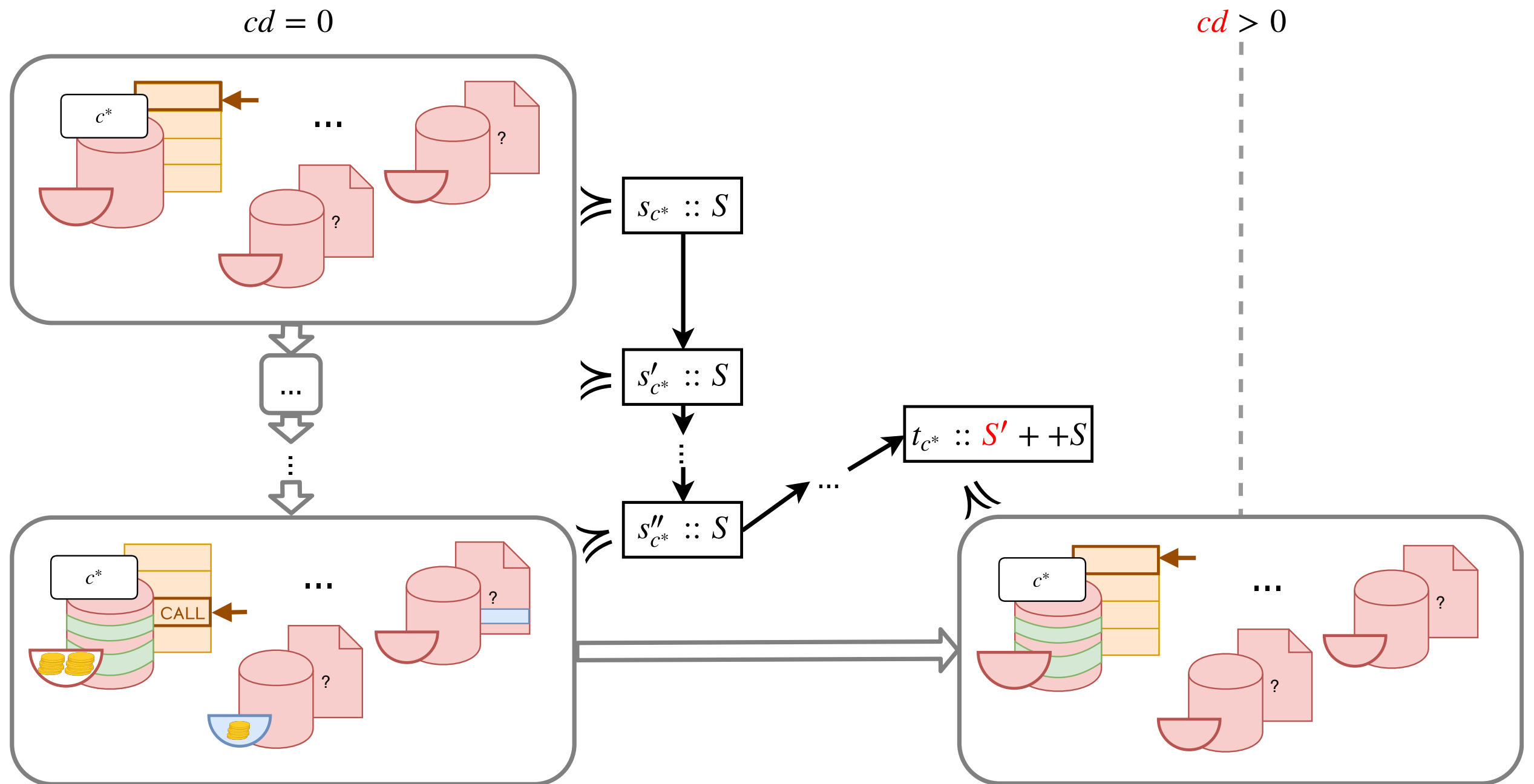
**x+2**



**2n**



# Abstract semantics - Call rule



# Abstract semantics - Call rule

preconditions are checked: enough elements on the stack, enough gas

$$\text{MState}_{pc} ((size, sa), ma, cd) \wedge size > 3 \wedge \hat{va} = sa[size - 2] \wedge \hat{va} \leq \hat{b} \\ \wedge \text{GState}_{pc} (\alpha, \hat{b}, sta, cd) \wedge \boxed{cd' > cd} \Rightarrow \text{MState}_0 (\boxed{(0, \lambda x. \top)}, \boxed{\lambda x. 0}, cd')$$

contract might be reentered  
at an arbitrarily higher call  
depth

execution starts at pc 0 in fresh  
machine state:  
empty stack + memory  
initialised to all zeros

$$\text{MState}_{pc} ((size, sa), ma, cd) \wedge size > 3 \wedge \hat{va} = sa[size - 2] \wedge \hat{va} \leq \hat{b} \\ \wedge \text{GState}_{pc} (\alpha, \hat{b}, sta, cd) \wedge cd' > cd \Rightarrow \text{ExEnv} (\boxed{\alpha}, \boxed{\top}, cd')$$

when reentering the active account at the  
point of calling is (still) the actor

the input to the reentering  
call is unknown

# Abstract semantics - Call rules

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the global storage of the  
active account is preserved

the balance might be  
arbitrarily changed

$$\text{MState}_{pc}((size, sa), ma, cd) \wedge size > 3 \wedge \hat{va} = sa[size - 2] \wedge \text{GState}_{pc}(\alpha, \hat{b}, sta, cd) \\ \wedge \hat{va} \leq \hat{b} \wedge \text{GState}_{pc}(\dot{a}, \hat{b}^*, sta^*, cd) \wedge \boxed{\dot{a} \neq \alpha} \wedge cd' > cd \Rightarrow \text{GState}_0(\dot{a}, \top, \boxed{[\top]}, cd')$$

all addresses different from the actor can have  
arbitrary storage (all positions mapped to T)

This is actually an artefact: the storage of other accounts but the  
active account cannot be accessed anyways given that only plain calls  
are executed



# Checking for single-entrancy

- How to check for single-entrancy now?
- Simple example:

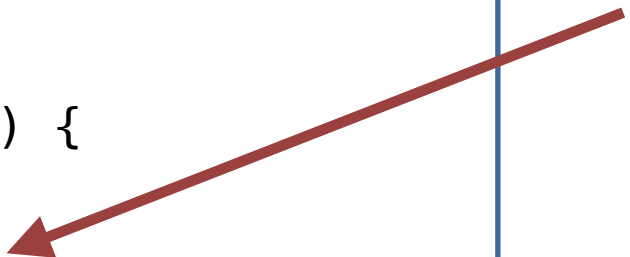
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contract Bob {  
    bool sent = false;  
  
    function ping(address c) {  
        if (!sent){  
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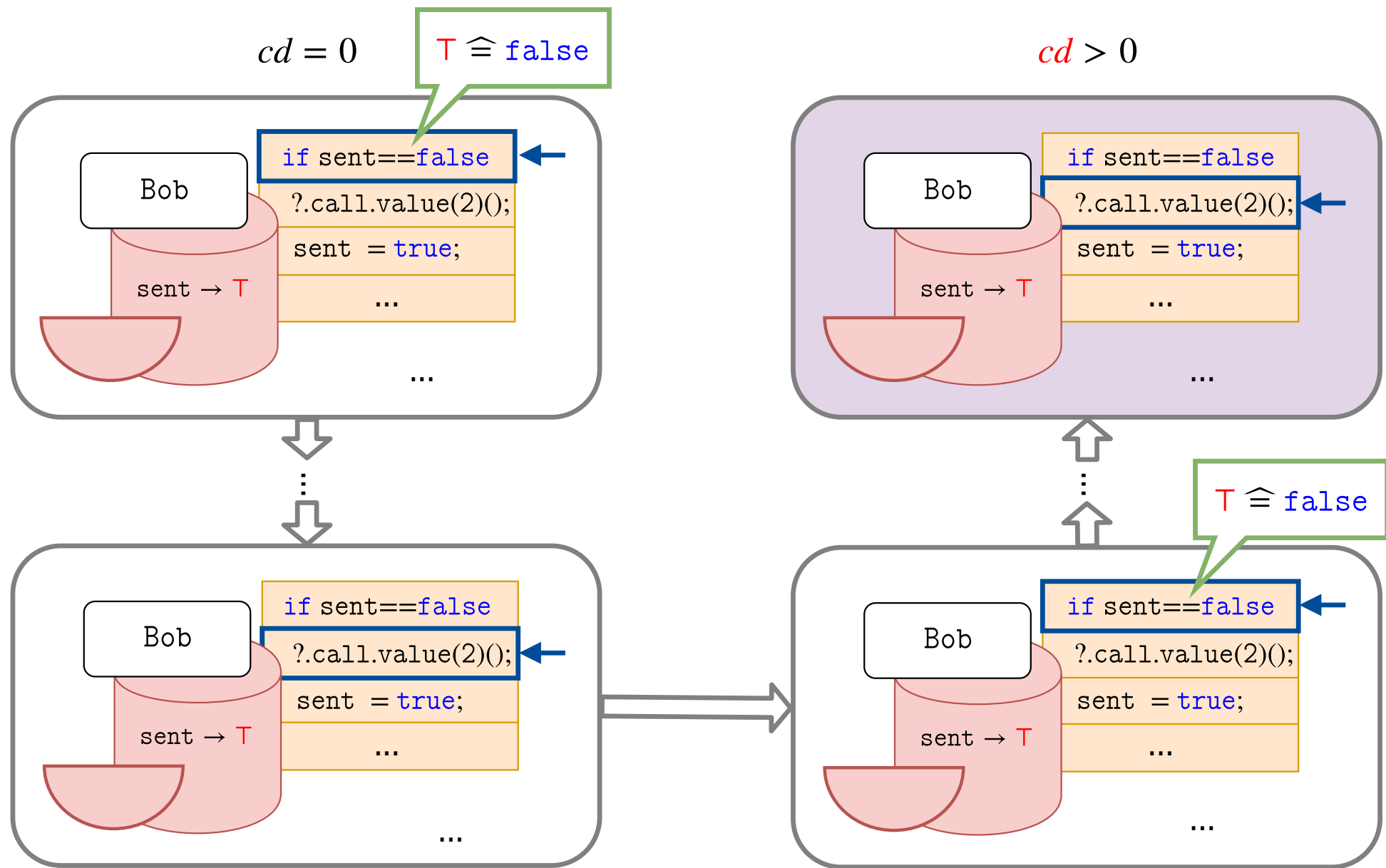
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Can it ever happen that we  
execute this call while re-  
entering?

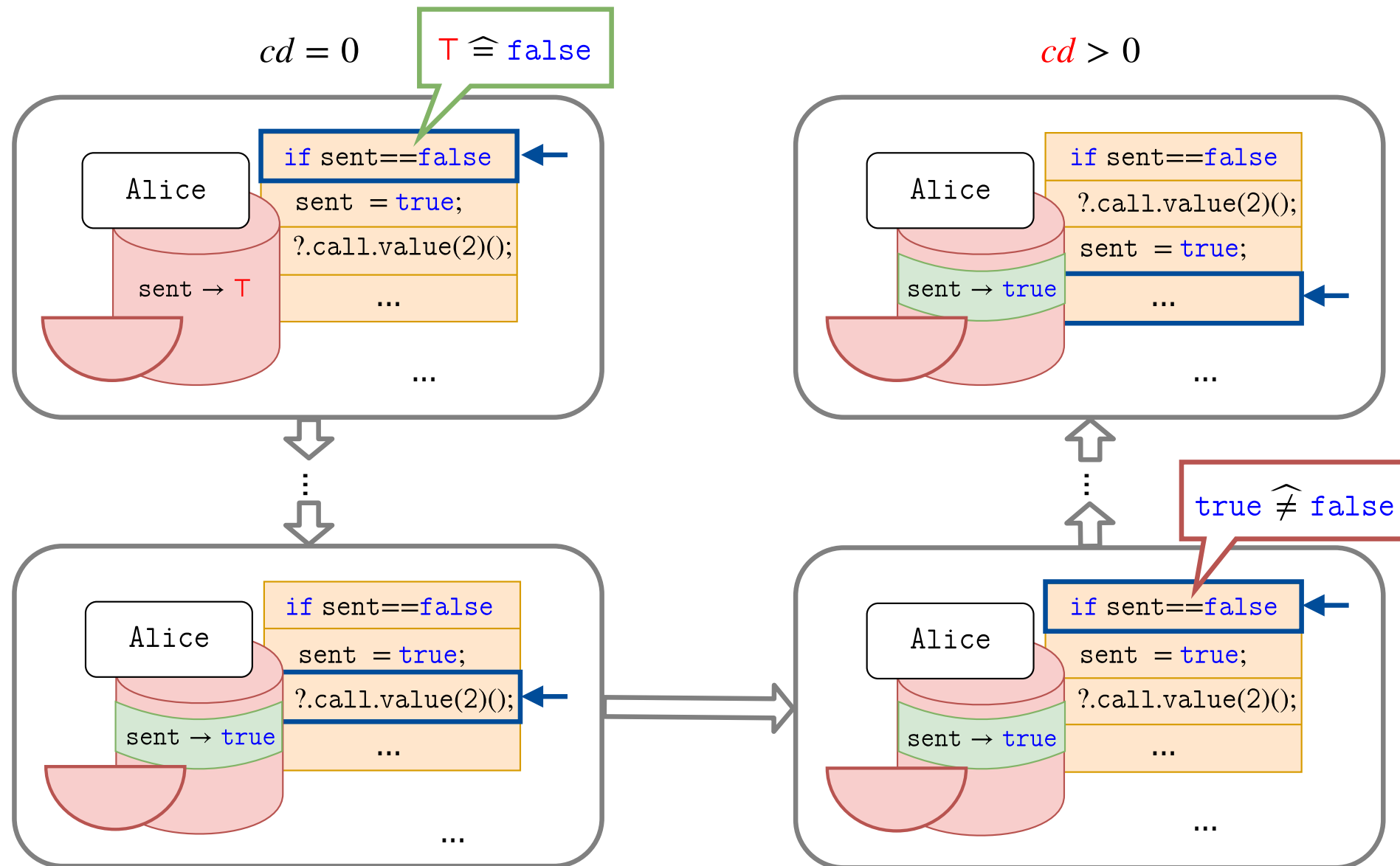
# Detecting reentrancy



Reachability query



# Proving single-entrancy



Reachability query



# EtherTrust

- Approach scales to full EVM bytecode!
- We implemented **EtherTrust** - a tool for static analysing Ethereum bytecode



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Average running time: much faster than the best state-of-the-art bug finding tool... and sound!

10k	$\Sigma$	# ter. SE	# $\overline{SE}$	# ter. MI	# $\overline{MI}$	$\emptyset t$
O	148	18	12	(18)	3	26,5
ET		100	4	107	2	2,8

SE: Single entrancy

MI: Independence of miner controlled state

#X: Number of contracts reported to violate X

#ter. X: Number of contracts for which the analysis terminates

O: Oyente (state-of-the-art) bug finder

ET: EtherTrust

# Simplifications in this tutorial

- Simplified gas treatment (constant gas cost of 1)
- Inherent exception propagation (all available gas is given to the caller)
- Simplified memory treatment (only memory cells are accessed, never fragments; word indexed memory)
- computations on logical (instead of bounded) integers
- No limits on call stack and machine stack
- Some interesting opcodes are omitted (DELEGATECALL, CALLCODE, **CREATE**, ...)



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# We are hiring PhDs and Postdocs!



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artificial intelligence**

**cyber-physical  
systems**

**computer-aided  
verification**

**distributed  
systems**

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M. Maffei | M. Ortiz | U. Schmid | M. Seidl  
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### HOW TO APPLY

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<http://logic-cs.at/phd>

The applicants are expected to have completed an excellent diploma or master's degree in computer science, mathematics, or a related field. Applications by the candidates can be submitted on continuous basis till October 2018 until all positions are filled.



# Handling abstract values

- Abstract operations:
- Abstract comparisons:

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- Abstract operations:

$$n \hat{+} m := n + m$$

$$\hat{v} \hat{+} \top := \top$$

$$\top \hat{+} \hat{v} := \top$$

$$\hat{v} \hat{+} \alpha := \top$$

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No constraints are collected for computations with  $\top$

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$$\alpha \hat{=} \hat{v} := \{true, false\}$$

Comparisons with unknown values evaluate to both true and false



# Abstract ADD - revisited

$\text{MState}_{pc}((size, sa), ma, cd)$

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$\text{MState}_{pc}((size, sa), ma, cd)$

$\Rightarrow \text{Exc}(cd)$



abstract operations are used!



# Abstract Memory access

$$ma \in \hat{D}/\{\alpha\} \rightarrow \hat{D}$$



Memory positions  
can't be  $\alpha$



Memory values  
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## MSTORE

$\text{MState}_{pc}((size, sa), ma, cd)$

$\wedge size > 1$

$\wedge \hat{x} = sa[size - 1]$

$\wedge \hat{p} = (\hat{x} = \alpha) ? \top : \hat{x}$

$\wedge \hat{y} = sa[size - 2]$

$\Rightarrow \text{MState}_{pc+1}((size - 2, sa), ma[\hat{p} \rightarrow \hat{y}], cd)$

# Abstract Memory access

$$ma \in \hat{D}/\{\alpha\} \rightarrow \hat{D}$$



Memory positions  
can't be  $\alpha$



Memory values  
come from the  
abstract domain

## MSTORE

$\text{MState}_{pc}((size, sa), ma, cd)$

$\wedge size > 1$

$\wedge \hat{x} = sa[size - 1]$

$\wedge \hat{p} = ((\hat{x} = \alpha) ? \top : \hat{x})$

$\wedge \hat{y} = sa[size - 2]$

$\Rightarrow \text{MState}_{pc+1}((size - 2, sa), ma[\hat{p} \rightarrow \hat{y}], cd)$

Instead of writing to  $\alpha$ ,  
we write to  $\top$

writing to  $\top$  means  
“writing everywhere”

# Abstract Memory access

$$ma \in \hat{D}/\{\alpha\} \rightarrow \hat{D}$$



Memory positions  
can't be  $\alpha$



Memory values  
come from the  
abstract domain

**MSTORE**

**MLOAD**

$\text{MState}_{pc}((size, sa), ma, cd)$

$\wedge size > 1$

$\wedge \hat{x} = sa[size - 1]$

$\wedge \hat{p} = ((\hat{x} = \alpha) ? \top : \hat{x})$

$\wedge \hat{y} = sa[size - 2]$

$\Rightarrow \text{MState}_{pc+1}((size - 2, sa), ma[\hat{p} \rightarrow \hat{y}], cd)$

$\text{MState}_{pc}((size, sa), ma, cd)$

$\wedge size > 0$

$\wedge sa[size - 1] \in \{\alpha, \top\}$

$\Rightarrow \text{MState}_{pc+1}((size - 2, sa[size - 1 \rightarrow \top]), ma, cd)$

Instead of writing to  $\alpha$ ,  
we write to  $\top$

writing to  $\top$  means  
“writing everywhere”

# Abstract Memory access

$$ma \in \hat{D}/\{\alpha\} \rightarrow \hat{D}$$



Memory positions  
can't be  $\alpha$



Memory values  
come from the  
abstract domain

## MSTORE

$$\text{MState}_{pc}((size, sa), ma, cd)$$

$$\wedge size > 1$$

$$\wedge \hat{x} = sa[size - 1]$$

$$\wedge \hat{p} = ((\hat{x} = \alpha) ? \top : \hat{x})$$

$$\wedge \hat{y} = sa[size - 2]$$

$$\Rightarrow \text{MState}_{pc+1}((size - 2, sa), ma[\hat{p} \rightarrow \hat{y}], cd)$$

Instead of writing to  $\alpha$ ,  
we write to  $\top$

writing to  $\top$  means  
“writing everywhere”

## MLOAD

$$\text{MState}_{pc}((size, sa), ma, cd)$$

$$\wedge size > 0$$

$$\wedge sa[size - 1] \in \{\alpha, \top\}$$

$$\Rightarrow \text{MState}_{pc+1}((size - 2, sa[size - 1 \rightarrow \top]), ma, cd)$$

Instead of “reading from  
everywhere”, we simply  
read  $\top$

# Abstract Memory access - continued

$\text{MState}_{pc} ((size, sa), ma, cd)$

$\wedge size > 0$

$\wedge n = sa[size - 1]$

$\Rightarrow \text{MState}_{pc+1} ((size, sa[size - 1 \rightarrow ma[n]]), ma, cd)$

## **MLOAD**

$\text{MState}_{pc} ((size, sa), ma, cd)$

$\wedge size > 0$

$\wedge n = sa[size - 1]$

$\Rightarrow \text{MState}_{pc+1} ((size, sa[size - 1 \rightarrow ma[\top]]), ma, cd)$

# Abstract Memory access - continued

$\text{MState}_{pc} ((size, sa), ma, cd)$

$\wedge size > 0$

$\wedge n = sa[size - 1]$

$\Rightarrow \text{MState}_{pc+1} ((size, sa[size - 1 \rightarrow ma[n]]), ma, cd)$

## MLOAD

$\text{MState}_{pc} ((size, sa), ma, cd)$

$\wedge size > 0$

$\wedge n = sa[size - 1]$

$\Rightarrow \text{MState}_{pc+1} ((size, sa[size - 1 \rightarrow ma[\boxed{\top}]]), ma, cd)$

When reading the memory at a concrete position, we additionally need to read from  $\top$ , as there we can find the values that have been written everywhere